

# CS 31: Intro to Systems C Programming

L03: C programming & Data representation

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# Announcements

- HW1 is due Thursday before class
  - up to groups of four
  - invitations sent from gradescope
- Lab 1 is due Thursday, 11.59 PM
- Clickers will count for credit from this week

# Reading Quiz

- Note the red border!
- 1 minute per question
- No talking, no laptops, phones during the quiz

# Class today...let's try something different

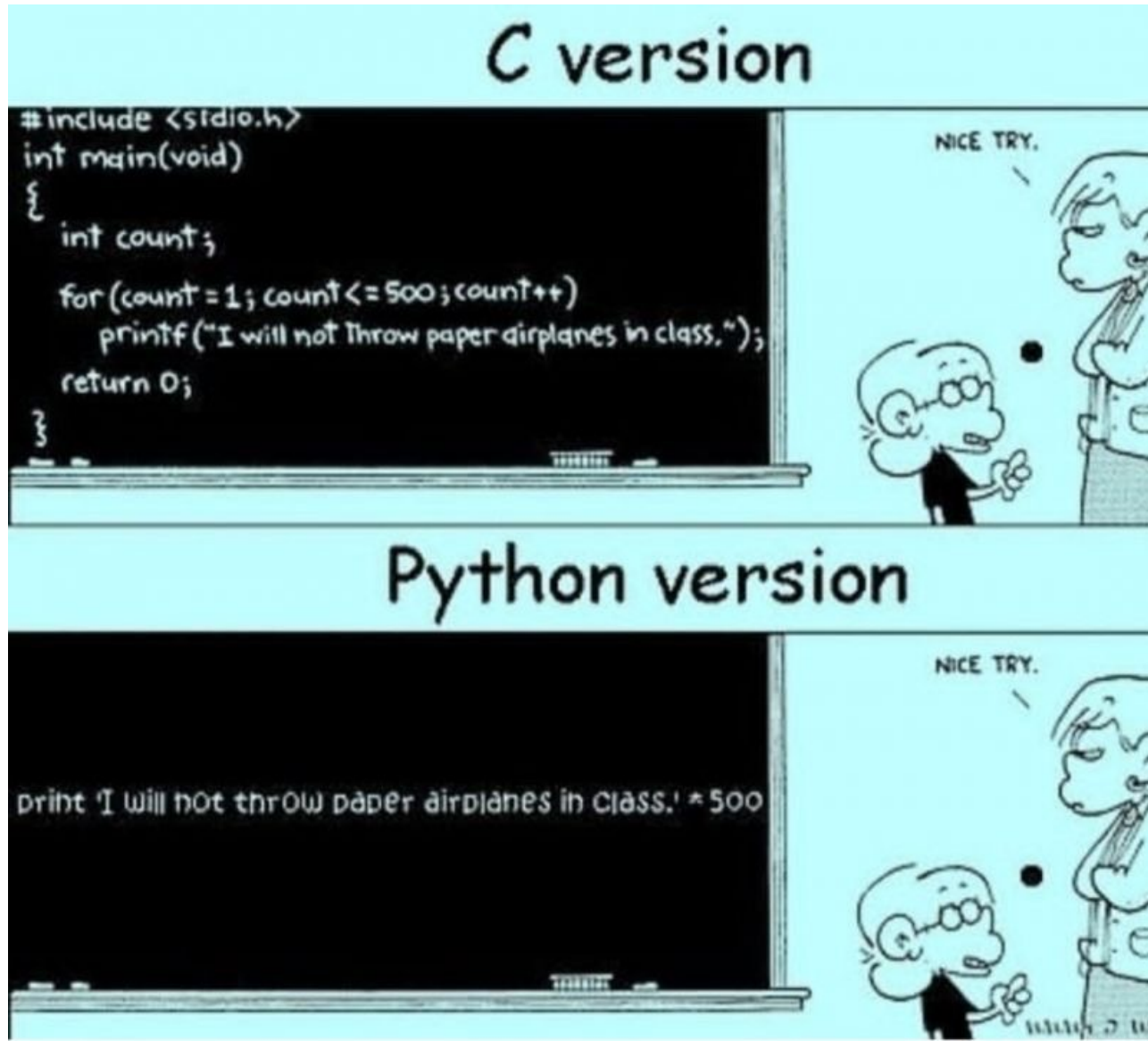
- reading quiz (5 mins)
  - content block /recap (15 mins)
  - group discussions (15 mins)
  - content block 2 (10 mins)
  - group discussions (15 mins)
- end of class---

# Agenda

- C programming
  - arrays, strings
  - functions and stack diagrams
  - structs
  - C is NOT the focus of this course: ask questions if you have them!
- Data representation
  - number systems + conversion
  - data types, storage
  - sizes, representation
  - signedness

# Python versus C: Paradigms

<https://devrant.com/rants/1755638/c-vs-python>



Recap

# Recap: Types in C

- All variables have an explicit type!

- `<variable type> <variable name>;`

- Examples:

```
int humidity;
```

```
humidity = 20;
```

```
float temperature;
```

```
temperature = 32.5
```



# Recap: An Example with Local Variables

```
/* a multiline comment:
   anything between slashdot and dotslash */

#include <stdio.h> // C's standard I/O library (for printf)

int main() {
    // first: declare main's local variables
    int x, y;
    float z;

    // followed by: main function statements
    x = 6;
    y = (x + 3)/2; //x and y are both ints
    z = x; //z is a float, value of x is converted to a float
    z = (z + 3)/2;

    printf(...) // Print x, y, z
}
```

Clicker choices



|   | X        | Y        | Z          |
|---|----------|----------|------------|
| A | 4        | 4        | 4          |
| B | 6        | 4        | 4          |
| C | 6        | 4.5      | 4          |
| D | <b>6</b> | <b>4</b> | <b>4.5</b> |
| E | 6        | 4.5      | 4.5        |

# Recap: Boolean values in C

- **Zero (0) is false, any non-zero value is true**
- **Logical** (operands int “boolean”->result int “boolean”):
  - ! (not): inverts truth value
  - && (and): true if both operands are true
  - || (or): true if either operand is true

Do the following statements evaluate to True or False?

