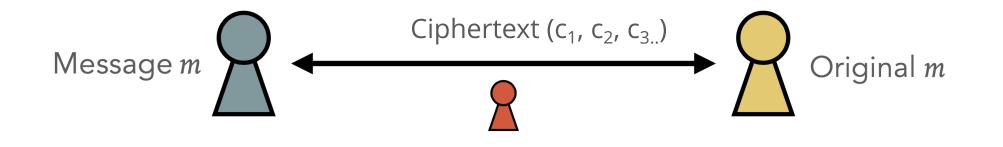
CS 88: Security and Privacy 12: Symmetric Key Cryptography 03-05-2024

slides adapted from Dave Levine, Jonathan Katz, Kevin Du



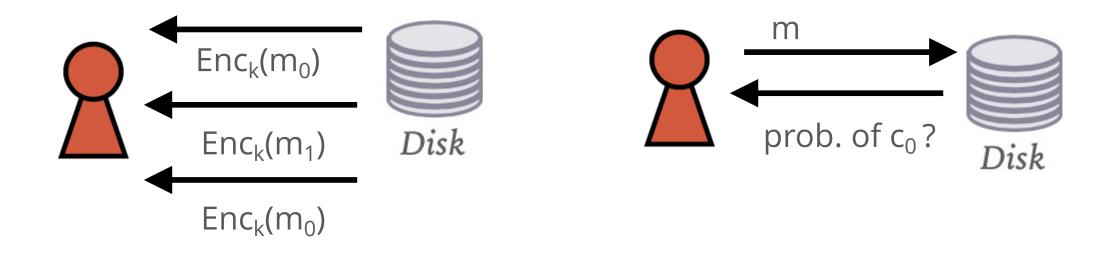
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Multiple message secrecy
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We are not going to formally define a notion of multiple-message secrecy

- Instead, define something stronger: <u>security against chosen-plaintext</u> <u>attacks (CPA-security)</u>
- minimal notion of security an encryption scheme should satisfy

Security against Chosen Plaintext Attack: Impossible?



It really is a problem if an attacker can tell when the same message is encrypted twice! This attack only works if encryption is deterministic!

Random Functions

Out of all possible function mappings between X and Y we choose one uniformly at random.

- e.g. for a 2 bit string mappings between X: $\{0, 1\}^2$ and Y: $\{0, 1\}^2$
- one possible mapping that we could choose:

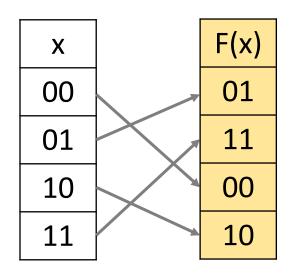
x	00	01	10	11
F(x)	01	11	00	10

Properties of function F(X) chosen uniformly at random:

- for any given $x \in X$, the probability that F(x) = y is $1/2^n$
- in our example example:
 - given $x \in X$, the probability that $F(x) = 1/2^2 = \frac{1}{4} = 0.25$
- F(x) property:
 - if x changes by one bit to give x' then
 - *F*(*x*') is completely independent of *F*(*x*).

Random Permutations

- Variant of random function is random permutation
 - treat them equivalently for our purposes .
- E.g.: random permutation over bit strings of length 2 Encryption: {0, 1}² -> {0, 1}²



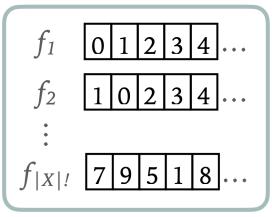
Important Property of the Random Permutation: *A permutation is invertible (bijective) function*

Given F(x) it is impossible to determine x without resorting to a brute force attack.

If |X| is very large? brute force not possible by an efficient (probabilistic polynomial time) attacker.

