CS 31: Introduction to Computer Systems

26-27: Virtual Memory

30 April, 2 May
Reading Quiz
Memory

• Abstraction goal: make every process think it has the same memory layout.
  – MUCH simpler for compiler if the stack always starts at 0xFFFFFFFF, etc.

• Reality: there’s only so much memory to go around, and no two processes should use the same (physical) memory addresses.

OS (with help from hardware) will keep track of who’s using each memory region.

<table>
<thead>
<tr>
<th>OS</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Text</td>
<td>Process 1</td>
</tr>
<tr>
<td>Data</td>
<td>Process 3</td>
</tr>
<tr>
<td>Heap</td>
<td>Process 2</td>
</tr>
<tr>
<td>Stack</td>
<td>Process 3</td>
</tr>
<tr>
<td></td>
<td>Process 1</td>
</tr>
</tbody>
</table>
Memory Terminology

**Virtual (logical) Memory**: The abstract view of memory given to processes. Each process gets an independent view of the memory.

**Physical Memory**: The contents of the hardware (RAM) memory. Managed by OS. Only **ONE** of these for the entire machine!

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**Address Space**: Range of addresses for a region of memory.

**Virtual address space (VAS)**: fixed size.

**Physical address**:

- 0x0
- 0xFFFFFFFF

---

**Virtual Memory**:

- Text
- Data
- Heap
- Stack

**Physical Memory**:

- Process 1
- Process 3
- Process 2
- Process 3
- Process 1

(Determined by amount of installed RAM.)
Memory Terminology

Note: It is common for VAS to appear larger than physical memory.

32-bit (IA32): Can address up to 4 GB, might have less installed
64-bit (X86-64): Our lab machines have 48-bit VAS (256 TB), 36-bit PAS (64 GB)

Address Space:
Range of addresses for a region of memory.
The set of available storage locations.

Virtual address space (VAS): fixed size.

(Determined by amount of installed RAM.)
Cohabitating Physical Memory

• If process is given CPU, must also be in memory.

• Problem
  – Context-switching time (CST): 10 µsec
  – Loading from disk: 10 MB/s
  – To load 1 MB process: 100 msec = 10,000 x CST
  – Too much overhead! Breaks illusion of simultaneity

• Solution: keep multiple processes in memory
  – Context switch only between processes in memory
Memory Issues and Topics

• Where should process memories be placed?
  – Topic: “Classic” memory management

• How does the compiler model memory?
  – Topic: Logical memory model

• How to deal with limited physical memory?
  – Topics: Virtual memory, paging

Plan: Start with the basics (out of date) to motivate why we need the complex machinery of virtual memory and paging.
Problem: Placement

• Where should process memories be placed?
  – Topic: “Classic” memory management

• How does the compiler model memory?
  – Topic: Logical memory model

• How to deal with limited physical memory?
  – Topics: Virtual memory, paging
Memory Management

- Physical memory starts as one big empty space.
Memory Management

• Physical memory starts as one big empty space.

• Processes need to be in memory to execute.
Memory Management

• Physical memory starts as one big empty space.
• When creating process, allocate memory
  – Find space that can contain process
  – Allocate region within that gap
  – Typically, leaves a (smaller) free space
Memory Management

• Physical memory starts as one big empty space.
• When creating process, allocate memory
  – Find space that can contain process
  – Allocate region within that gap
  – Typically, leaves a (smaller) free space
• When process exits, free its memory
  – Creates a gap in the physical address space.
  – If next to another gap, coalesce.
Fragmentation

• Eventually, memory becomes fragmented
  – After repeated allocations/de-allocations

• Internal fragmentation
  – Unused space within process
  – Cannot be allocated to others
  – Can come in handy for growth

• External fragmentation
  – Unused space outside any process (gaps)
  – Can be allocated (too small/not useful?)
Which form of fragmentation is easiest for the OS to reduce/eliminate? Why?

A. Internal fragmentation

B. External fragmentation

C. Neither
Placing Memory

• When searching for space, what if there are multiple options?

• Algorithms
  – *First (or next) fit*
  – Best fit
  – Worst fit

• Complication
  – Is region fixed or variable size?

OLD SOLUTION
Placing Memory

• When searching for space, what if there are multiple options?
• Algorithms
  – First (or next) fit
  – Best fit
  – Worst fit
• Complication
  – Is region fixed or variable size?
Placing Memory

• When searching for space, what if there are multiple options?

• Algorithms
  – First (or next) fit
  – Best fit
  – Worst fit

• Complication
  – Is region fixed or variable size?
Which memory allocation algorithm leaves the smallest fragments (external)?