#1: `(!10) || (5 > 2)`

#2: `(-1) && ((!5) > -1)`

Clicker choices

|   | #1    | #2    |
|---|-------|-------|
| A | True  | True  |
| B | True  | False |
| C | False | True  |
| D | False | False |

# Recap: Conditional Statements

## Chaining if-else if

```
if(<boolean expr1>) {  
    if-expr1-true-body  
} else if (<bool expr2>){  
    else-if-expr2-true-body  
    (expr1 false)  
}  
...  
} else if (<bool exprN>){  
    else-if-exprN-true-body  
}
```

## With optional else:

```
if(<boolean expr1>) {  
    if-expr1-true-body  
} else if (<bool expr2>){  
    else-if-expr2-true-body  
}  
...  
} else if (<bool exprN>){  
    else-if-exprN-true-body  
} else {  
    else body  
    (all exprX's false)  
}
```

Very similar to Python, just remember { } are blocks

# Recap: For loops: different than Python's

```
for (<init>; <cond>; <step>) {  
    for-loop-body-statements  
}  
<next stmt after loop>;
```

1. Evaluate <init> one time, when first eval **for** statement
2. Evaluate <cond>, if it is false, drop out of the loop (<next stmt after>)
3. Evaluate the statements in the for loop body
4. Evaluate <step>
5. Goto step (2)

```
for(i=1; i <= 10; i++) { // example for loop  
    printf("%d\n", i*i);  
}
```

What does this for loop print?

# Recap: While Loops

Basically identical to Python while loops:

```
while(<boolean expr>) {  
    while-expr-true-body  
}
```

```
x = 20;  
while (x < 100) {  
    y = y + x;  
    x += 4; // x = x + 4;  
}  
<next stmt after loop>;
```

```
x = 20;  
while(1) {  
    y = y + x;  
    x += 4;  
    if(x >= 100) {  
        break; // break out of loop  
    }  
}  
<next stmt after loop>;
```

# Data Collections in C

- Many complex data types out there (CS 35)
- C has a few simple ones built-in:
  - Arrays
  - Strings (arrays of characters)
  - Structures (`struct`)
- Often combined in practice, e.g.:
  - An array of structs
  - A struct containing strings

# Arrays and Strings

- C's support for collections of values
  - Array buckets store a single type of value
  - There is no “string” data type ☹️
  - Specify max capacity (num buckets) when you declare an array variable (single memory chunk)

```
<type> <var_name>[<num buckets>];
```

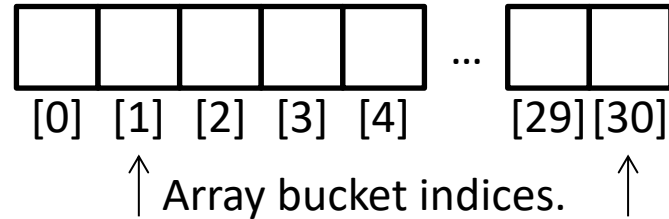
```
int arr[5]; // an array of 5 integers
```

```
float rates[40]; // an array of 40 floats
```

# Array Characteristics

```
int january_temps[31]; // Daily high temps
```

“january\_temps”  
Location of [0] in  
memory.



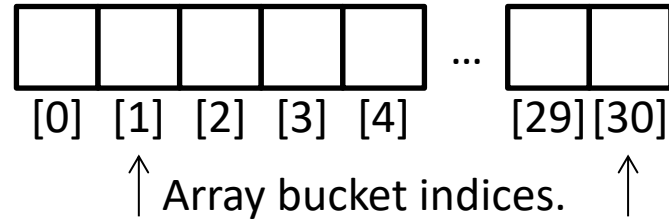
- Indices start at 0! Why?
- Array variable name means, to the compiler, the beginning of the memory chunk. (The memory **address**)
  - january\_temps” (without brackets!) Location of [0] in memory.
  - Keep this in mind, we’ll return to it soon (functions).



# Array Characteristics

```
int january_temps[31]; // Daily high temps
```

“january\_temps”  
Location of [0] in  
memory.



- Indices start at 0! Why?
- **The index refers to an offset from the start of the array**
  - e.g., `january_temps[3]` means “three integers forward from the starting address of `january_temps`”

# Characters and Strings

A character (type `char`) is numerical value that holds one letter.

```
char my_letter = 'w'; // Note: single quotes
```

What is the numerical value?

- `printf(“%d %c”, my_letter, my_letter);`
- Would print: 119 w

Why is 'w' equal to 119?

- ASCII Standard says so.
- American Standard Code for Information Interchange

| Dec | Hex | Char             | Dec | Hex | Char  | Dec | Hex | Char | Dec        | Hex | Char |
|-----|-----|------------------|-----|-----|-------|-----|-----|------|------------|-----|------|
| 0   | 00  | Null             | 32  | 20  | Space | 64  | 40  | @    | 96         | 60  | `    |
| 1   | 01  | Start of heading | 33  | 21  | !     | 65  | 41  | A    | 97         | 61  | a    |
| 2   | 02  | Start of text    | 34  | 22  | "     | 66  | 42  | B    | 98         | 62  | b    |
| 3   | 03  | End of text      | 35  | 23  | #     | 67  | 43  | C    | 99         | 63  | c    |
| 4   | 04  | End of transmit  | 36  | 24  | \$    | 68  | 44  | D    | 100        | 64  | d    |
| 5   | 05  | Enquiry          | 37  | 25  | %     | 69  | 45  | E    | 101        | 65  | e    |
| 6   | 06  | Acknowledge      | 38  | 26  | &     | 70  | 46  | F    | 102        | 66  | f    |
| 7   | 07  | Audible bell     | 39  | 27  | '     | 71  | 47  | G    | 103        | 67  | g    |
| 8   | 08  | Backspace        | 40  | 28  | (     | 72  | 48  | H    | 104        | 68  | h    |
| 9   | 09  | Horizontal tab   | 41  | 29  | )     | 73  | 49  | I    | 105        | 69  | i    |
| 10  | 0A  | Line feed        | 42  | 2A  | *     | 74  | 4A  | J    | 106        | 6A  | j    |
| 11  | 0B  | Vertical tab     | 43  | 2B  | +     | 75  | 4B  | K    | 107        | 6B  | k    |
| 12  | 0C  | Form feed        | 44  | 2C  | ,     | 76  | 4C  | L    | 108        | 6C  | l    |
| 13  | 0D  | Carriage return  | 45  | 2D  | -     | 77  | 4D  | M    | 109        | 6D  | m    |
| 14  | 0E  | Shift out        | 46  | 2E  | .     | 78  | 4E  | N    | 110        | 6E  | n    |
| 15  | 0F  | Shift in         | 47  | 2F  | /     | 79  | 4F  | O    | 111        | 6F  | o    |
| 16  | 10  | Data link escape | 48  | 30  | 0     | 80  | 50  | P    | 112        | 70  | p    |
| 17  | 11  | Device control 1 | 49  | 31  | 1     | 81  | 51  | Q    | 113        | 71  | q    |
| 18  | 12  | Device control 2 | 50  | 32  | 2     | 82  | 52  | R    | 114        | 72  | r    |
| 19  | 13  | Device control 3 | 51  | 33  | 3     | 83  | 53  | S    | 115        | 73  | s    |
| 20  | 14  | Device control 4 | 52  | 34  | 4     | 84  | 54  | T    | 116        | 74  | t    |
| 21  | 15  | Neg. acknowledge | 53  | 35  | 5     | 85  | 55  | U    | 117        | 75  | u    |
| 22  | 16  | Synchronous idle | 54  | 36  | 6     | 86  | 56  | V    | 118        | 76  | v    |
| 23  | 17  | End trans. block | 55  | 37  | 7     | 87  | 57  | W    | <u>119</u> | 77  | w    |
| 24  | 18  | Cancel           | 56  | 38  | 8     | 88  | 58  | X    | 120        | 78  | x    |
| 25  | 19  | End of medium    | 57  | 39  | 9     | 89  | 59  | Y    | 121        | 79  | y    |
| 26  | 1A  | Substitution     | 58  | 3A  | :     | 90  | 5A  | Z    | 122        | 7A  | z    |
| 27  | 1B  | Escape           | 59  | 3B  | ;     | 91  | 5B  | [    | 123        | 7B  | {    |
| 28  | 1C  | File separator   | 60  | 3C  | <     | 92  | 5C  | \    | 124        | 7C  |      |
| 29  | 1D  | Group separator  | 61  | 3D  | =     | 93  | 5D  | ]    | 125        | 7D  | }    |
| 30  | 1E  | Record separator | 62  | 3E  | >     | 94  | 5E  | ^    | 126        | 7E  | ~    |
| 31  | 1F  | Unit separator   | 63  | 3F  | ?     | 95  | 5F  | _    | 127        | 7F  | □    |