What we have, ideally: Random Functions

Consider the set of all permutations $F_k: X \to X$

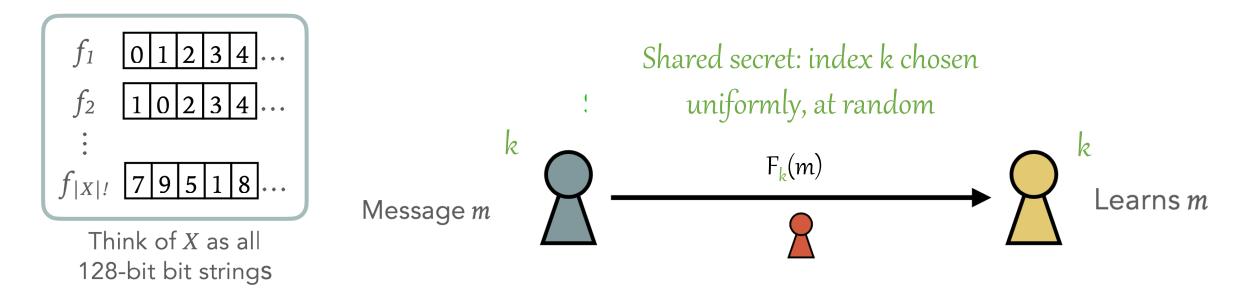


Think of *X* as all 128-bit bit strings

If you know k, then $F_k(x)$ is trivial to invert If you don't know k, then $F_k(x)$ is one-way <u>One-way function</u>

What we have, ideally: Random Functions

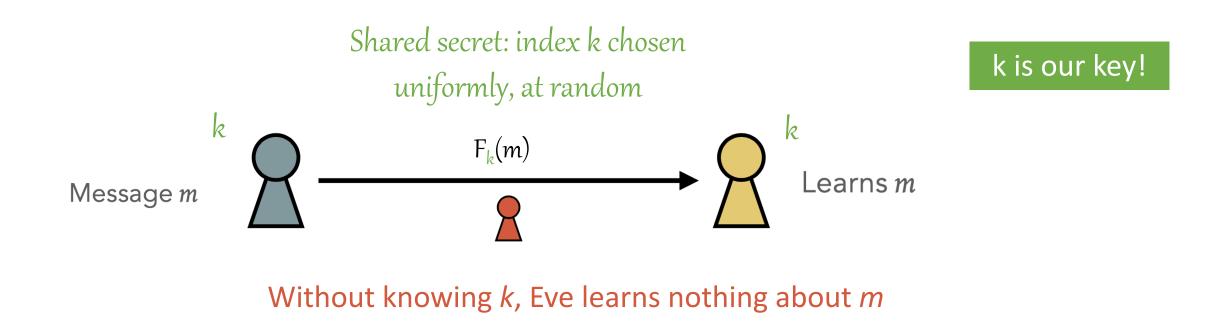
Consider the set of all permutations $F_k: X \to X$



Without knowing k, Eve learns nothing about m

k is our key!

What we have, approximately: Pseudo-Random Functions

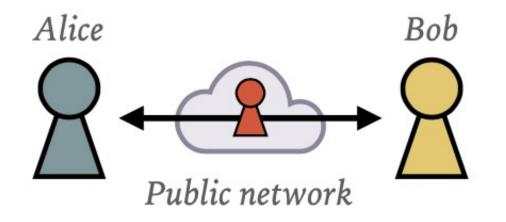


In essence, this protocol is saying "Let's use the ith permutation function" Infeasible to store all permutation functions – so instead cryptographers construct *pseudorandom functions*

A Perfectly Secure Encryption Scheme

Regardless of any prior information the attacker has about the plaintext the ciphertext observed by the attacker

should leak no additional information about the plaintext.



Alice can only observe one ciphertext going over the network

Computational Secrecy

Would be okay if a scheme leaked information with a tiny probability to eavesdroppers with bounded computational resources.