A. first-fit
B. worst-fit
C. best-fit

Is leaving small fragments a good thing or a bad thing?
Placing Memory

- When searching for space, what if there are multiple options?
- Algorithms
  - *First (or next) fit: fast*
  - Best fit
  - Worst fit
- Complication
  - Is region fixed or variable size?
Placing Memory

• When searching for space, what if there are multiple options?

• Algorithms
  – First (or next) fit
  – *Best fit: leaves small fragments*
  – Worst fit

• Complication
  – Is region fixed or variable size?
Placing Memory

• When searching for space, what if there are multiple options?

• Algorithms
  – First (or next) fit
  – Best fit
  – Worst fit: leaves large fragments

• Complication
  – Is region fixed or variable size?

not obvious which is better unless you know more about workload – which of these is ultimately better for your system
What if it doesn’t fit?

• There may still be significant unused space
  – External fragments
  – Internal fragments

• Approaches
What if it doesn’t fit?

• There may still be significant unused space
  – External fragments
  – Internal fragments

• Approaches
  – Compaction
What if it doesn’t fit?

• There may still be significant unused space
  – External fragments
  – Internal fragments

• Approaches
  – Compaction
  – *Break process memory into pieces*
    • Easier to fit.
    • More state to keep track of.
Problem Summary: Placement

• When placing process, it may be hard to find a large enough free region in physical memory.
• Fragmentation makes this harder over time (free pieces get smaller, spread out)
• General solution: don’t require all of a process’s memory to be in one piece!
Problem Summary: Placement

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Problem: Addressing

• Where should process memories be placed?
  – Topic: “Classic” memory management

• How does the compiler model memory?
  – Topic: Logical memory model

• How to deal with limited physical memory?
  – Topics: Virtual memory, paging
(More) Problems with Memory Cohabitation

• **Addressing:**
  – Compiler generates memory references
  – Unknown where process will be located

• **Protection:**
  – Modifying another process’s memory

• **Space:**
  – The more processes there are, the less memory each individually can have
Compiler’s View of Memory

• Compiler generates memory addresses
  – Needs empty region for text, data, stack
  – Ideally, very large to allow data and stack to grow
  – Alternative: three independent empty regions

• Without abstractions compiler would need to know...
  – Physical memory size
  – Where to place data (e.g., stack at high end)
    • Must avoid allocated regions in memory
Address Spaces

• Address space
  – Set of addresses for memory
• Usually linear: 0 to $N-1$ (size $N$)
• Physical Address Space
  – 0 to $N-1$, $N = \text{size}$
  – Kernel occupies lowest addresses
Virtual vs. Physical Addressing

- **Virtual addresses**
  - Assumes separate memory starting at 0
  - Compiler generated
  - Independent of location in physical memory

- **OS**: Map virtual to physical
When should we perform the mapping from virtual to physical address? Why?

A. When the process is initially loaded: convert all the addresses to physical addresses.

B. When the process is running: map the addresses as they’re used.

C. Perform the mapping at some other time. When?
Hardware for Virtual Addressing

- Base register filled with start address
- To translate address, add base
- Achieves relocation
- To move process: change base
Hardware for Virtual Addressing

- Base register filled with start address
- To translate address, add base
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\[ P_2 \]

\[ P_1 \]

\[ P_3 \]
Hardware for Virtual Addressing

- Base register filled with start address
- To translate address, add base
- Achieves relocation
- To move process: change base
- Protection?
Protection

• Bound register works with base register
• Is address < bound
  – Yes: add to base
  – No: invalid address, invoke OS
• Achieves protection

When would we need to update these base & bound registers?
Memory Registers Part of Context

• On Every Context Switch
  – Load base/bound registers for selected process
  – Only kernel does loading of these registers
  – Kernel must be protected from all processes

• Benefit
  – Allows each process to be separately located
  – Protects each process from all others
Problem Summary: Addressing

- Compiler has no idea where, in physical memory, the process’s data will be.
- Compiler generates instructions to access VAS.
- General solution: OS must translate process’s VAS accesses to the corresponding physical memory location.
Problem Summary: Addressing

- General solution: OS must translate process’s VAS accesses to the corresponding physical memory location.

When the process tries to access a virtual address, the OS translates it to the corresponding physical address.

movl (address 0x74), %eax
Problem Summary: Addressing

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When the process tries to access a virtual address, the OS translates it to the corresponding physical address.

```
movl (address 0x74), %eax
```
Let’s combine these ideas:

1. Allow process memory to be divided up into multiple pieces.

2. Keep state in OS (+ hardware/registers) to map from virtual addresses to physical addresses.

Result: Keep a table to store the mapping of each region.
Problem Summary: Addressing

- General solution: OS must translate process’s VAS accesses to the corresponding physical memory location.