Characters  
and Strings

\$ man ascii

119 = w



# Characters and Strings

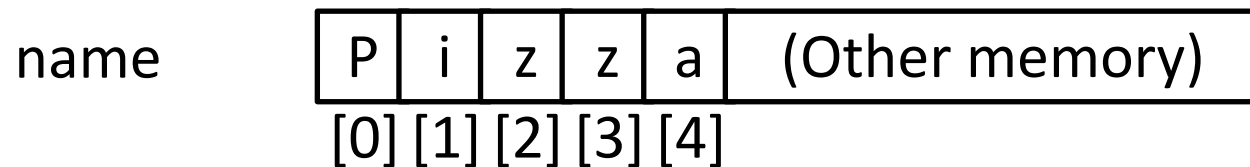
- A character (type `char`) is numerical value that holds one letter.
- A string is a memory block containing characters, one after another...

- Examples:

```
char food[6] = "Pizza";
```

Hmm, suppose we used `printf` and `%s` to print name.

How does it know where the string ends and other memory begins?



0 is the "Null character"

Special stuff over here in the lower values.

| Dec | Hex | Char             | Dec | Hex | Char  | Dec | Hex | Char | Dec        | Hex | Char |
|-----|-----|------------------|-----|-----|-------|-----|-----|------|------------|-----|------|
| 0   | 00  | Null             | 32  | 20  | Space | 64  | 40  | @    | 96         | 60  | `    |
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| 31  | 1F  | Unit separator   | 63  | 3F  | ?     | 95  | 5F  | _    | 127        | 7F  | □    |

Characters and Strings

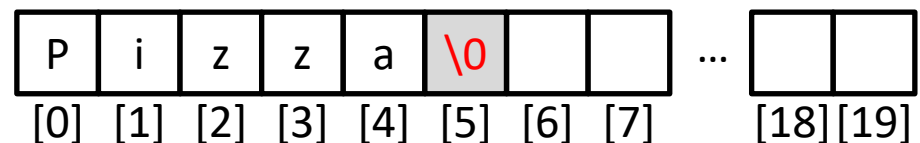
\$ man ascii



# Characters and Strings

- A character (type `char`) is numerical value that holds one letter.
- A string is a memory block containing characters, one after another, with a **null terminator** (numerical 0) at the end.
- Examples:

```
char name[20] = "Pizza";
```



# Strings in C

- C String library functions: `#include <string.h>`
  - Common functions (`strlen`, `strcpy`, etc.) make strings easier
  - Less friendly than Python strings
- More on strings later, in labs.
- For now, remember about strings:
  - Allocate enough space for null terminator!
  - If you're modifying a character array (string), don't forget to set the null terminator!
  - If you see crazy, unpredictable behavior with strings, check these two things!

# Functions and Stack Diagrams



# Functions: Specifying Types

Need to specify the **return type** of the function, and the **type of each parameter**:

```
<return type> <func name> ( <param list> ) {  
    // declare local variables first  
    // then function statements  
    return <expression>;  
}
```

```
// my_function takes 2 int values and returns an int
```

```
int my_function(int x, int y) {  
    int result;  
    result = x;  
    if(y > x) {  
        result = y+5;  
    }  
    return result*2;  
}
```

Compiler will yell at you if you try to pass the wrong type!

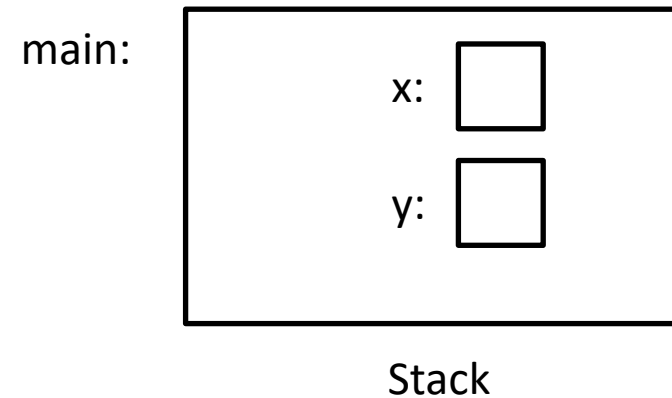
# Function Arguments

Arguments are **passed by value**

– The function gets a separate copy of the passed variable

```
int func(int a, int b) {  
    a = a + 5;  
    return a - b;  
}
```

```
int main() {  
    // declare two integers  
    → int x, y;  
    x = 4;  
    y = 7;  
    y = func(x, y);  
    printf("%d, %d", x, y);  
}
```