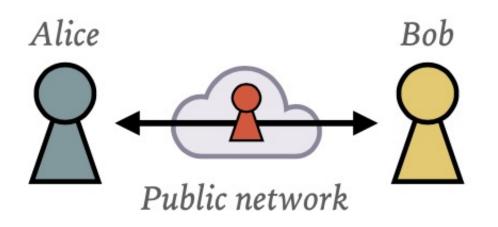
- Allowing security to fail with a tiny probability (negligible in key length n)
 - how tiny is tiny? 2⁻⁶⁰ : probability of an event occurring every 100 billion years!
- Only consider efficient attackers (bounded in polynomial time by key length)
 - attackers that can brute-force the key space in bounded time.
 - try testing 2¹¹² keys? Would take a supercomputer since Big Bang!
 - modern key space? 2¹²⁸ or more!

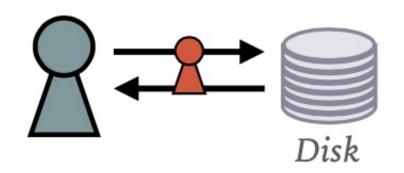
BLACKBOXES

To this end, we'll cover several "blackboxes": what properties do they provide, and how can we responsibly put them together



Scenarios and Goals



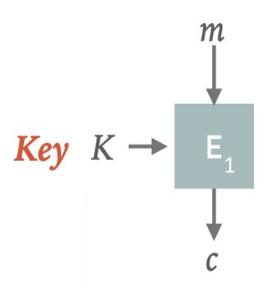


Block Ciphers

ConfidentialityKeep others from
reading Alice's messages/dataBlockIntegrityKeep others from undetectably
tampering with Alice's messages/dataIntegrityAuthenticityKeep others from undetectably
impersonating Alice (keep her to her word too!)

Block Ciphers

ENCRYPTION



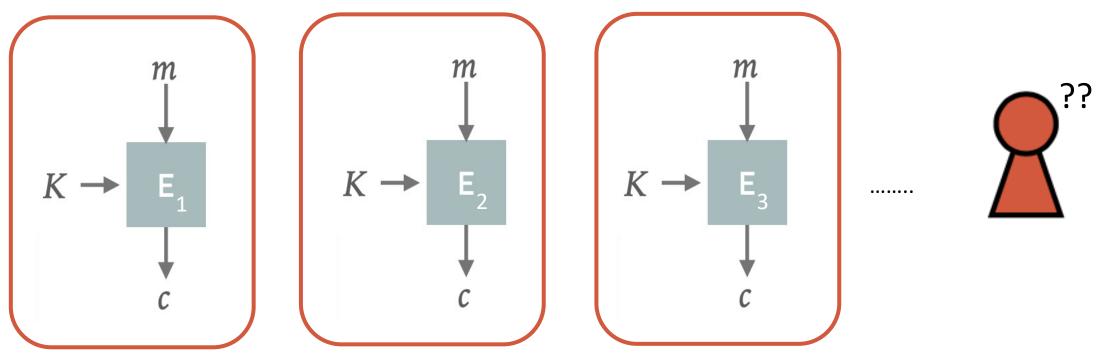
Encryption Function: E: $\{0, 1\}^k \times \{0, 1\}^n \rightarrow \{0, 1\}^n$ Fix the key K, then, E_k : $\{0, 1\}^n \rightarrow \{0, 1\}^n$

- <u>plaintext size: n</u>
- <u>ciphertext size:n</u>
- E_k : permutation on n-bit strings.
- invertible (bijective function) given the key

Once the key is fixed: E(k,m) is indistinguishable from a function chosen uniformly at random from all possible functions between block-sized binary strings.

Block Ciphers ENCRYPTION

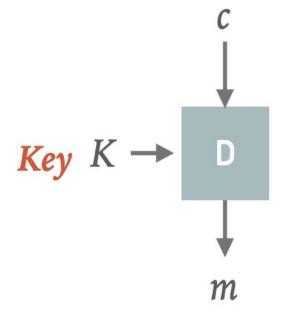
Once the key is fixed: E(k,m) is indistinguishable from a function chosen uniformly at random from all possible functions between block-sized binary strings.



