

CS 88: Security and Privacy

11: Introduction to Cryptography

10-06-2022

slides adapted from Dave Levine, Vitaly Shmatikov, Christo Wilson, and Franz Roesner



A CRYPTO NERD'S
IMAGINATION:

HIS LAPTOP'S ENCRYPTED.
LET'S BUILD A MILLION-DOLLAR
CLUSTER TO CRACK IT.

NO GOOD! IT'S
4096-BIT RSA!

BLAST! OUR
EVIL PLAN
IS FOILED!



WHAT WOULD
ACTUALLY HAPPEN:

HIS LAPTOP'S ENCRYPTED.
DRUG HIM AND HIT HIM WITH
THIS \$5 WRENCH UNTIL
HE TELLS US THE PASSWORD.

GOT IT.



Cryptography

- Cryptography: An ancient art
 - 500BC – 20th century: Design -> break -> repair -> break -> repair ->.....
- Modern Cryptography: Cryptography as a science
 - relies on rigorous threat models
 - firm theoretical foundations and proofs!

Modern Cryptography

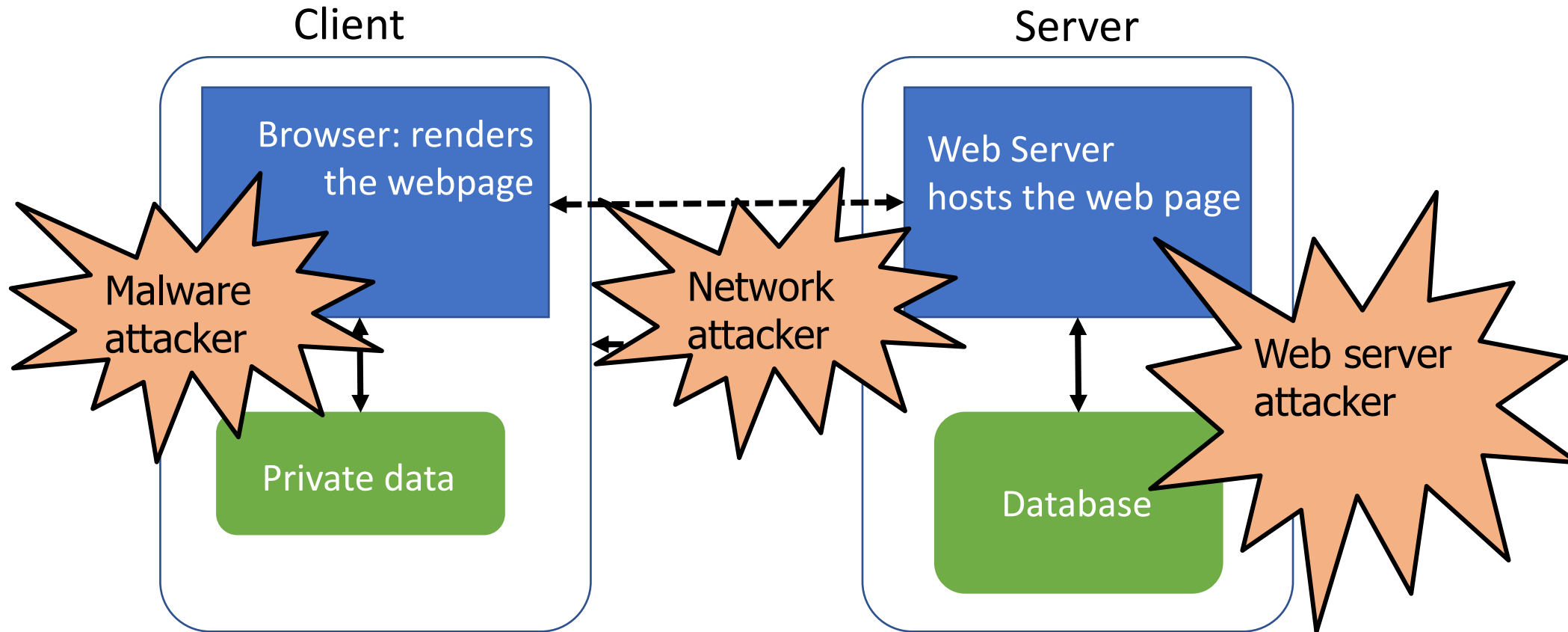
*Design, analysis and implementation of **mathematical techniques** for **securing** information, systems and computation against **adversarial attacks**.*

Modern Cryptography: How many of the following actions involve cryptography ?