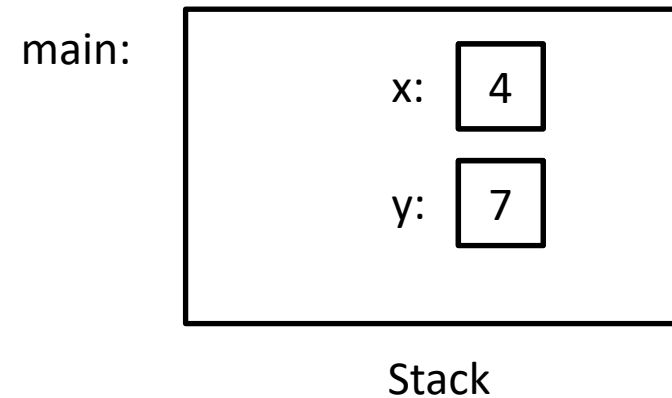


# Function Arguments

Arguments are **passed by value**

– The function gets a separate copy of the passed variable

```
int func(int a, int b) {  
    a = a + 5;  
    return a - b;  
}  
  
int main() {  
    // declare two integers  
    int x, y;  
    x = 4;  
    → y = 7;  
    y = func(x, y);  
    printf("%d, %d", x, y);  
}
```

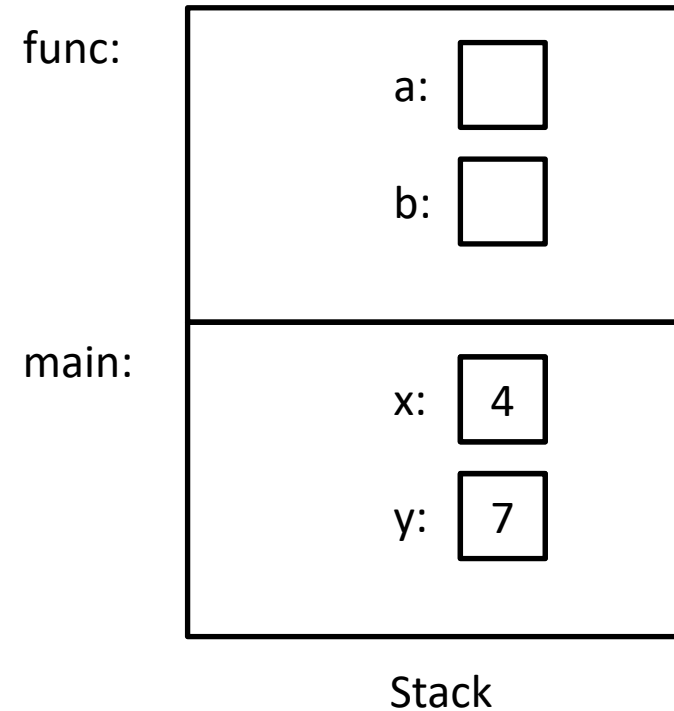


# Function Arguments

Arguments are **passed by value**

– The function gets a separate copy of the passed variable

```
int func(int a, int b) {  
    a = a + 5;  
    return a - b;  
}  
  
int main() {  
    // declare two integers  
    int x, y;  
    x = 4;  
    y = 7;  
    → y = func(x, y);  
    printf("%d, %d", x, y);  
}
```

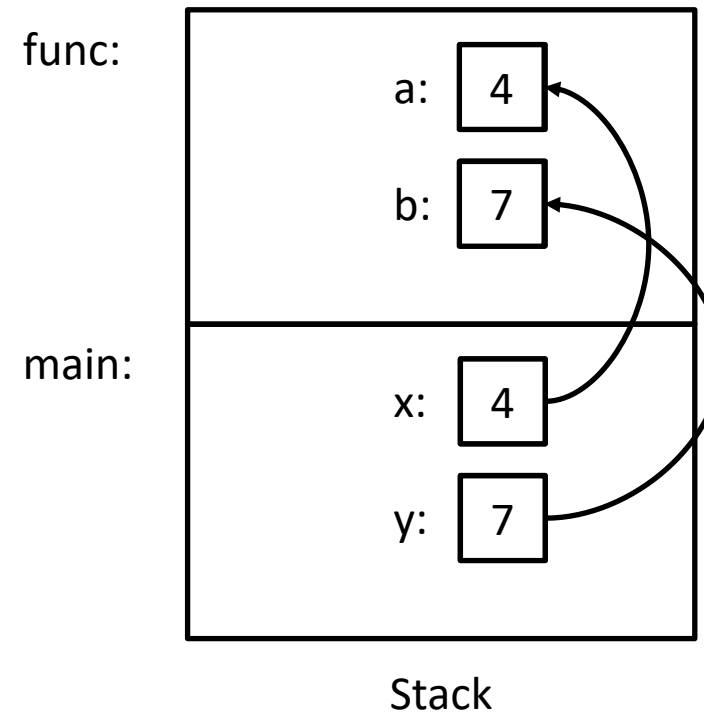


# Function Arguments

Arguments are **passed by value**

– The function gets a separate copy of the passed variable

```
→ int func(int a, int b) {  
    a = a + 5;  
    return a - b;  
}  
  
int main() {  
    // declare two integers  
    int x, y;  
    x = 4;  
    y = 7;  
    y = func(x, y);  
    printf("%d, %d", x, y);  
}
```