Attacker has no way of knowing which random function was chosen to permute the plaintext to the ciphertext



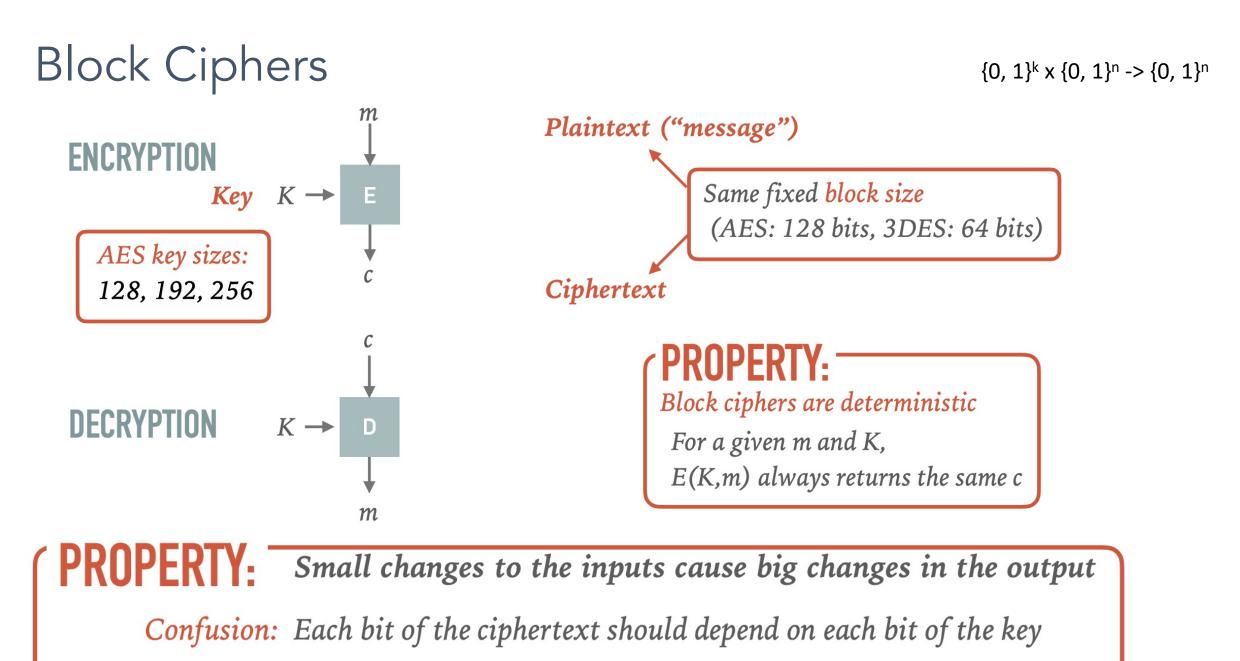
DECRYPTION



Inverse mapping of the permutation is the decryption algorithm, given the key $D_k(E_k(M)) = M$