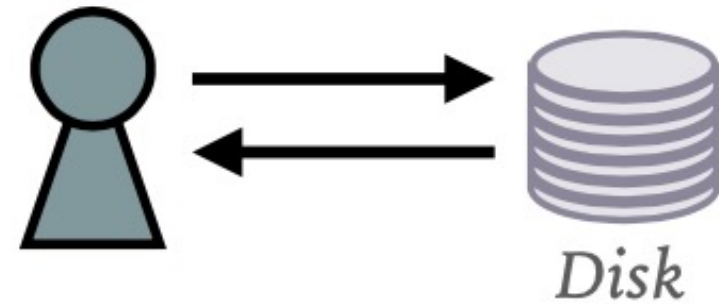
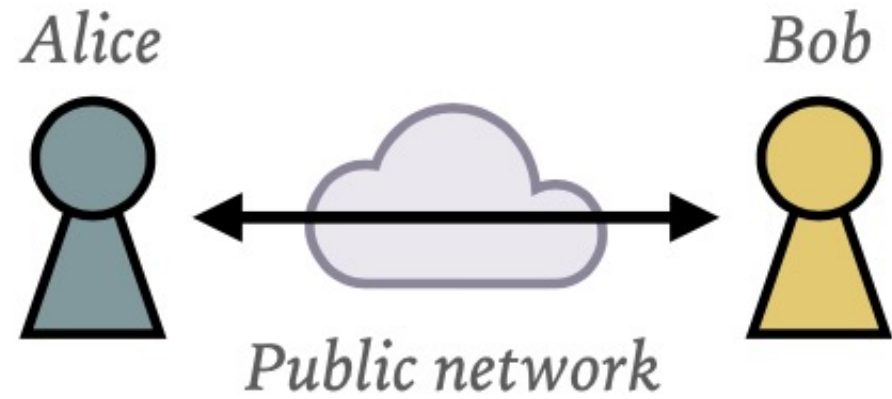
1. Git cloning your lab repo
2. Connecting to Swarthmore's WiFi
3. Updating software on your device
4. Making online purchases

A. 1 B. 2 C. 3 D. 4 E. 0

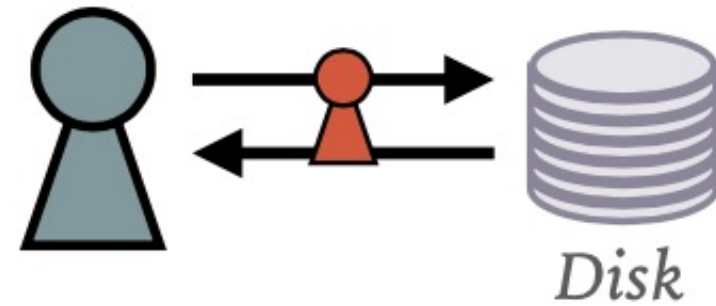
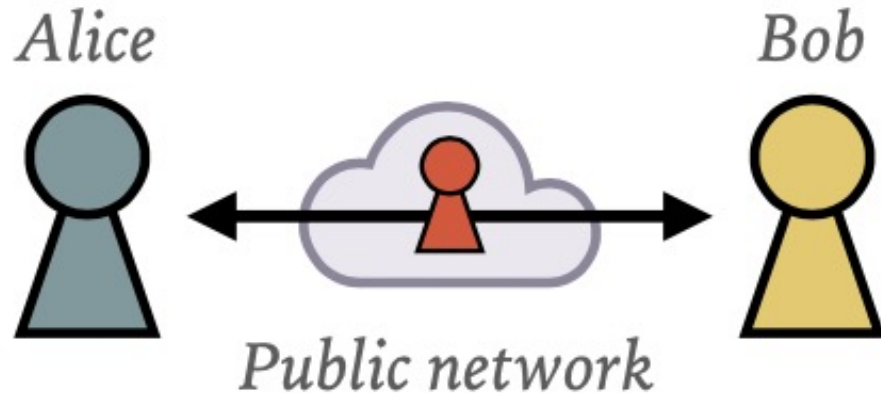
Where Does the Attacker Live?



Scenarios and Goals



Scenarios and Goals



- Confidentiality** Keep others from reading Alice's messages/data
- Integrity** Keep others from undetectably tampering with Alice's messages/data
- Authenticity** Keep others from undetectably impersonating Alice (keep her to her word too!)

Recall the Bigger Picture

- Cryptography: small piece of a larger system
- Protect the entire system (recall: the weakest link)
 - physical security
 - OS security
 - Network security
 - Users
 - Cryptography
- **Cryptography is a crucial part of this toolbox**



Cryptography: Terms



- Encryption (E): The process of transforming a message so that its meaning is not obvious
- Decryption (D): The process of transforming an encrypted message back into its original form.
- Plaintext (P): Original, unencrypted form of a message
- Ciphertext (C): The encrypted form of a message