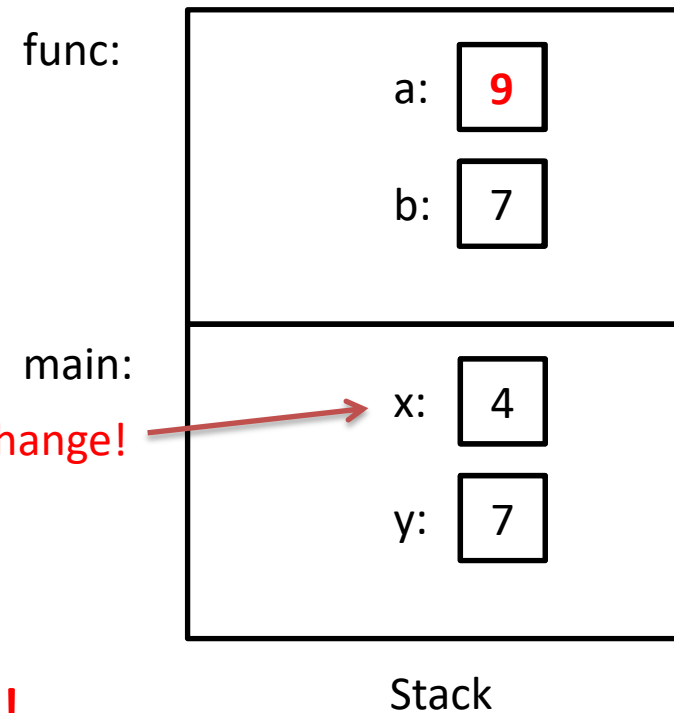
# Function Arguments

Arguments are **passed by value**

- The function gets a separate copy of the passed variable

```
int func(int a, int b) {  
→ a = a + 5;  
  return a - b;  
}  
  
int main() {  
  // declare two integers  
  int x, y;  
  x = 4;  
  y = 7;  
  y = func(x, y);  
  printf("%d, %d", x, y);  
}
```

Note: This doesn't change!



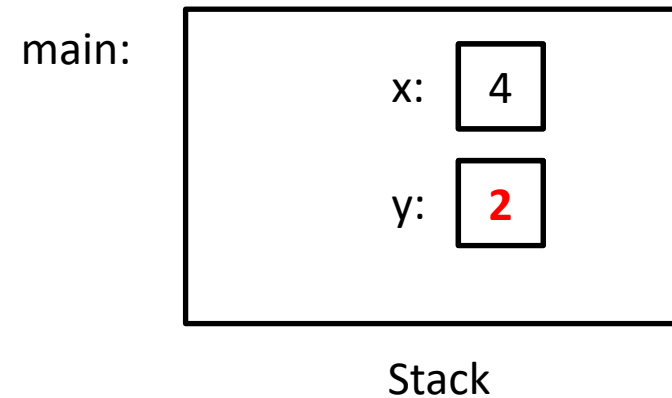
No impact on values in main!

# Function Arguments

Arguments are **passed by value**

– The function gets a separate copy of the passed variable

```
int func(int a, int b) {  
    a = a + 5;  
    return a - b;  
}  
  
int main() {  
    // declare two integers  
    int x, y;  
    x = 4;  
    y = 7;  
    → y = func(x, y);  
    printf("%d, %d", x, y);  
}
```

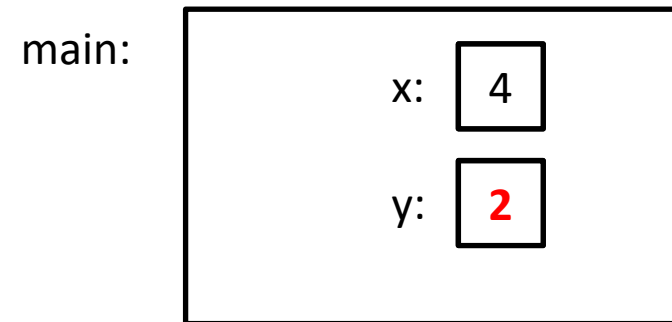


# Function Arguments

Arguments are **passed by value**

– The function gets a separate copy of the passed variable

```
int func(int a, int b) {  
    a = a + 5;  
    return a - b;  
}  
  
int main() {  
    // declare two integers  
    int x, y;  
    x = 4;  
    y = 7;  
    y = func(x, y);  
    → printf("%d, %d", x, y);  
}
```



Stack

Output: 4, 2



# What will this print?

```
int func(int a, int y, int my_array[]) {
    y = 1;
    my_array[a] = 0;
    my_array[y] = 8;
    return y;
}

int main() {
    int x;
    int values[2];

    x = 0;
    values[0] = 5;
    values[1] = 10;

    x = func(x, x, values);

    printf("%d, %d, %d", x, values[0], values[1]);
}
```

- A. 0, 5, 8
- B. 0, 5, 10
- C. 1, 0, 8
- D. 1, 5, 8
- E. 1, 5, 10

Hint: What does the name of an array mean to the compiler?

# What will this print?

```
int func(int a, int y, int my_array[]) {
    y = 1;
    my_array[a] = 0;
    my_array[y] = 8;
    return y;
}

int main() {
    int x;
    int values[2];

    x = 0;
    values[0] = 5;
    values[1] = 10;

    x = func(x, x, values);

    printf("%d, %d, %d", x, values[0], values[1]);
}
```

- A. 0, 5, 8
- B. 0, 5, 10
- C. 1, 0, 8
- D. 1, 5, 8
- E. 1, 5, 10

Hint: Still accessing the same memory location of array in func

# Discussion Block 1

# structs

- Treat a collection of values as a single type:
  - C is not an object oriented language, no classes
  - A `struct` is similar to the data part of a class
- Rules:
  1. Define a new `struct` type outside of any function
  2. Declare variables of the new struct type
  3. Use `dot notation` to `access the field values` of a struct variable

# Struct Example

Suppose we want to represent a student type.

```
struct student {
    char name[20];
    int grad_year;
    float gpa;
};
// Variable bob is of type struct student
struct student bob;
// Set name (string) with strcpy()
strcpy(bob.name, "Robert Paulson");
bob.grad_year = 2019;
bob.gpa = 3.1;

printf("Name: %s, year: %d, GPA: %f", bob.name, bob.grad_year, bob.gpa);
```

# Arrays of Structs

```
struct student {
    char name[20];
    int grad_year;
    float gpa;
};
//create an array of struct students!
struct student classroom[50];

strcpy(classroom[0].name, "Alice");
classroom[0].grad_year = 2023
classroom[0].gpa = 4.0;
```

```
// With a loop, create an army of Alice clones!
int i;
for (i = 0; i < 50; i++) {
    strcpy(classroom[i].name, "Alice");
    classroom[i].grad_year = 2023;
    classroom[i].gpa = 4.0;
}
```