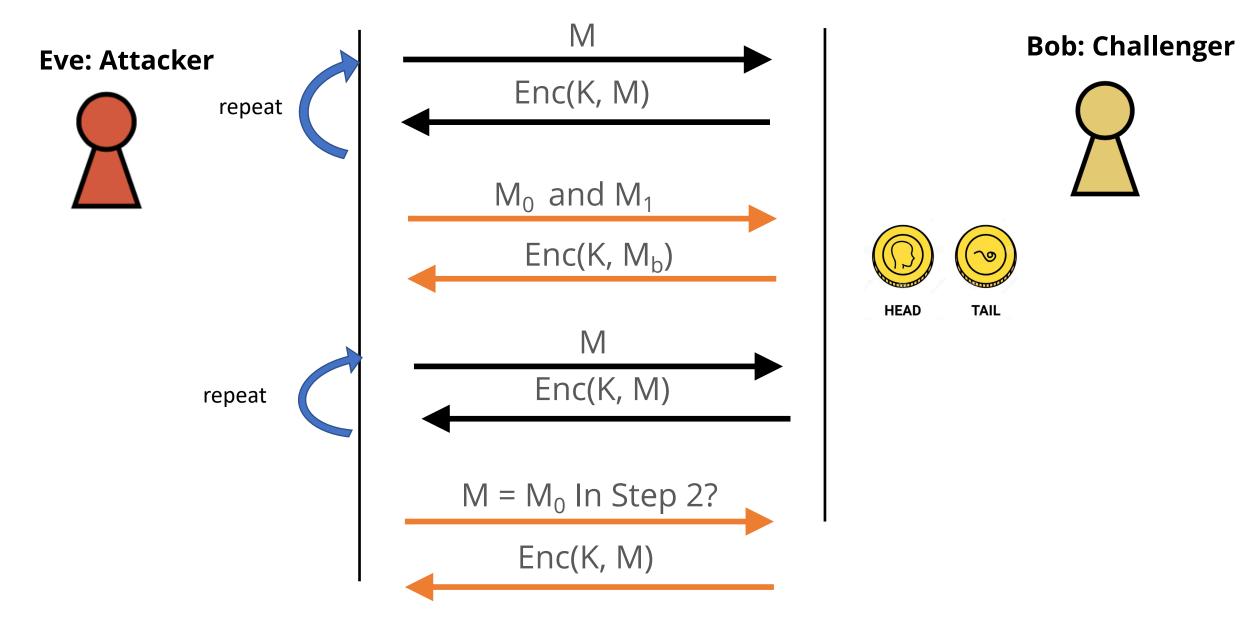
without the key: best attack is a brute force exhaustive search over the entire key space!

Attacker has no way of knowing which random function was chosen to permute the plaintext to the ciphertext

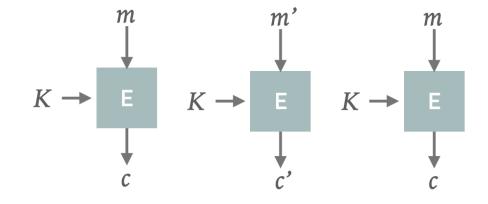


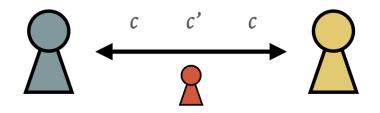
Diffusion: Flipping a bit in m should flip each bit in c with Pr = 1/2

Chosen Plaintext Attack



Problem #1: Block Ciphers Are Deterministic





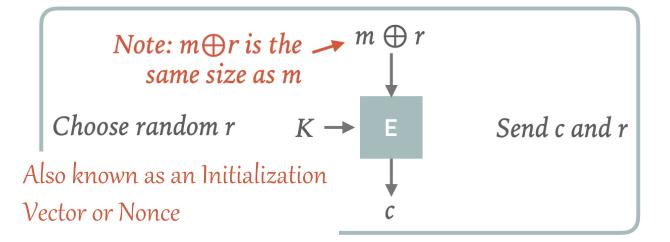
A FIX:

PROPERTY: -

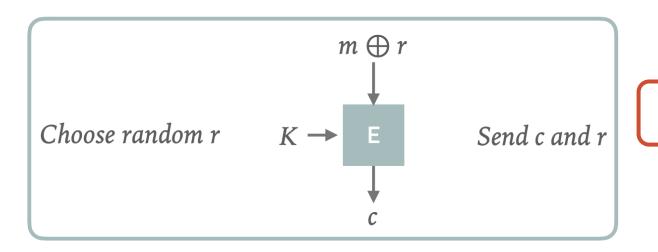
Block ciphers are deterministic

For a given m and K, E(K,m) always returns the same c

An eavesdropper could determine when messages are re-sent



Initialization Vector (nonce)