When the process tries to access a virtual address, the OS translates it to the corresponding physical address.

OS must keep a table, for each process, to map VAS to PAS. One entry per divided region.

```assembly
movl (address 0x74), %eax
```
Two (Real) Approaches

- Segmented address space/memory
  - Partition address space and memory into segments
  - Segments are generally different sizes

- Paged address space/memory
  - Partition address space and memory into pages
  - All pages are the same size
Two (Real) Approaches

- Segmented address space/memory
  - Partition address space and memory into segments
  - Segments are generally different sizes
- Paged address space/memory
  - Partition address space and memory into pages
  - **All pages are the same size**

In this class, we’re only going to look at paging, the most common method today.
Paging Vocabulary

• For each process, the **virtual** address space is divided into fixed-size **pages**.

• For the system, the **physical** memory is divided into fixed-size **frames**.

• **The size of a page is equal to that of a frame.**
  - Often 4 KB in practice.
Main Idea

• ANY virtual page can be stored in any available frame.
  – Makes finding an appropriately-sized memory gap very easy – they’re all the same size.

• For each process, OS keeps a table mapping each virtual page to physical frame.
Main Idea

• ANY virtual page can be stored in any available frame.
  – Makes finding an appropriately-sized memory gap very easy – they’re all the same size.

Implications for fragmentation?

External: goes away. No more awkwardly-sized, unusable gaps.

Internal: About the same. Process can always request memory and not use it.
Addressing

• Like we did with caching, we’re going to chop up memory addresses into partitions.

• Virtual addresses:
  – High-order bits: page #
  – Low-order bits: offset within the page

• Physical addresses:
  – High-order bits: frame #
  – Low-order bits: offset within the frame
Example: 32-bit virtual addresses

• Suppose we have 8-KB (8192-byte) pages.
• We need enough bits to individually address each byte in the page.
  – How many bits do we need to address 8192 items?
Example: 32-bit virtual addresses

- Suppose we have 8-KB (8192-byte) pages.
- We need enough bits to individually address each byte in the page.
  - How many bits do we need to address 8192 items?
    - \(2^{13} = 8192\), so we need 13 bits.
  - Lowest 13 bits: offset within page.
Example: 32-bit virtual addresses

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- Remaining 19 bits: page number.
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Address Partitioning

Virtual address:

We’ll call these bits $p$.  

Physical address:

We’ll call these bits $i$.  

We’ll (still) call these bits $i$.  

Once we’ve found the frame, which byte(s) do we want to access?
Address Partitioning

Virtual address:

We’ll call these bits $p$.  

We’ll call these bits $i$.  

OS Page Table For Process

Where is this page in physical memory?  
(In which frame?)

Physical address:

We’ll call these bits $f$.  

Once we’ve found the frame, which byte(s) do we want to access?  

We’ll (still) call these bits $i$.  

## Address Translation

### Logical Address

<table>
<thead>
<tr>
<th>Page $p$</th>
<th>Offset $i$</th>
</tr>
</thead>
</table>

- **Page Table**
  - V
  - R
  - D
  - Frame
  - Perm
  - ...

### Physical Memory
Address Translation

Logical Address

Page $p$  Offset $i$

Page Table

Physical Memory
Address Translation

Logical Address

Page \( p \)  |  Offset \( i \)
---|---

Physical Address

Physical Memory
Page Table

• One table per process
• Table entry elements
  – V: valid bit
  – R: referenced bit
  – D: dirty bit
  – Frame: location in phy mem
  – Perm: access permissions
• Table parameters in memory
  – Page table base register
  – Page table size register
Address Translation

• Physical address = frame of $p$ + offset $i$
• First, do a series of checks
Check if Page $p$ is Within Range

Logical Address

Page $p$ | Offset $i$
---|---

PTBR
PTSR

$p < \text{PTSR}$

Physical Address

V | R | D | Frame | Perm | ...

Frame
Check if Page Table Entry $p$ is Valid

<table>
<thead>
<tr>
<th>Logical Address</th>
</tr>
</thead>
<tbody>
<tr>
<td>Page $p$</td>
</tr>
<tr>
<td>Offset $i$</td>
</tr>
</tbody>
</table>

- **PTBR**
- **PTSR**

- **V == 1**
- **Physical Address**
Check if Operation is Permitted

Logical Address

Page $p$  Offset $i$

PTBR  PTSR

Perm (op)

V  R  D  Frame  Perm ...

