

let a = 5,
b = 10: a: 5 b: 10.

let f = lam(x): x + a end:
f(1)

lam(x): if false: a
else: x + 1
end
end

PROVABILITY

def f(i): lambda: i
map(f, range(0, 10))

TRUTH

for i in range(0, 10):
l.append(lambda: i)

interp(e) $\rightarrow v_1$
 \downarrow
 e_1

interp(swap(e, x, y)) $\rightarrow v_2$
 \downarrow
 e_2

$$v_1 == v_2$$

$$e_1 == e_2$$

$$s_1 == s_2$$

identical(v_1, v_2)

lam(x, y): x / y end

lam(y, x): y / x end

v-clos(ate, [list: "x", "y"], -)

v-clos(ate, [list: "y", "x"], -)

swap(e, x, y)

rename(rename(e, x, n1), y, n2) = e'

rn(rename(e', n1, y), n2, x)

lam(x): x end.

idtype("x") → idtype("x")

a → a

let f = lam(x): x end:

f(1)

f("a").

idtype("f") = idtype("x") → idtype("x")

idtype("f") =

Num^① → type(f(1))^②

① Num = idtype("x")

② type(f(1)) = idtype("x")

Str = idtype("x")

Str = Num

```
fun ident <a>(x :: a) → a:  
  x  
end
```

```
ident <Num> (1)           f <T>  
ident <Str> ("a")  
→ (lam (x :: Num) → Num; x end) (1)  
→ (lam (x :: Str) → Str; x end) ("a")
```

```
fun map <a,b> (f :: (a → b), l :: List <a>) → List <b>:
```

cases

l empty ⇒ empty

l link (fst, r) ⇒

link (f(fst), map <a,b> (f, r))

end

end

Name, List <Types> → Expr.

"map" Num, Str → map
...
map <Num, Str> (...)
end

```
fun ident <a>(x :: a) → a:  
  4  
end
```

just x?

any value w/ x's type?

ident <Num> (2)

ident <Str> ("a")

(lam (x :: Str) → Str : 4 end) ("a")
↖ ↗

type-check :: Expr, TypeEnv, Types

data Type:

```
  fun  
  | + id(x :: Str)  
end
```