# Arrays of Structs

```
struct student classroom[3];

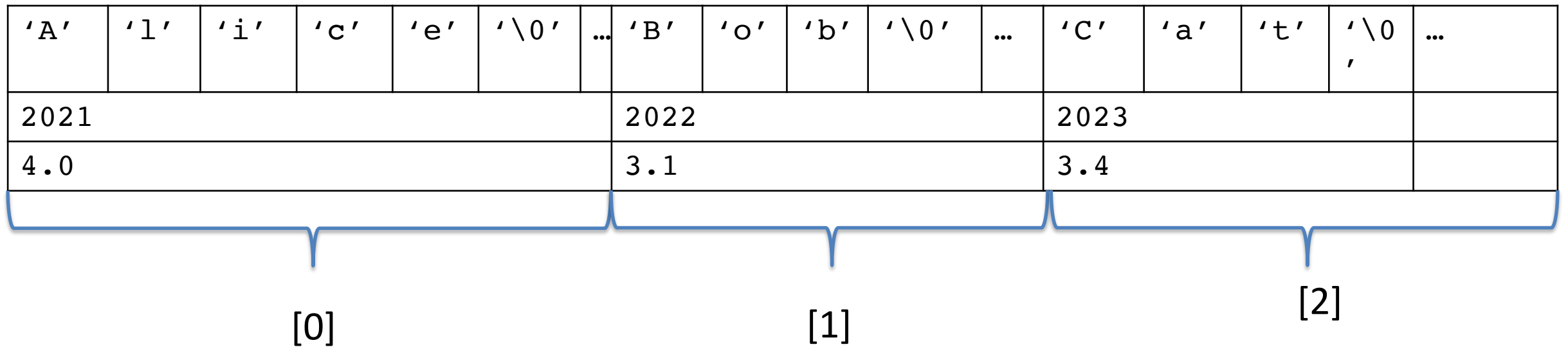
strcpy(classroom[0].name, "Alice");
classroom[0].grad_year = 2021;
classroom[0].gpa = 4.0;

strcpy(classroom[1].name, "Bob");
classroom[1].grad_year = 2022;
classroom[1].gpa = 3.1

strcpy(classroom[2].name, "Cat");
classroom[2].grad_year = 2023;
classroom[2].gpa = 3.4
```

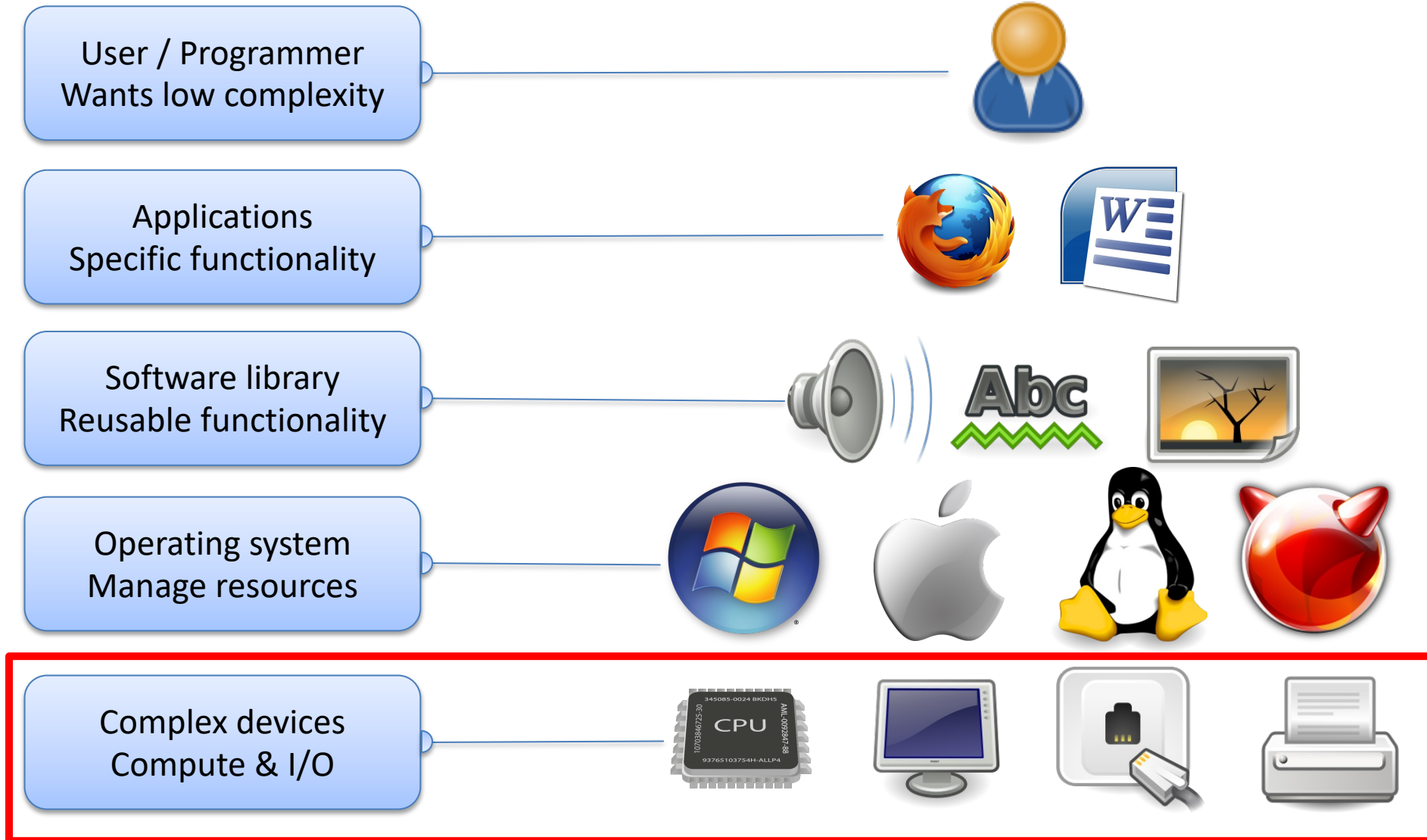
# Array of Structs: Layout in Memory

classroom: array of structs





# Abstraction



# Data Storage

- Lots of technologies out there:
  - Magnetic (hard drive, floppy disk)
  - Optical (CD / DVD / Blu-Ray)
  - Electronic (RAM, registers, ...)
- Focus on electronic for now
  - We'll see (and build) digital circuits soon
- Relatively easy to differentiate two states
  - Voltage present
  - Voltage absent

# Bits and Bytes

- Bit: a 0 or 1 value (binary)
  - HW represents as two different voltages
    - 1: the presence of voltage (**high voltage**)
    - 0: the absence of voltage (**low voltage**)
- **Byte**: 8 bits, the smallest addressable unit  
Memory: 01010101    10101010    00001111    ...  
(address)    [0]    [1]    [2]    ...
- Other names:
  - 4 bits: Nibble
  - “Word”: Depends on system, often 4 bytes

# Files

Sequence of bytes... nothing more, nothing less



# Binary Digits (BITS)

- One bit: two values (0 or 1)
- Two bits: four values (00, 01, 10, or 11)
- Three bits: eight values (000, 001, ..., 110, 111)



How many unique values can we represent with 9 bits? Why?

