

Bubble Sort

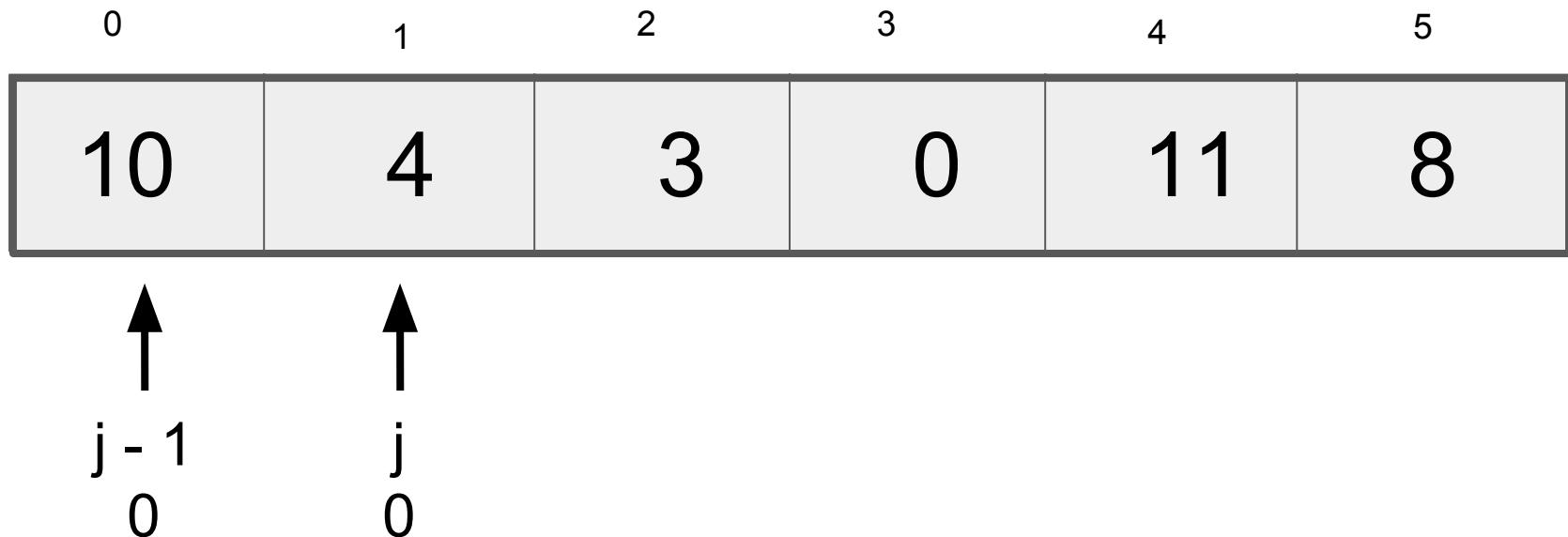
Bubble Sort

0	1	2	3	4	5
10	4	3	0	11	8

What do we do first?