Formal Notation: We seek a cryptosystem for which $P = D (E (P))$

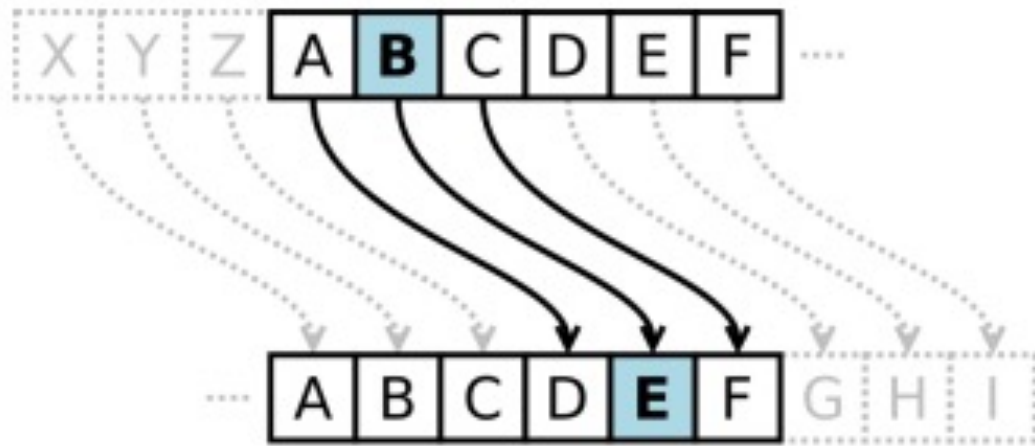
Historical Ciphers

- Substitution Cipher
 - Monoalphabetic - Ceasar's Cipher – fixed subst. over the entire message
 - Polyalphabetic – a number of substitutions at different positions in the message
- Transposition Ciphers
- Codebooks
- Machines

Recommended Reading: The Codebreakers by David Kahn, The Code Book by Simon Singh

Ceasar CIPHER: Substitution Cipher

Plaintext letters replaced with letters fixed shift way in the alphabet.



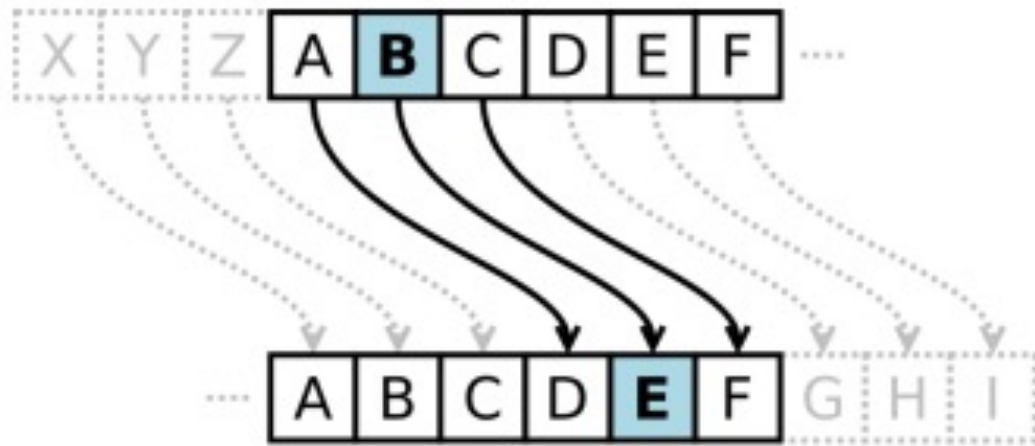
Example:

- Plaintext: HEY BRUTUS BRING A KNIFE TO THE PARTY.
- Ciphertext: **KHB EUXWXV EULQJ D NQLIH WR WKH SDUWB**
- Key Shift 3:
 - ABCDEFGHIJKLMNOPQRSTUVWXYZ
 - DEF_GHIJKLMNOPQRSTUVWXYZABC



Ceasar Cipher: Substitution Cipher

Plaintext letters replaced with letters fixed shift way in the alphabet.