IV or r needs to be different (unpredictable) each time

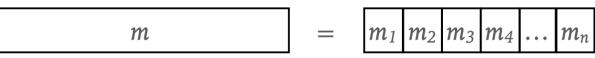
Random: Must send r with the message This is good if messages can be reordered

Counter: Don't need to send r; the receiver can infer it from the message number This is good if messages are delivered in-order

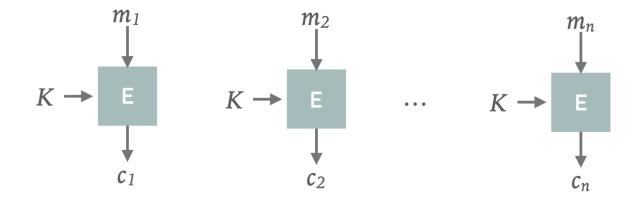
Problem #2: Block Ciphers have fixed size

Fixed block size m m

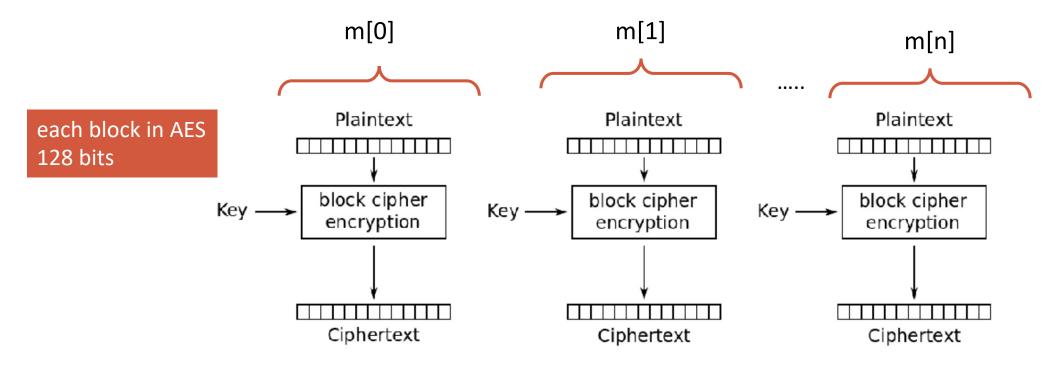
If we want to encrypt a message larger than the block size (128 bits), we simply break up the message into block-size length pieces...



...and encrypt each block



Modes of Encryption: Electronic Codebook Mode (ECB)



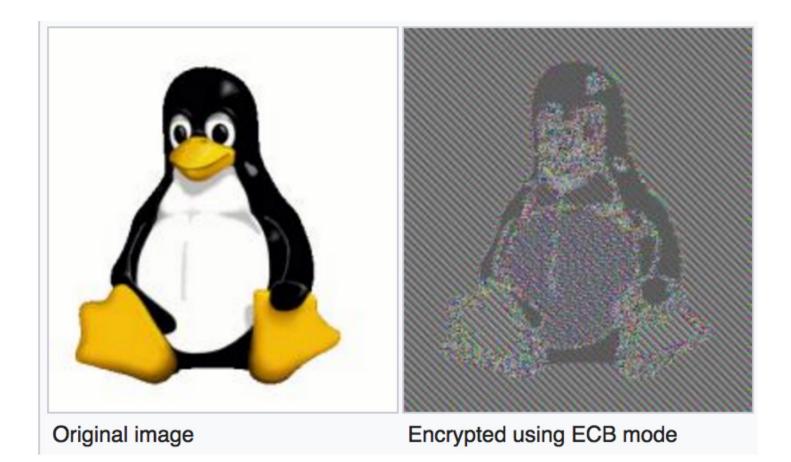
Electronic Codebook (ECB) mode encryption