Bubble Sort

len = 6

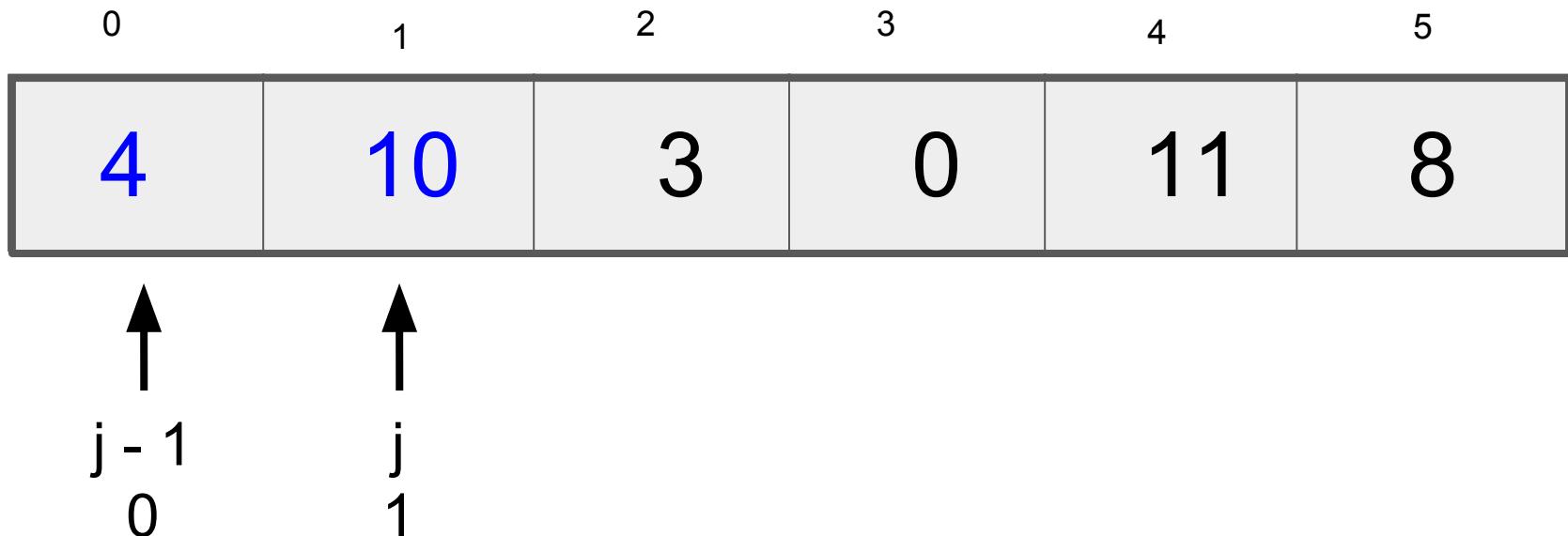


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 6

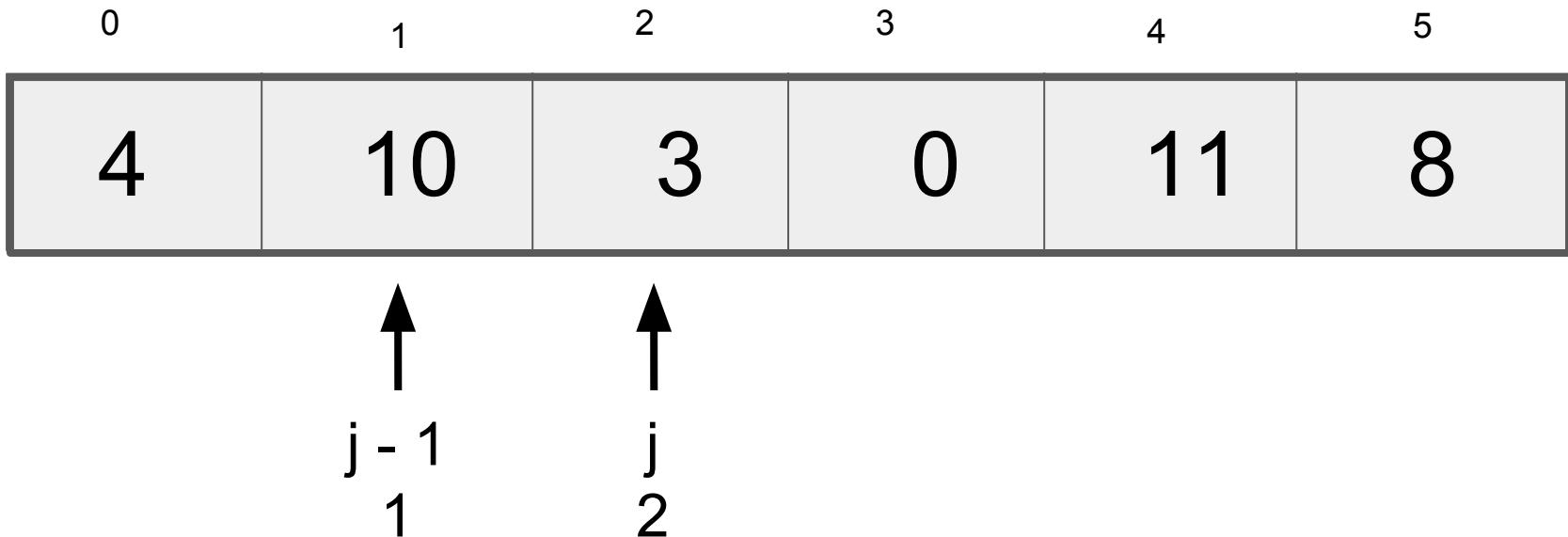


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 6