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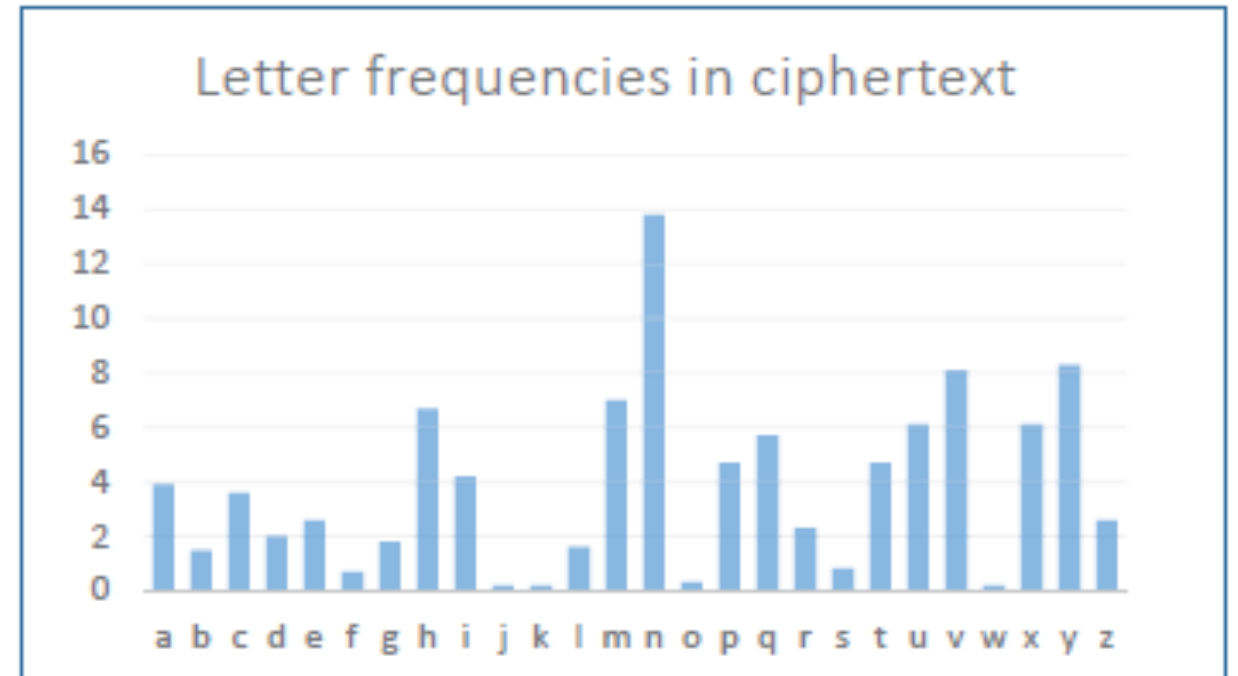
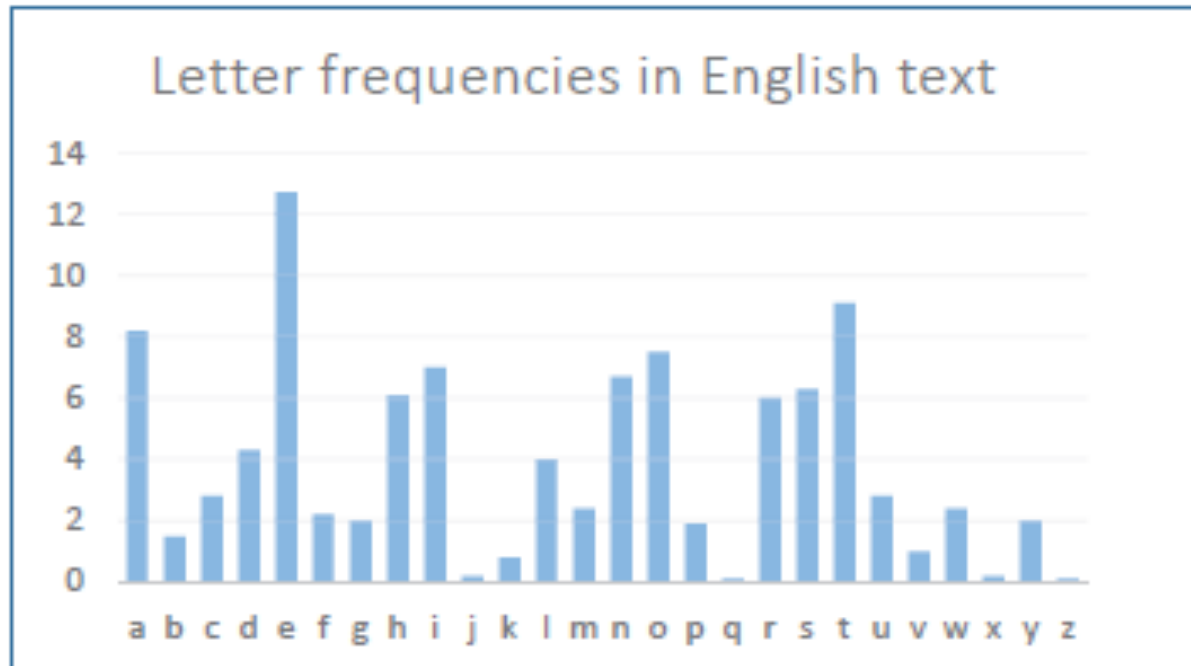
- Encryption and Decryption are symmetric.
- Key space?
 - 26
- Attack shift ciphers?
 - brute force

Substitution Cipher

- **Superset of shift ciphers:** each letter is substituted for another one.
- One implementation: Add a secret key
- Example
 - Plaintext: ABCDEFGHIJKLMNOPQRSTUVWXYZ
 - Cipher: ZEBRASCDFGHIJKLMNOPQTUVWXY
- “state-of-the-art” for thousands of years

Monoalphabetic Substitution Cipher

- What is the key space?
 - $26!$ approx. = 2^{88}
- Launching an attack?
 - frequency analysis: the study of frequency of letters or groups of letters (grams).
 - Common letters: T, A, E, I, O
 - Common 2-letter combinations (bi-grams): TH, HE, IN, ER
 - Common 3-letter combinations (tri-grams): THE, AND, ING.



Cryptanalysis of Monoalphabetic Substitution

- Dominates cryptography through the first millennium
- Frequency analysis
 - Remember Al-Kindi from 800 AD?
- Lessons?
 - Use large blocks: instead of replacing ~6 bits at a time, replace 64 or 128 bits
 - Leads to block ciphers like DES and AES
 - Use different substitutions to prevent frequency analysis
 - Leads to polyalphabetic substitution ciphers and stream ciphers

Vigenère Cipher (1596)



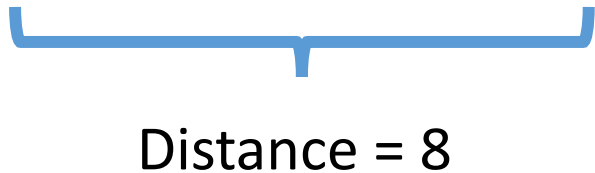
- Main weakness of monoalphabetic substitution ciphers:
 - Each letter in the ciphertext corresponds to only one letter in the plaintext
- Polyalphabetic substitution cipher
 - Given a key $K = (k_1, k_2, \dots, k_m)$
 - Shift each letter p in the plaintext by k_i , where i is modulo m