Physical Address
Translate Address

Logical Address

Page $p$  Offset $i$

PTBR  PTSR

V  R  D  Frame  Perm  ...

concat

Physical Address
Physical Address by Concatenation

Logical Address

Page \( p \) \hspace{1cm} \text{Offset} \ i

\begin{align*}
\text{PTBR} \quad &\quad \text{PTSR} \\
\end{align*}

\begin{align*}
|V| \: |R| \: |D| \: \text{Frame} \: \text{Perm} \: \ldots
\end{align*}

Physical Address

Frame \( f \) \hspace{1cm} \text{Offset} \ i
Sizing the Page Table

Logical Address

Number of bits \( n \) specifies max size of table, where number of entries = \( 2^n \)

Number of bits needed to address physical memory \textit{in units of frames}

Number of bits specifies page size
Example of Sizing the Page Table

• Given: 32 bit virtual addresses, 1 GB physical memory
  – Address partition: 20 bit page number, 12 bit offset
Example of Sizing the Page Table

- Given: 32 bit virtual addresses, 1 GB physical memory
  - Address partition: 20 bit page number, 12 bit offset
How many entries (rows) will there be in this page table?

A. $2^{12}$, because that’s how many the offset field can address
B. $2^{20}$, because that’s how many the page field can address
C. $2^{30}$, because that’s how many we need to address 1 GB
D. $2^{32}$, because that’s the size of the entire address space
Example of Sizing the Page Table

- Given: 32 bit virtual addresses, 1 GB physical memory
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Example of Sizing the Page Table

- Given: 32 bit virtual addresses, 1 GB physical memory
  - Address partition: 20 bit page number, 12 bit offset
What will be the frame size, in bytes?

A. 2^{12}, because that’s how many bytes the offset field can address
B. 2^{20}, because that’s how many bytes the page field can address
C. 2^{30}, because that’s how many bytes we need to address 1 GB
D. 2^{32}, because that’s the size of the entire address space
Example of Sizing the Page Table

- **Page** $p$: 20 bits
- **Offset** $i$: 12 bits

20 bits to address $2^{20} = 1$ M entries

Page size = frame size = $2^{12} = 4096$ bytes

- Given: 32 bit virtual addresses, 1 GB physical memory
  - Address partition: 20 bit page number, 12 bit offset
How many bits do we need to store the frame number?

- Given: 32 bit virtual addresses, 1 GB physical memory
  - Address partition: 20 bit page number, 12 bit offset
- A: 12  B: 18  C: 20  D: 30  E: 32
Example of Sizing the Page Table

- Given: 32 bit virtual addresses, 1 GB physical memory
  - Address partition: 20 bit page number, 12 bit offset

Page $p$: 20 bits
Offset $i$: 12 bits

- 20 bits to address $2^{20} = 1$ M entries
- 18 bits to address $2^{30}/2^{12}$ frames

Page size = frame size = $2^{12} = 4096$ bytes

Size of an entry?
How big is an entry, in bytes?
(Round to a power of two bytes.)

- Given: 32 bit virtual addresses, 1 GB physical memory
  - Address partition: 20 bit page number, 12 bit offset
- A: 1   B: 2   C: 4   D: 8
Example of Sizing the Page Table

- Given: 32 bit virtual addresses, 1 GB physical memory
  - Address partition: 20 bit page number, 12 bit offset

Page $p$: 20 bits

- 20 bits to address $2^{20} = 1$ M entries

Offset $i$: 12 bits

- 18 bits to address $2^{30}/2^{12}$ frames

Page size = frame size = $2^{12} = 4096$ bytes

- 4 bytes needed to contain $24 (1+1+1+18+3+...)$ bits

Total table size?
Example of Sizing the Page Table

- **Page p**: 20 bits
- **Offset i**: 12 bits

20 bits to address $2^{20} = 1$ M entries

18 bits to address $2^{30}/2^{12}$ frames

4 bytes needed to contain $24 (1+1+1+18+3+...)$ bits

Page size = frame size = $2^{12} = 4096$ bytes

Table size = $1$ M x 4 = 4 MB

- 4 MB of bookkeeping for *every process*?
  - 200 processes -> 800 MB just to store page tables...
Concerns

• We’re going to need a ton of memory just for page tables...

• Wait, if we need to do a lookup in our page table, which is in memory, every time a process accesses memory...
  – Isn’t that slowing down memory by a factor of 2?
Multi-Level Page Tables
(You’re not responsible for this. Take an OS class for the details.)