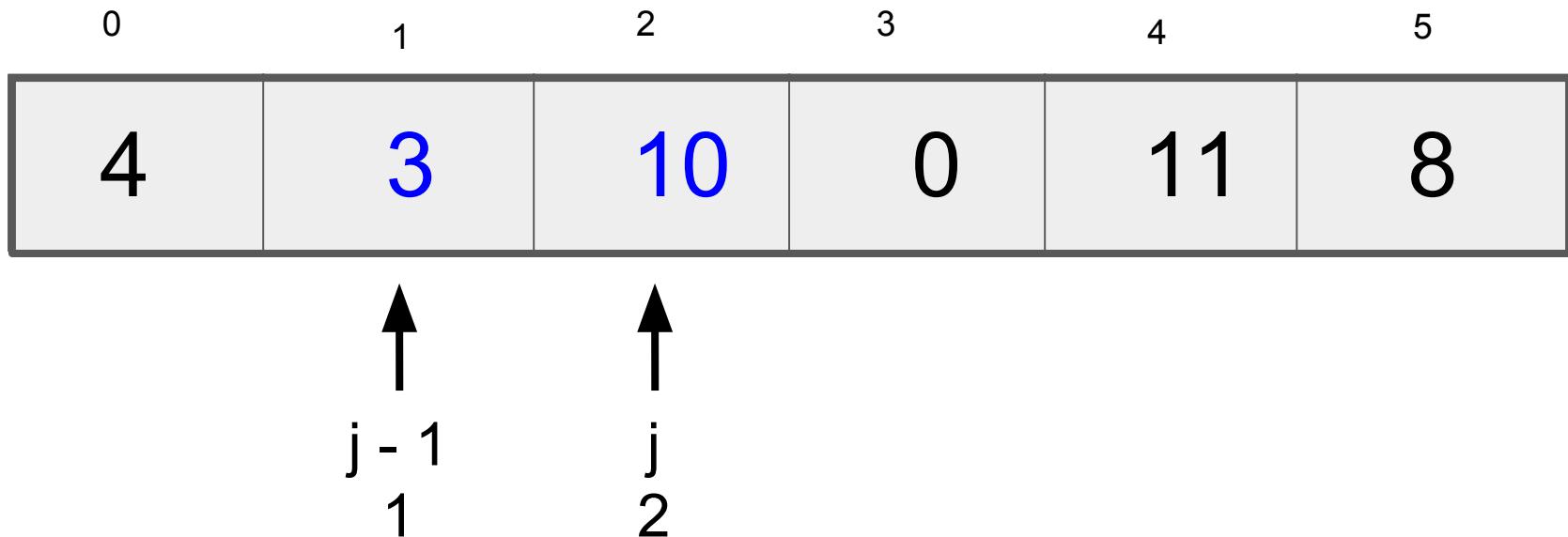


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 6



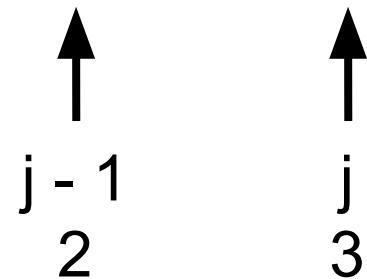
Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 6