Encryption:

inputs: plaintext: m, key: k, ciphertext: c[i] = E(k, m[i]) Decryption:

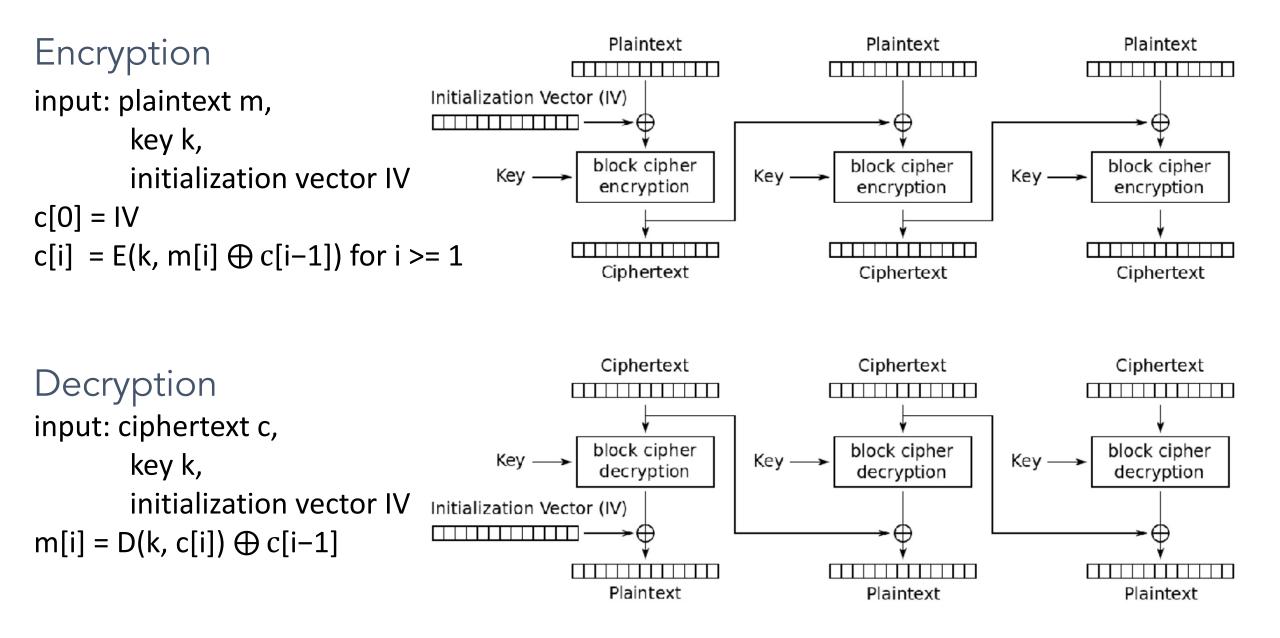
inputs: ciphertext: c, key: k,
plaintext: m[i] = D(k, c[i])

spot the problem?



NEVER use ECB (but over 50% of Android apps do)

Modes of Encryption: Cipher Block Chaining Mode (CBC)