- One bit: two values (0 or 1)
- Two bits: four values (00, 01, 10, or 11)
- Three bits: eight values (000, 001, ..., 110, 111)

- A. 18
- B. 81
- C. 256
- D. 512
- E. Some other number of values.

How many unique values can we represent with 9 bits? Why?

- One bit: two values (0 or 1)
- Two bits: four values (00, 01, 10, or 11)
- Three bits: eight values (000, 001, ..., 110, 111)

A. 18

B. 81

C. 256

D. 512

E. Some other number of values.

# How many values?

1 bit:

0

1



# How many values?

1 bit:

2 bits:



# How many values?

1 bit:

0

1

2 bits:

0 0

0 1

1 0

1 1

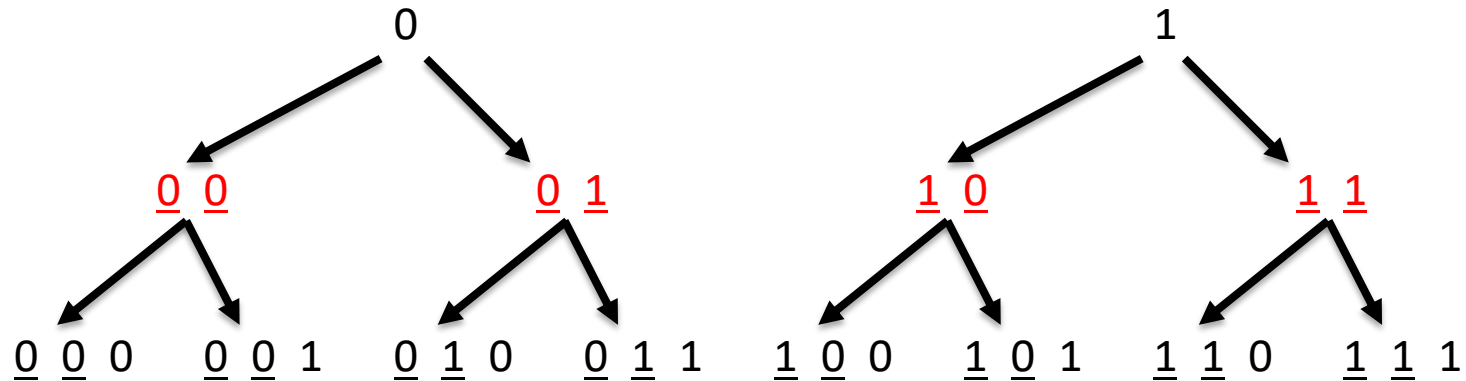
3 bits:

0 0 0    0 0 1

0 1 0    0 1 1

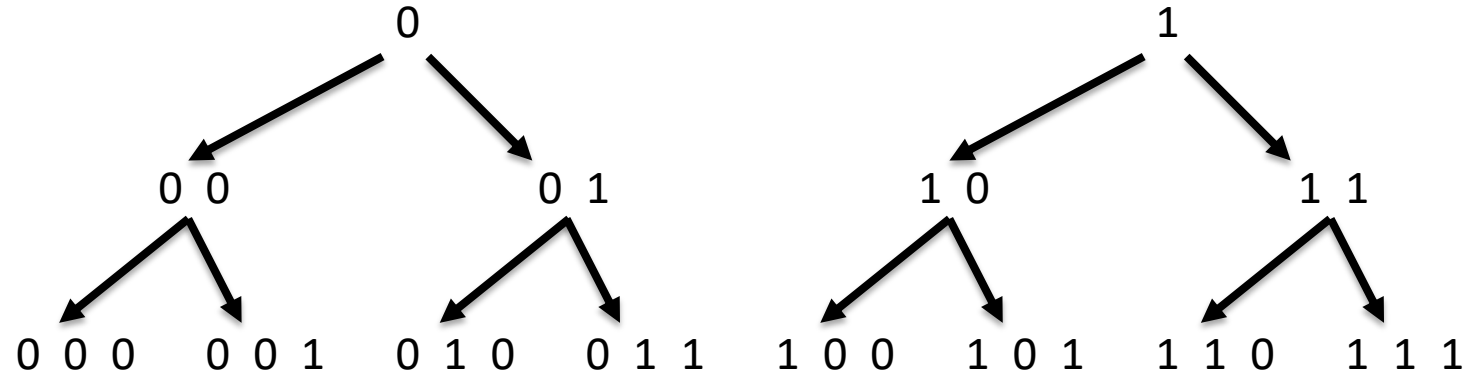
1 0 0    1 0 1

1 1 0    1 1 1



# How many values?

1 bit:



2 bits:

3 bits:

4 bits:

0 0 0 0    0 0 0 1    0 0 1 0    0 0 1 1    16 values  
0 1 0 0    0 1 0 1    0 1 1 0    0 1 1 1  
  
1 0 0 0    1 0 0 1    1 0 1 0    1 0 1 1  
1 1 0 0    1 1 0 1    1 1 1 0    1 1 1 1

N bits:  $2^N$  values

# C types and their (typical!) sizes

- 1 byte: char, unsigned char
- 2 bytes: short, unsigned short
- 4 bytes: int, unsigned int, float
- 8 bytes: long long, unsigned long long, double
- 4 or 8 bytes: long,

```
unsigned long v1;  
short s1;  
long long ll;
```

```
// prints out number of bytes  
printf("%lu %lu %lu\n", sizeof(v1), sizeof(s1), sizeof(ll));
```

WARNING: These sizes are **NOT** a guarantee. Don't always assume that every system will use these values!

How do we use this storage space (bits) to represent a value?