0	1	2	3	4	5
4	3	10	0	11	8

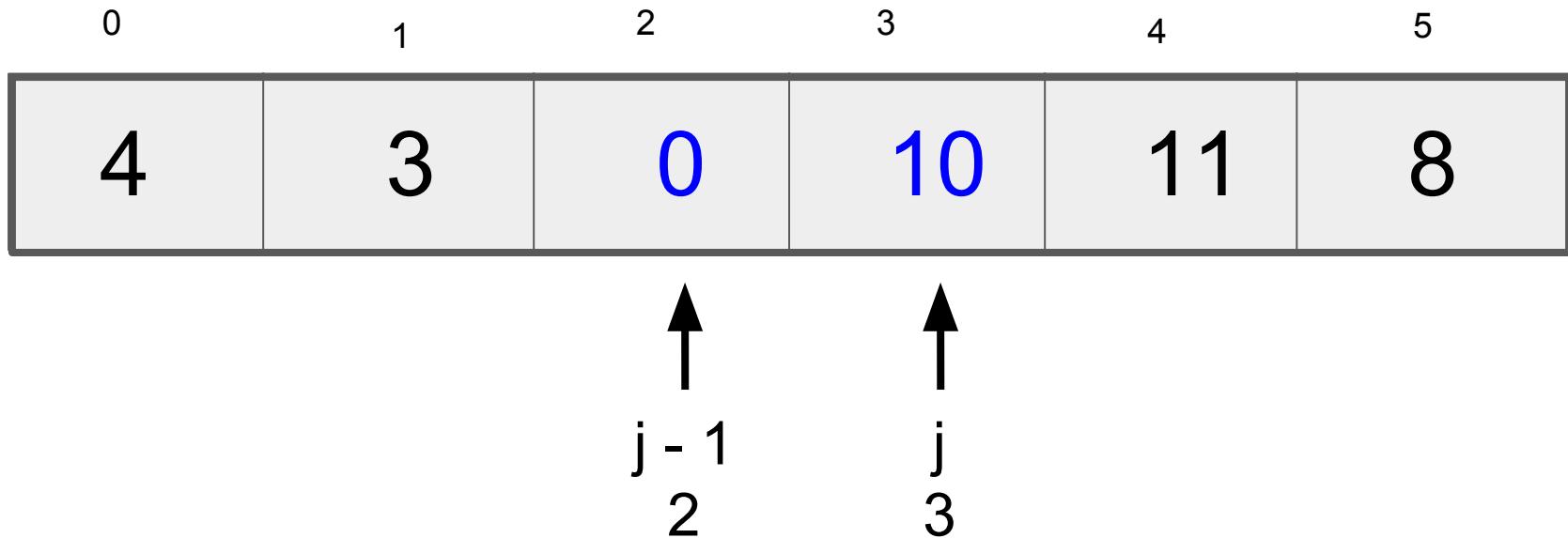


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 6

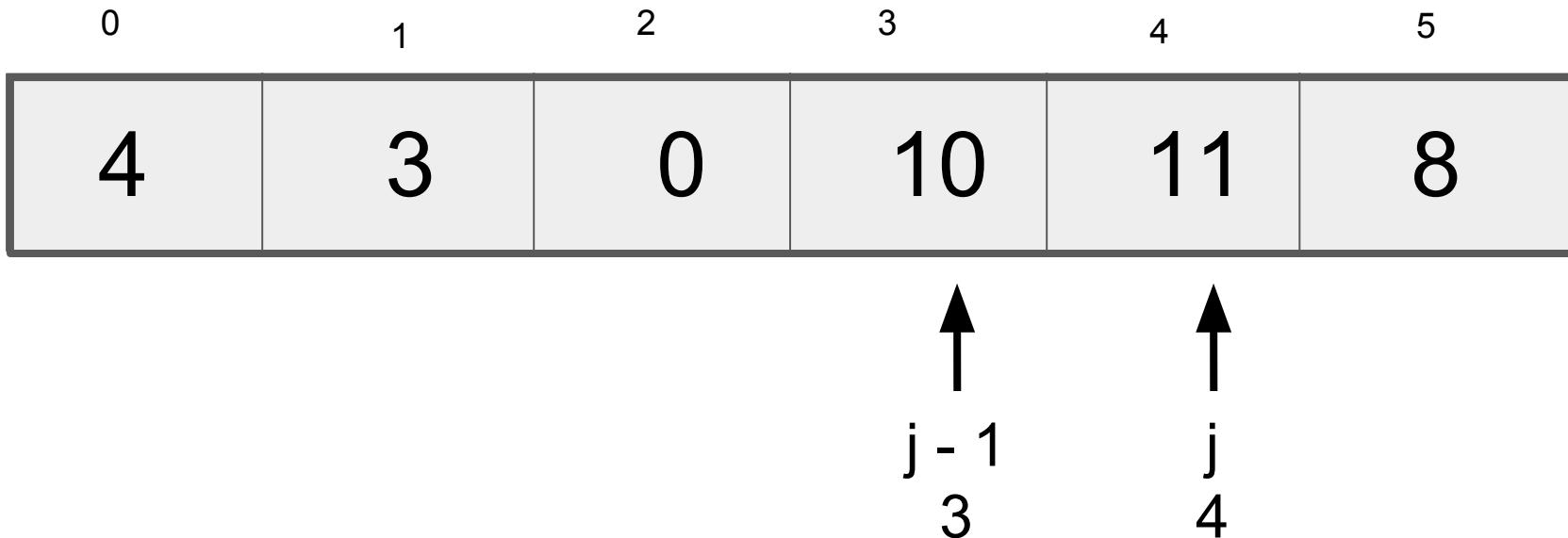


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 6