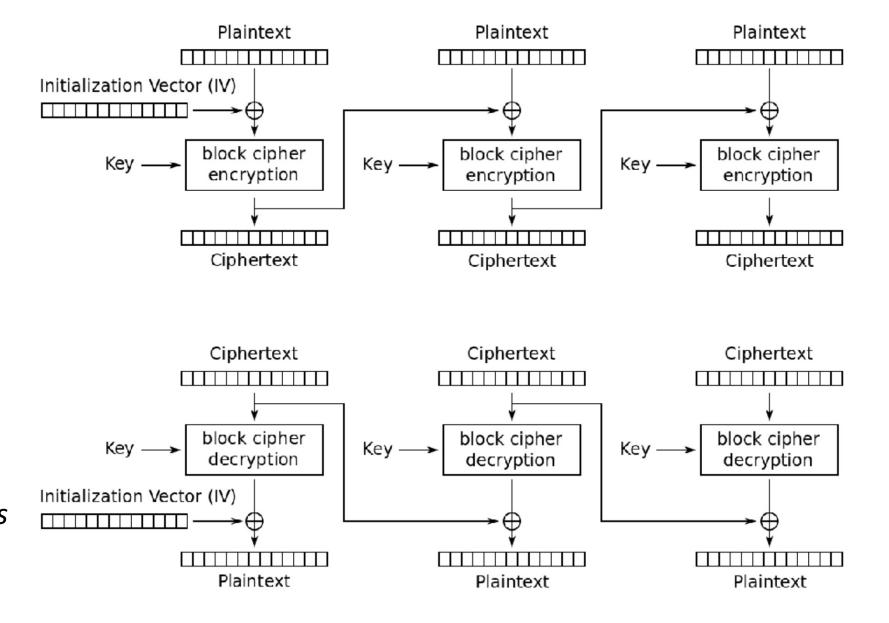


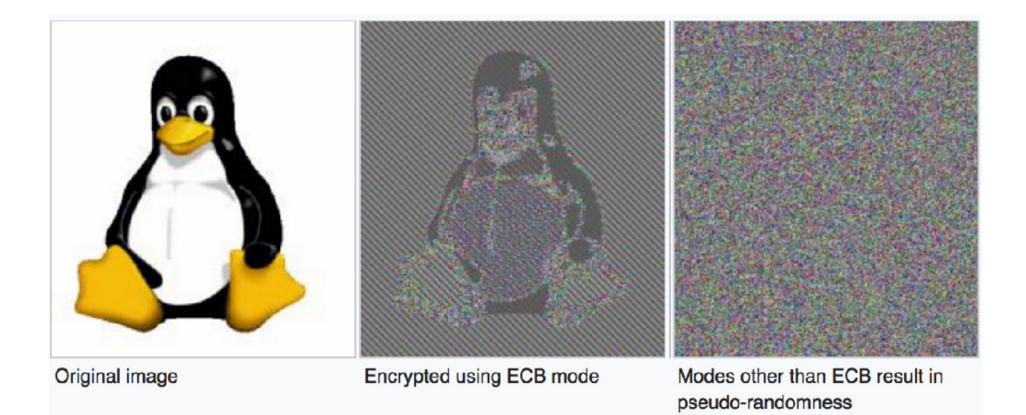
Modes of Encryption: Cipher Block Chaining Mode (CBC)

Security Input to the Encryption algorithm at each step is extremely likely to be different from the previous step.

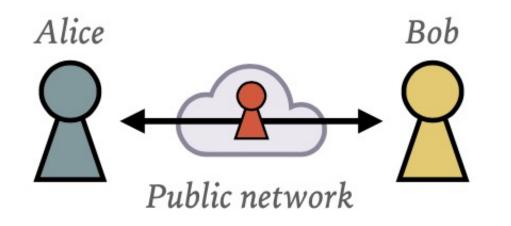
Performance Encryption: Not Parallelizable Decryption: Parallelizable recovering m[i] does not require m[i-1]. Only requires c[i-1] which is already

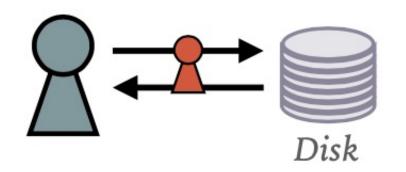
known.





Symmetric Key Cryptography





Confidentiality	Keep others from reading Alice's messages/data
Integrity	Keep others from undetectably tampering with Alice's messages/data
Authenticity	Keep others from undetectably impersonating Alice (keep her to her word too!)

Block Ciphers

Limitations?

- what if Eve modifies the packet in transit?
- How do we share keys?