CS41 Lab 1

August 31, 2021

In typical labs this semester, you'll be working on a number of problems in groups of 3-4 students each. You will not be handing in solutions; the primary purposes of these labs are to have a lowpressure space to discuss algorithm design, and to gain experience collaborating with others on algorithm design and analysis.

However, it will be common to have some overlap between lab exercises and homework sets.

1. Lower Bound for the Hiking Problem

Argue that any solution to the Hiking Problem must take at least m miles.

2. A third algorithm for the Hiking Problem

It seems like algorithm 2 for the Hiking Problem spends a lot of time walking over alreadysearched parts of the trail. Let's try to make an adjustment so we spend more time looking at not-yet-searched parts of the trail.

HIKING()

 $1 \ k = 1.$

- 2 while you haven't found your friend yet:
- 3 hike k miles north
- 4 return to start
- 5 hike k miles south
- 6 return to start
- 7 k = 2k.

In this problem, you'll practice and formalize the analysis for the distance traveled in HIKING as a function of the initial distance from your friend in the worst case.

- (a) First, assume that your friend is *m* miles north of you. How many iterations of the loop do you execute before reaching your friend?
- (b) For any loop iteration *except* the final loop iteration, how far do you hike during this iteration? (express your answer in terms of k)
- (c) How far do you hike during the final loop iteration?
- (d) Now, calculate the total distance traveled by adding up the distance hiked over all loop iterations. (Feel free to look up or ask about any math formulas you might need.)
- (e) Next, repeat the steps above for the case where your friend is m miles south of you.
- (f) In the worst case, how far do you travel if your friend is m miles away?

- 3. Is Algorithm #2 the most efficient algorithm you can do for the Hiking problem? Either argue why this is the most efficient, or try to understand **why** this algorithm is not efficient, and design and analyze a more efficient algorithm. You should feel free to brainstorm and try out many possible ideas.
- 4. Counterfeit Coins. You are given *n* coins and a balance scale. To use this scale, you put a number of coins in a pile on the left part of the scale, and a number of coins in a pile on the right. The scale indicates which pile is heavier.

Most of the coins are identical in every aspect; however, one of the coins is counterfeit and much heavier than the rest. Design an algorithm to identify the counterfeit coin that uses the scale at most $\log_3 n$ times.