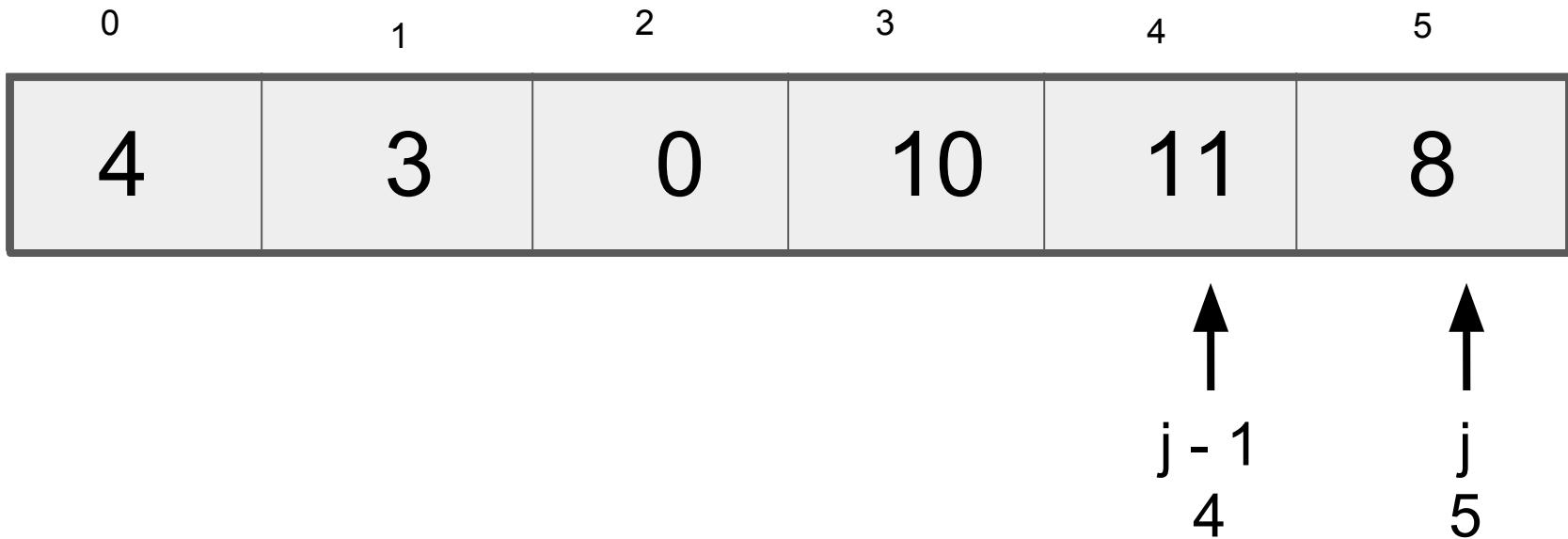


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 6

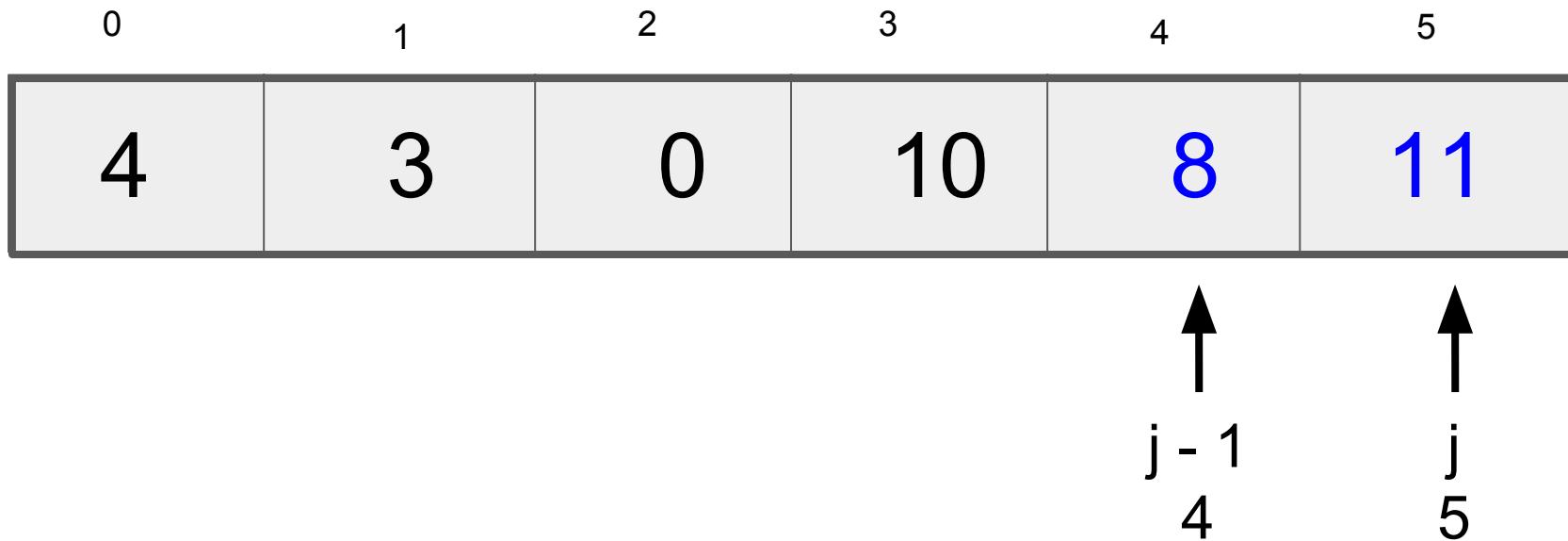


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 6

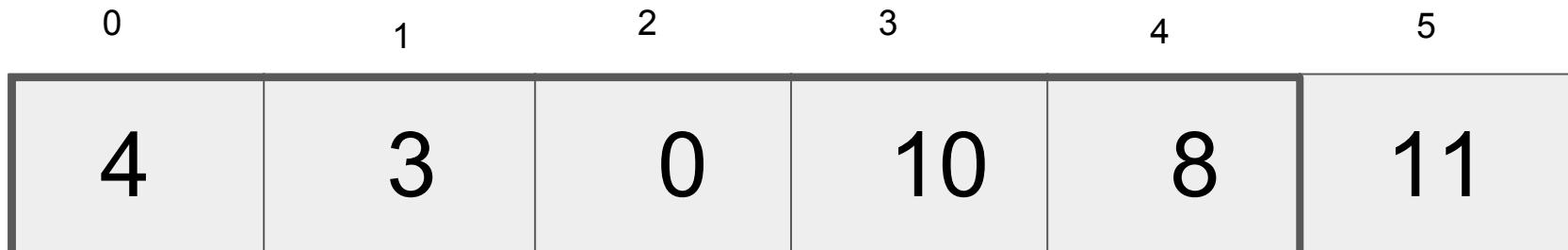