Logical Address

1st-level Page $d$ | 2nd-level Page $p$ | Offset $i$

Points to (base) frame containing 2nd-level page table

Reduces memory usage SIGNIFICANTLY: only allocate page table space when we need it. More memory accesses though...
Cost of Translation

• Each lookup costs another memory reference
  – For each reference, additional references required
  – Slows machine down by factor of 2 or more

• Take advantage of locality
  – Most references are to a small number of pages
  – Keep translations of these in high-speed memory (a cache for page translation)
Problem Summary: Addressing

- General solution: OS must translate process’s VAS accesses to the corresponding physical memory location.

When the process tries to access a virtual address, the OS translates it to the corresponding physical address.

OS must keep a table, for each process, to map VAS to PAS. One entry per divided region.

```assembly
movl (address 0x74), %eax
```
Problem: Storage

• Where should process memories be placed?
  – Topic: “Classic” memory management

• How does the compiler model memory?
  – Topic: Logical memory model

• How to deal with limited physical memory?
  – Topics: Virtual memory, paging
Recall “Storage Problem”

• We must keep multiple processes in memory, but how many?
  – Lots of processes: they must be small
  – Big processes: can only fit a few

• How do we balance this tradeoff?

Locality to the rescue!
VM Implications

• Not all pieces need to be in memory
  – Need only piece being referenced
  – Other pieces can be on disk
  – Bring pieces in only when needed
• Illusion: there is much more memory
• What’s needed to support this idea?
  – A way to identify whether a piece is in memory
  – A way to bring in pieces (from where, to where?)
  – Relocation (which we have)
Virtual Memory based on Paging

• Before
  – All virtual pages were in physical memory
Virtual Memory based on Paging

• Now
  – All virtual pages reside on disk
  – Some also reside in physical memory (which ones?)
• Ever been asked about a swap partition on Linux?
Sample Contents of Page Table Entry

<table>
<thead>
<tr>
<th>Valid</th>
<th>Ref</th>
<th>Dirty</th>
<th>Frame number</th>
<th>Prot: rwx</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

- Valid: is entry valid (page in physical memory)?
- Ref: has this page been referenced yet?
- Dirty: has this page been modified?
- Frame: what frame is this page in?
- Protection: what are the allowable operations?
  - read/write/execute
A page fault occurs. What must we do in response?

A. Find the faulting page on disk.

B. Evict a page from memory and write it to disk.

C. Bring in the faulting page and retry the operation.

D. Two of the above

E. All of the above
Address Translation and Page Faults

- Get entry: index page table with page number
- If valid bit is off, page fault
  - Trap into operating system
  - Find page on disk (kept in kernel data structure)
  - Read it into a free frame
    - may need to make room: page replacement
  - Record frame number in page table entry, set valid
  - Retry instruction (return from page-fault trap)
Page Faults are Expensive

• Disk: 5-6 orders magnitude slower than RAM
  – Very expensive; but if very rare, tolerable
• Example
  – RAM access time: 100 nsec
  – Disk access time: 10 msec
  – \( p = \) page fault probability
  – Effective access time: \( 100 + p \times 10,000,000 \) nsec
  – If \( p = 0.1\% \), effective access time = 10,100 nsec!
Handing faults from disk seems very expensive. How can we get away with this in practice?

A. We have lots of memory, and it isn’t usually full.

B. We use special hardware to speed things up.

C. We tend to use the same pages over and over.

D. This is too expensive to do in practice!
Principle of Locality

• Not all pieces referenced uniformly over time
  – Make sure most referenced pieces in memory
  – If not, thrashing: constant fetching of pieces

• References cluster in time/space
  – Will be to same or neighboring areas
  – Allows prediction based on past
Page Replacement

• Goal: remove page(s) not exhibiting locality

• Page replacement is about
  – which page(s) to remove
  – when to remove them

• How to do it in the cheapest way possible
  – Least amount of additional hardware
  – Least amount of software overhead
Basic Page Replacement Algorithms

• FIFO: select page that is oldest
  – Simple: use frame ordering
  – Doesn’t perform very well (oldest may be popular)
• OPT: select page to be used furthest in future
  – Optimal, but requires future knowledge
  – Establishes best case, good for comparisons
• LRU: select page that was least recently used
  – Predict future based on past; works given locality
  – Costly: time-stamp pages each access, find least
• Goal: minimize replacements (maximize locality)
Summary

• We give each process a virtual address space to simplify process execution.

• OS maintains mapping of virtual address to physical memory location (e.g., in page table).
  – One page table for every process
  – TLB hardware helps to speed up translation

• Provides the abstraction of very large memory: not all pages need be resident in memory
  – Bring pages in from disk on demand