# Let's start with what we know...

- Digits 0-9
- Positional numbering
- Digits are composed to make larger numbers
- Known as **Base 10** representation



# Decimal number system (Base 10)

- Sequence of digits in range [0, 9]

64025



Digit #0: 1's place, "least significant digit"

Digit #1: 10's place

Digit #4: "most significant digit"

# Decimal: Base 10

A number, written as the sequence of N digits,

$$d_{n-1} \dots d_2 d_1 d_0$$

where  $d$  is in  $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$ , represents the value:

$$[d_{n-1} * 10^{n-1}] + [d_{n-2} * 10^{n-2}] + \dots + [d_1 * 10^1] + [d_0 * 10^0]$$

64025 =

$$6 * 10^4 + 4 * 10^3 + 0 * 10^2 + 2 * 10^1 + 5 * 10^0$$

$$60000 + 4000 + 0 + 20 + 5$$

# Binary: Base 2

- Used by computers to store digital values.
- Indicated by prefixing number with **0b**
- A number, written as the sequence of N digits,  $d_{n-1}...d_2d_1d_0$ , where d is in  $\{0,1\}$ , represents the value:

$$[d_{n-1} * 2^{n-1}] + [d_{n-2} * 2^{n-2}] + \dots + [d_2 * 2^2] + [d_1 * 2^1] + [d_0 * 2^0]$$



# Converting Binary to Decimal

Most significant bit  $\longrightarrow$  10001111  $\longleftarrow$  Least significant bit  
7 6 5 4 3 2 1 0

Representation:  $1 \times 2^7 + 0 \times 2^6 \dots + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$   
128 + + 8 + 4 + 2 + 1

10001111 = 143

# Hexadecimal: Base 16

- Indicated by prefixing number with 0x

A number, written as the sequence of N digits,

$$d_{n-1} \dots d_2 d_1 d_0,$$

where d is in {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F}, represents:

$$[d_{n-1} * 16^{n-1}] + [d_{n-2} * 16^{n-2}] + \dots + [d_2 * 16^2] + [d_1 * 16^1] + [d_0 * 16^0]$$

# Generalizing: Base $b$

- The meaning of a digit depends on its position in a number.

A number, written as the sequence of  $N$  digits,

$$d_{n-1} \dots d_2 d_1 d_0$$

in base  $b$  represents the value:

$$[d_{n-1} * b^{n-1}] + [d_{n-2} * b^{n-2}] + \dots + [d_2 * b^2] + [d_1 * b^1] + [d_0 * b^0]$$

Base 10:  $[d_{n-1} * 10^{n-1}] + [d_{n-2} * 10^{n-2}] + \dots + [d_1 * 10^1] + [d_0 * 10^0]$

## Other (common) number systems.

- Base 2: How data is stored in hardware.
- Base 8: Used to represent file permissions.
- Base 10: Preferred by people.
- Base 16: Convenient for representing memory addresses.
- Base 64: Commonly used on the Internet, (e.g. email attachments).

It's **all** stored as binary in the computer.

**Different representations** (or visualizations) of the **same information!**

## Discussion block 2

# Important Point...

- You can represent the same value in a variety of number systems or bases.
- It's **all** stored as binary in the computer.
  - Presence/absence of voltage.

# Hexadecimal: Base 16

- Fewer digits to represent same value
  - Same amount of information!
- Like binary, the base is power of 2
- Each digit is a “nibble”, or half a byte.

## Each hex digit is a “nibble”

- One hex digit: 16 possible values (0-9, A-F)
- $16 = 2^4$ , so **each hex digit** has exactly **four bits worth of information**.
- We can map each hex digit to a four-bit binary value.  
(helps for converting between bases)



# Each hex digit is a “nibble”

Example value: 0x1B7

Four-bit value: 1

Four-bit value: B (decimal 11)

Four-bit value: 7

In binary:    0001    1011    0111

          1    B    7

# Converting Decimal -> Binary

- Two methods:
  - division by two remainder
  - powers of two and subtraction

Method 1: decimal value  $D$ , binary result  $b$  ( $b_i$  is  $i$ th digit):

```
i = 0
while (D > 0)
    if D is odd
        set  $b_i$  to 1
    if D is even
        set  $b_i$  to 0
    i++
    D = D/2
```

Example: Converting 105

idea:

example:  $D = 105$

$b_0 = 1$

Method 1: decimal value  $D$ , binary result  $b$  ( $b_i$  is  $i$ th digit):

```
i = 0
while (D > 0)
    if D is odd
        set  $b_i$  to 1
    if D is even
        set  $b_i$  to 0
    i++
    D = D/2
```

Example: Converting 105

|       |         |                  |           |
|-------|---------|------------------|-----------|
| idea: | D       | example: D = 105 | $b_0 = 1$ |
|       | D = D/2 | D = 52           | $b_1 = 0$ |

Method 1: decimal value D, binary result b ( $b_i$  is  $i$ th digit):

```
i = 0
while (D > 0)
    if D is odd
        set  $b_i$  to 1
    if D is even
        set  $b_i$  to 0
    i++
    D = D/2
```

Example: Converting 105

idea:

```
D
D = D/2
D = D/2
D = D/2
D = D/2
D = D/2
D = D/2
D = 0 (done)
```

```
example: D = 105
D = 52
D = 26
D = 13
D = 6
D = 3
D = 1
D = 0
```

```
 $b_0 = 1$ 
 $b_1 = 0$ 
 $b_2 = 0$ 
 $b_3 = 1$ 
 $b_4 = 0$ 
 $b_5 = 1$ 
 $b_6 = 1$ 
 $b_7 = 0$ 
```

105 = 01101001



## Method 2

- $2^0 = 1, 2^1 = 2, 2^2 = 4, 2^3 = 8, 2^4 = 16, 2^5 = 32, 2^6 = 64, 2^7 = 128$

- 

To convert 105:

- Find largest power of two that's less than 105 (64)
- Subtract 64 ( $105 - 64 = \underline{41}$ ), put a 1 in  $d_6$
- Subtract 32 ( $41 - 32 = \underline{9}$ ), put a 1 in  $d_5$
- Skip 16, it's larger than 9, put a 0 in  $d_4$
- Subtract 8 ( $9 - 8 = \underline{1}$ ), put a 1 in  $d_3$
- Skip 4 and 2, put a 0 in  $d_2$  and  $d_1$
- Subtract 1 ( $1 - 1 = \underline{0}$ ), put a 1 in  $d_0$  (Done)

$$\frac{1}{d_6}$$

$$\frac{1}{d_5}$$

$$\frac{0}{d_4}$$

$$\frac{1}{d_3}$$

$$\frac{0}{d_2}$$

$$\frac{0}{d_1}$$

$$\frac{1}{d_0}$$

What is the value of 357 in binary?

- A. 101100011
- B. 101100101
- C. 101101001
- D. 101110101
- E. 110100101

$$2^0 = 1, \quad 2^1 = 2, \quad 2^2 = 4, \quad 2^3 = 8, \quad 2^4 = 16,$$
$$2^5 = 32, \quad 2^6 = 64, \quad 2^7 = 128, \quad 2^8 = 256$$