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 5



↑
j - 1
0

↑
j
1

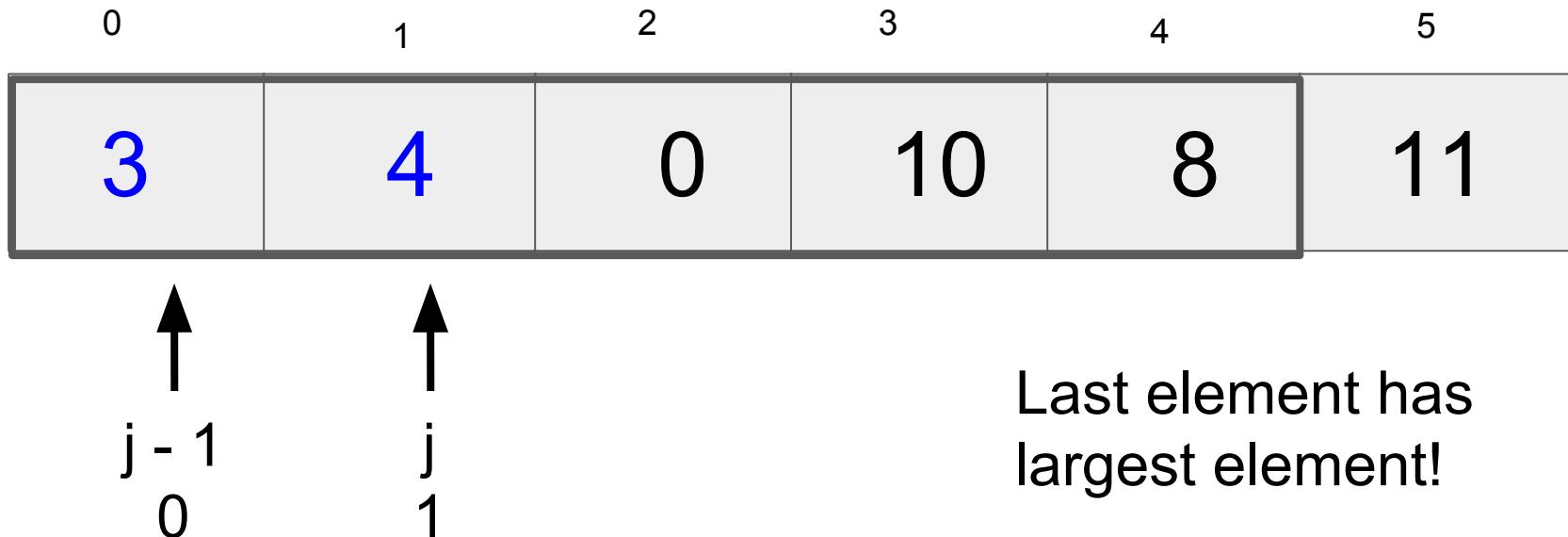
Last element has
largest element!

Reset and compare pairs with shorter list!

What next?