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25

Plaintext CRYPTOGRAPHY
Key LUCKLUCKLUCK (Shift 11 20 2 10 11 20 2 11 ...)
Ciphertext NLAZEIIBLJJI

Kasisky Test

Plaintext	T	H	E	S	U	N	A	N	D	T	H	E	M	A	N	I	N	T	H	E	M	O	O	N
Key	K	I	N	G	K	I	N	G	K	I	N	G	K	I	N	G	K	I	N	G	K	I	N	G
Ciphertext	D	P	R	Y	E	V	N	T	N	B	U	K	W	I	A	O	X	B	U	K	W	W	B	T



- Repeating patterns (of length >2) in ciphertext are a tell
 - Likely due to repeated plaintext encrypted under repeated key characters
 - The distance is likely to be a multiple of the key length

Cryptanalysis of Vigenère Cipher

- Cracking Vigenère (1854 or 1863)
 1. Guess the key length x using Kasisky test of index of coincidence
 2. Divide the ciphertext into x shift cipher encryptions
 3. Use frequency analysis on each shift cipher
- Lessons?
 - As key length increases, letter frequency becomes more random
 - If key never repeated, Vigenère wouldn't be breakable!

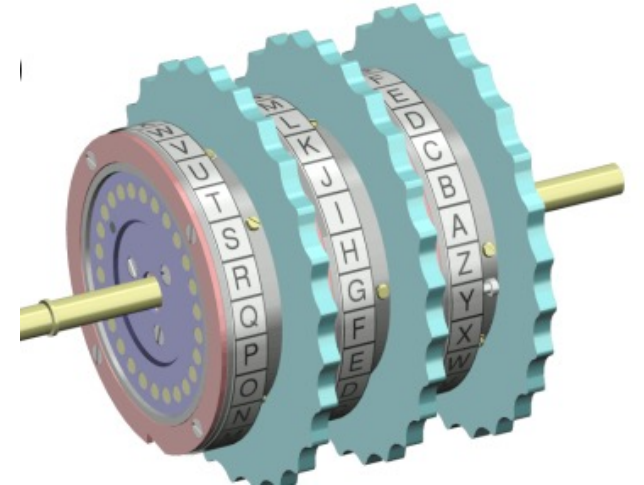




- WW2 German Enigma machine
 - Polyalphabetic substitution cipher
 - Substitution table changes from character to character
 - Rotors control substitutions
- Allies broke Enigma (even before the war), significant intelligence impact
- Computers were built to break WW2 ciphers, by Alan Turing and others

Enigma Machine

- Use rotors that change position after each key
- Key: initial setting of the rotors
- Key space?
 - 26^n for n rotors
- KeyGen:
 - Choose rotors, rotor orders, rotor positions, and plugboard settings
 - 158,962,555,217,826,360,000 possible keys!



Cryptanalysis: Enigma

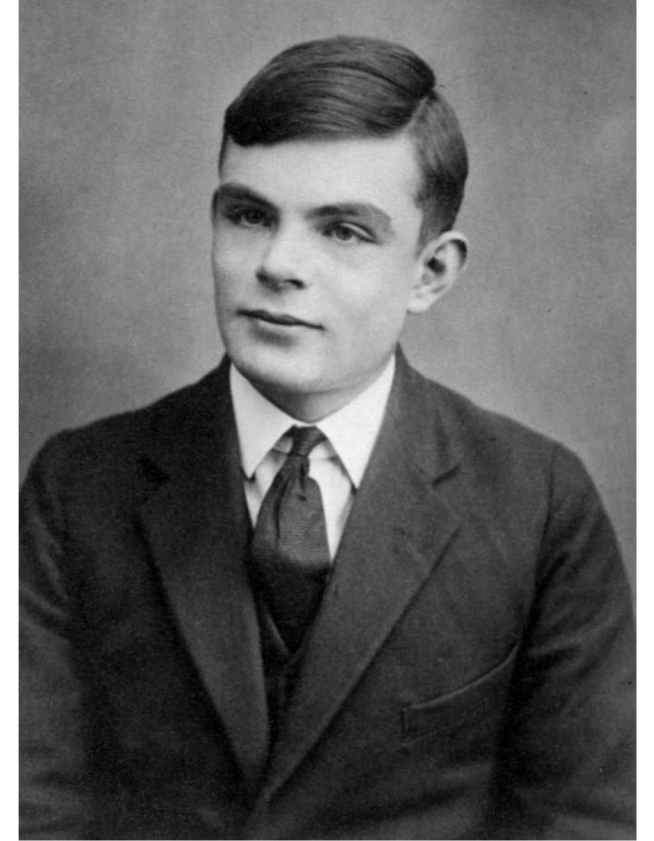
- Polish and British cryptographers built BOMBE, a machine to brute-force Enigma keys
- Why was Enigma breakable?
 - Kerckhoff's principle: The Allies stole Enigma machines, so they knew the algorithm
 - Known plaintext attacks: the Germans often sent predictable messages (e.g. the weather report every morning)
 - Chosen plaintext attacks: the Allies could trick the Germans into sending a message (e.g. "soldiers at Normandy")
 - Brute-force: BOMBE would try many keys until the correct one was found