Bubble Sort

len = 5

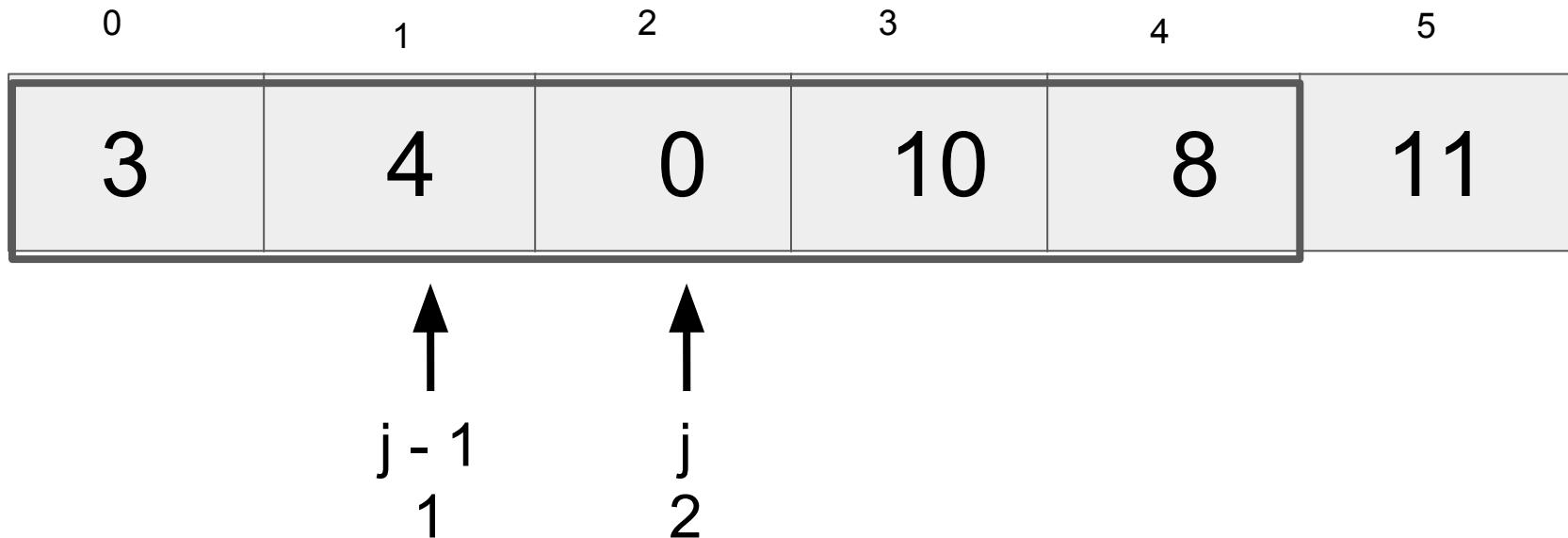


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 5

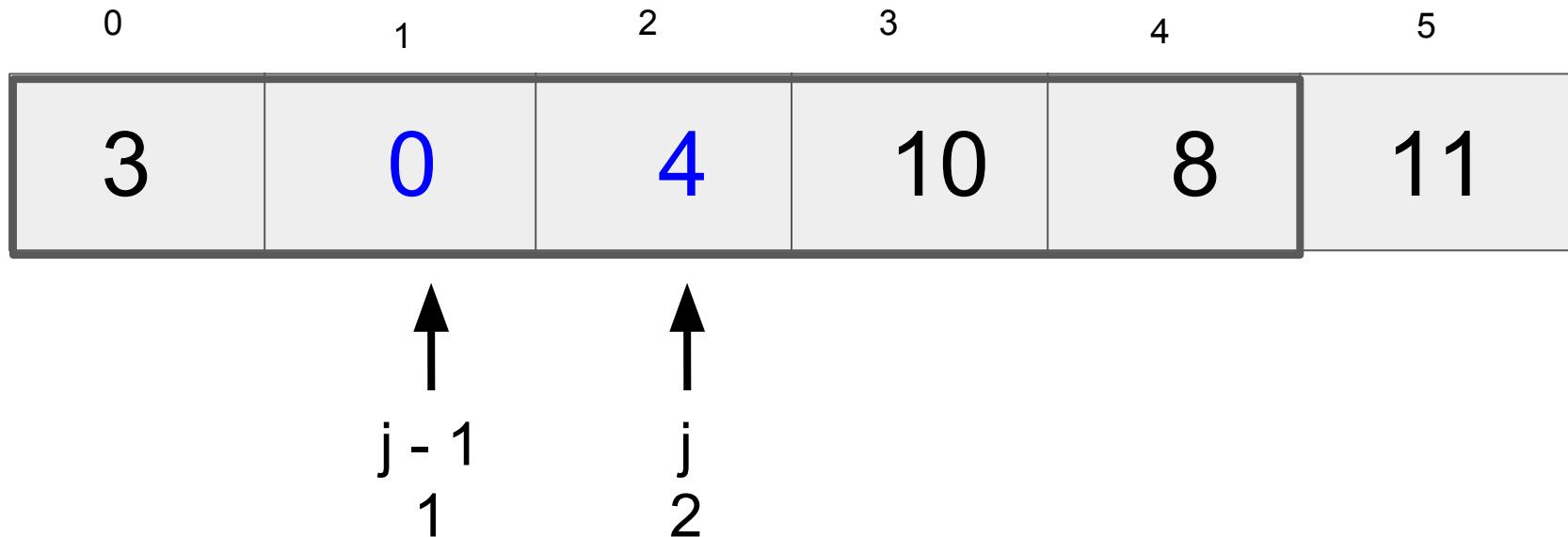


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 5