BOMBE machine

Legacy of Enigma

- Alan Turing, one of the cryptographers who broke Enigma, would go on to become one of the founding fathers of computer science
- Most experts agree that the Allies breaking Enigma shortened the war in Europe by about a year



Alan Turing

Cryptography by Computers

- The modern era of cryptography started after WWII, with the work of Claude Shannon
- “New Directions in Cryptography” (1976) showed how number theory can be used in cryptography
 - Its authors, Whitfield Diffie and Martin Hellman, won the Turing Award in 2015 for this paper
- *This is the era of cryptography we’ll be focusing on.*



How Cryptosystems work today

- Layered approach:
 - Cryptographic protocols (e.g., CBC mode encryption)
 - Built on: Cryptographic primitives (block ciphers)
- Flavors of cryptography:
 - Symmetric: private key
 - Asymmetric: public key
- Public algorithms: Kerckhoff's principle
- *Security proofs based on assumptions (not this course)*
- **Warning!**
 - careful about inventing your own!
 - Use vetted libraries to apply crypto algorithms!



Cryptosystem Stack

- Primitives:
 - AES/DES
 - ESA / ElGamal / Elliptic Curve
- Modes
 - Block mode (CBC, ECV, CTR, GCM..)
 - Padding structures
- Protocols:
 - TLS, SSL, SSH
- Usage of protocols:
 - Browser security
 - Secure remote logins

Flavors of Cryptography

- Symmetric cryptography
 - Both communicating parties have access to a shared random string K , called the key.
- Asymmetric cryptography
 - Each party creates a public key p_k and a secret key s_k
 - Inventors won Turing Award!

Kerckhoff's Principle

- Security of a cryptographic object should depend only on the secrecy of the secret (private) key.
- Security should not depend on the secrecy of the algorithm itself.
- Foreshadow: Need for randomness – the key to keep private

Flavors of Cryptography

- Symmetric cryptography
 - Both communicating parties have access to a shared random string K , called the key.
 - Challenge: How do you privately share a key?
- Asymmetric cryptography
 - Each party creates a public key p_k and a secret key s_k
 - Challenge: How do you validate a public key?
- Key Insight: Randomness –
 - something an adversary won't know, can't predict and can't figure out.

Randomness



Explicit Uses of Randomness:

- Generate secret cryptographic keys
- Generate random initialization vectors for encryption

Non-obvious Use cases

- Generate passwords for new users
- Shuffle the order of votes in an electronic voting machine
- Shuffle cards etc. (for online games)

Randomness



Randomness



- Ideally, to the attacker, it is indistinguishable from a string of bits chosen uniformly, at random.
- However, this is impossible with Alice and Bob having a shared secret.

What we have, ideally: Random Functions

Consider the set of all permutations $f_i: X \rightarrow X$

f_1	0	1	2	3	4	...
f_2	1	0	2	3	4	...
\vdots						
$f_{ X !}$	7	9	5	1	8	...

If you know i , then $f_i(x)$ is trivial to invert

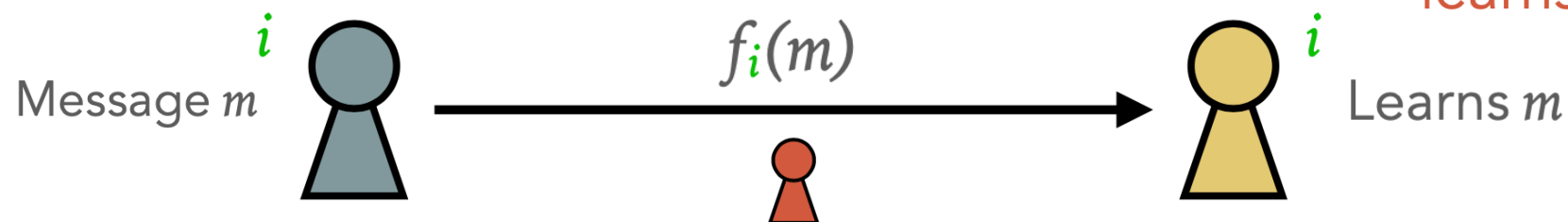
If you don't know i , then $f_i(x)$ is one-way

“One-way trapdoor function”

Think of X as all
128-bit bit strings

Shared secret: index i chosen u.a.r.

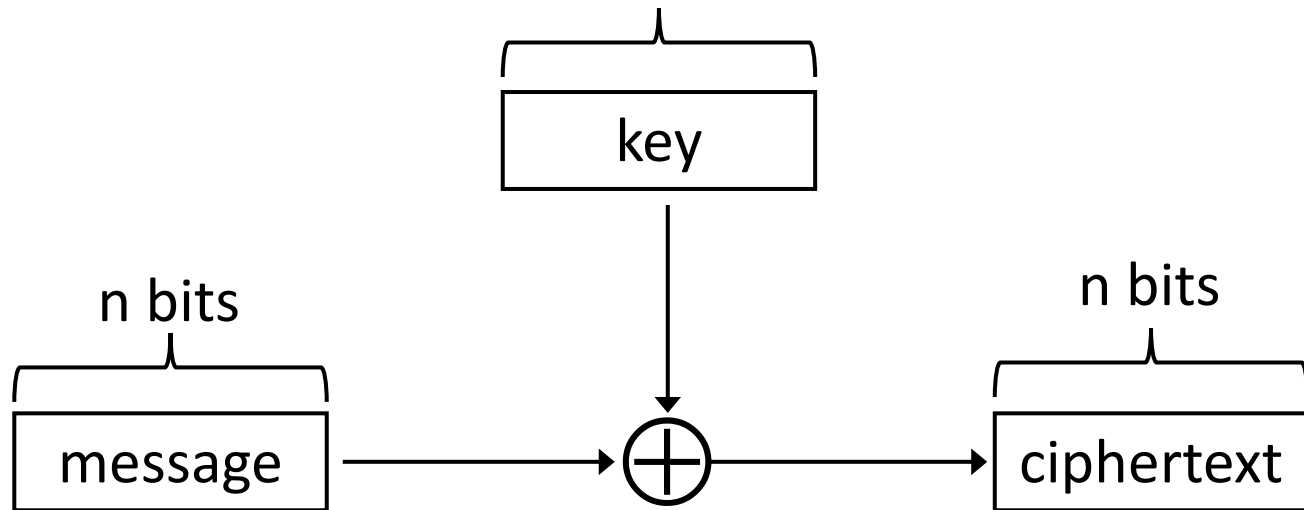
Without knowing i ,
learns nothing about m



i is our key

One Time Pad (1920s)

- Fix the vulnerability of the Vigenère cipher by using very long keys
- Key is a random string that is at least as long as the plaintext
- Similar encryption as with Vigenère (different shift per letter)



Review: XOR

The XOR operator takes two bits and outputs one bit:

$0 \oplus 0 = 0$
$0 \oplus 1 = 1$
$1 \oplus 0 = 1$
$1 \oplus 1 = 0$

Useful properties of XOR:

$x \oplus 0 = x$
$x \oplus x = 0$
$x \oplus y = y \oplus x$
$(x \oplus y) \oplus z = x \oplus (y \oplus z)$
$(x \oplus y) \oplus x = y$

Review: XOR Algebra

Algebra works on XOR too

$y \oplus 1 = 0$	Goal: Solve for y
$y \oplus 1 \oplus 1 = 0 \oplus 1$	XOR both sides by 1
$y = 1$	Simplify with identities

One-Time Pads: Key Generation

Alice

K	0	1	1	0	0	1	0	1	0	1	1	1
-----	---	---	---	---	---	---	---	---	---	---	---	---

The key K is a randomly-chosen bitstring.

Recall: We are in the symmetric-key setting, so we'll assume Alice and Bob both know this key.

One-Time Pads: Encryption

The plaintext M is the bitstring that Alice wants to encrypt.

Idea: Use XOR to scramble up M with the bits of K .

Alice

K

0	1	1	0	0	1	0	1	0	1	1	1
---	---	---	---	---	---	---	---	---	---	---	---

M

1	0	0	1	1	0	0	1	0	1	0	0
---	---	---	---	---	---	---	---	---	---	---	---

One-Time Pads: Encryption

Alice												
K	0	1	1	0	0	1	0	1	0	1	1	1
	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus
M	1	0	0	1	1	0	0	1	0	1	0	0
	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
C	1	1	1	1	1	1	0	0	0	0	1	1

Encryption algorithm: XOR each bit of K with the matching bit in M .

The ciphertext C is the encrypted bitstring that Alice sends to Bob over the insecure channel.

One-Time Pads: Decryption

Bob receives the ciphertext C . Bob knows the key K . How does Bob recover M ?

Bob

K	0	1	1	0	0	1	0	1	0	1	1	1
C	1	1	1	1	1	1	0	0	0	0	1	1

One-Time Pads: Decryption

Bob

<i>K</i>	0	1	1	0	0	1	0	1	0	1	1	1
	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus	\oplus
<i>C</i>	1	1	1	1	1	1	0	0	0	0	1	1
	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓	↓
<i>M</i>	1	0	0	1	1	0	0	1	0	1	0	0

Decryption algorithm: XOR each bit of *K* with the matching bit in *C*.

Cryptanalysis of OTP

- The key is random, so ciphertext is also random
- OTP achieves Perfect Secrecy
 - Shannon or Information Theoretic Security
 - Basic idea: ciphertext reveals no “information” about plaintext
- The adversary believes the probability that the plaintext is m is $P(\text{PT}=m)$ **before seeing the ciphertext**
 - Maybe they are very sure, or maybe they have no idea.
- The adversary believes the probability that the plaintext is m is $P(\text{PT}=m \mid \text{CT}=c)$ **after seeing that the ciphertext is c .**
 - $P(\text{PT}=m \mid \text{CT}=c) = P(\text{PT} = m)$ means that after knowing that the ciphertext is c , the adversary’s belief does not change.
- Intuitively, the adversary learned **nothing** from the ciphertext

Put Another Way

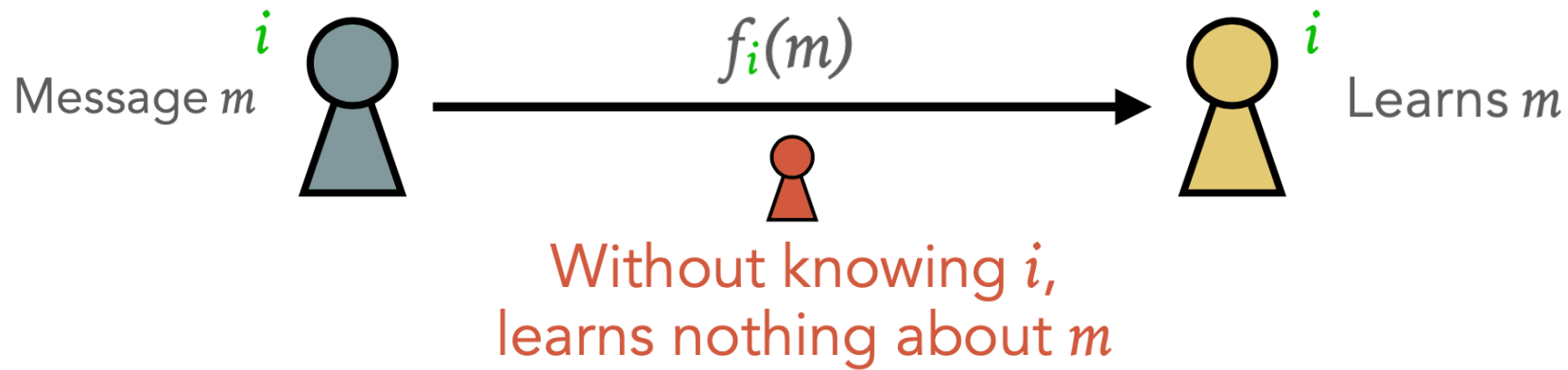
- Imagine you have a ciphertext c where the length $|c| = 1000$
- I can give you a key k_i with $|k_i| = 1000$ such that:
 - The decrypted message m_i is the first 1000 characters of Hamlet
- Or, I can give you a key k_j with $|k_j| = 1000$ such that:
 - The decrypted message m_j is the first 1000 characters of the US Constitution
- If an algorithm offers perfect secrecy then:
 - For a given ciphertext of length n
 - All possible corresponding plaintexts of length n are possible decryptions

Cryptanalysis of OTP

- Intuitively, the key is random, so ciphertext is also random
- OTP achieves Perfect Secrecy
 - Shannon or Information Theoretic Security
 - Basic idea: ciphertext reveals no “information” about plaintext
- Caveats
 - If the length of the OTP key is less than the length of the message...
 - It’s not a OTP anymore, not perfectly secret!
 - If you reuse the OTP key...
 - It’s not a OTP anymore, not perfectly secret!
- Major issue with OTP in practice?
 - How to securely distribute the key books to both parties

What we have, ideally: Random Functions

Shared secret: index i chosen u.a.r.



i is our key

In essence, this protocol is saying “Let’s use the i th permutation function”
Infeasible to store all permutation functions – so instead cryptographers construct *pseudorandom functions*

What we have, ideally: Random Functions

- When describing algorithms, we assume access to uniformly distributed bits/bytes to use for key generation
- Where do these actually come from?
- Precise details depend on the system
 - Linux or unix: `/dev/random` or `/dev/urandom`
 - **Do not use C's `rand()` or `java.util.Random`**
 - Use crypto libraries instead

Random-number generation

- Two steps:
 1. Continually collect a “pool” of high-entropy (i.e., “unpredictable”) data
 2. When random bits are requested, process this data to generate a sequence of uniform, independent bits/bytes
 - May “block” if insufficient entropy available

How Random is "Random"?

OXFFFFFFF EVERY TIME IS OXDEADBEEF —

How a months-old AMD microcode bug destroyed my weekend [UPDATED]

AMD shipped Ryzen 3000 with a serious microcode bug in its random number generator.

JIM SALTER - 10/29/2019, 7:00 AM



Uptime

IT and business computing insights

Crypto shocker: four of every 1,000 public keys provide no security (updated)

By Dan Goodin | Published 7 days ago

WORLD U.S. N.Y. / REGION BUSINESS TECHNOLOGY SCIENCE HEALTH SPORTS OPINION A

Flaw Found in an Online Encryption Method

JOHN MARKOFF

Published: February 14, 2012

SAN FRANCISCO — A team of European and American mathematicians and cryptographers have discovered an unexpected weakness in the encryption system widely used worldwide for online shopping, banking, e-mail and other Internet services intended to remain private and secure.

RECOMMEND

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LINKEDIN

COMMENTS
(127)

E-MAIL

How might we get “good” random numbers?

- For security applications, want “cryptographically secure pseudorandom numbers”
- Libraries include cryptographically secure pseudorandom number generators (CSPRNG)
- Linux:
 - `/dev/random`: blocking: waits for enough entropy
 - `/dev/urandom`: nonblocking, possibly less entropy
 - `getrandom()` – syscall! – by default blocking
- Internally:
 - Entropy pool: gathered from multiple sources
 - e.g.: mouse/keyboard/network timings
- Better idea:
 - AMD/Intel’s on-chip random number generator: RDRAND
 - Hopefully no hardware bugs!