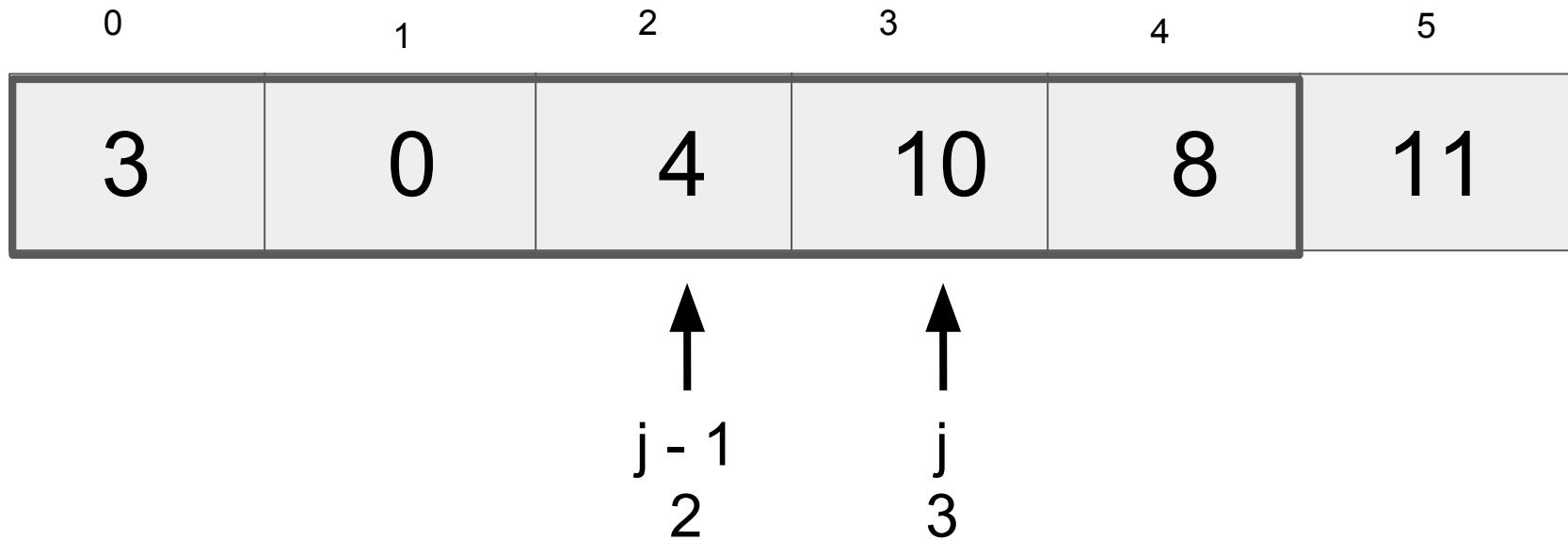


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 5

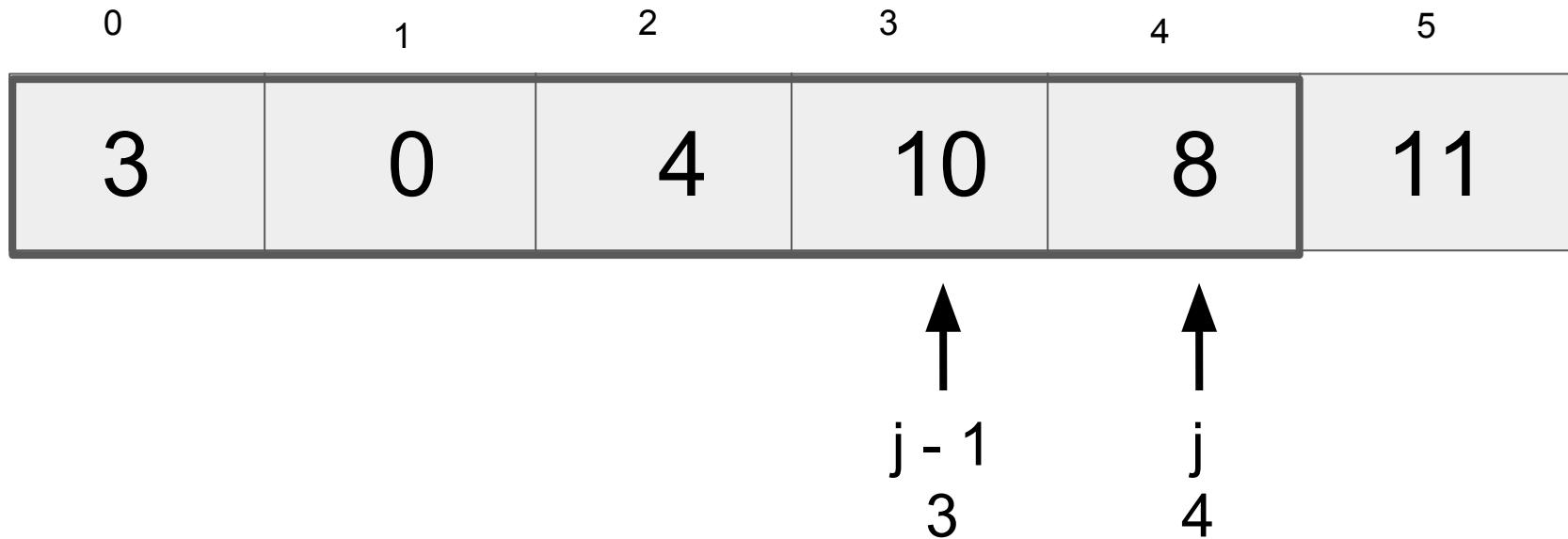


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 5

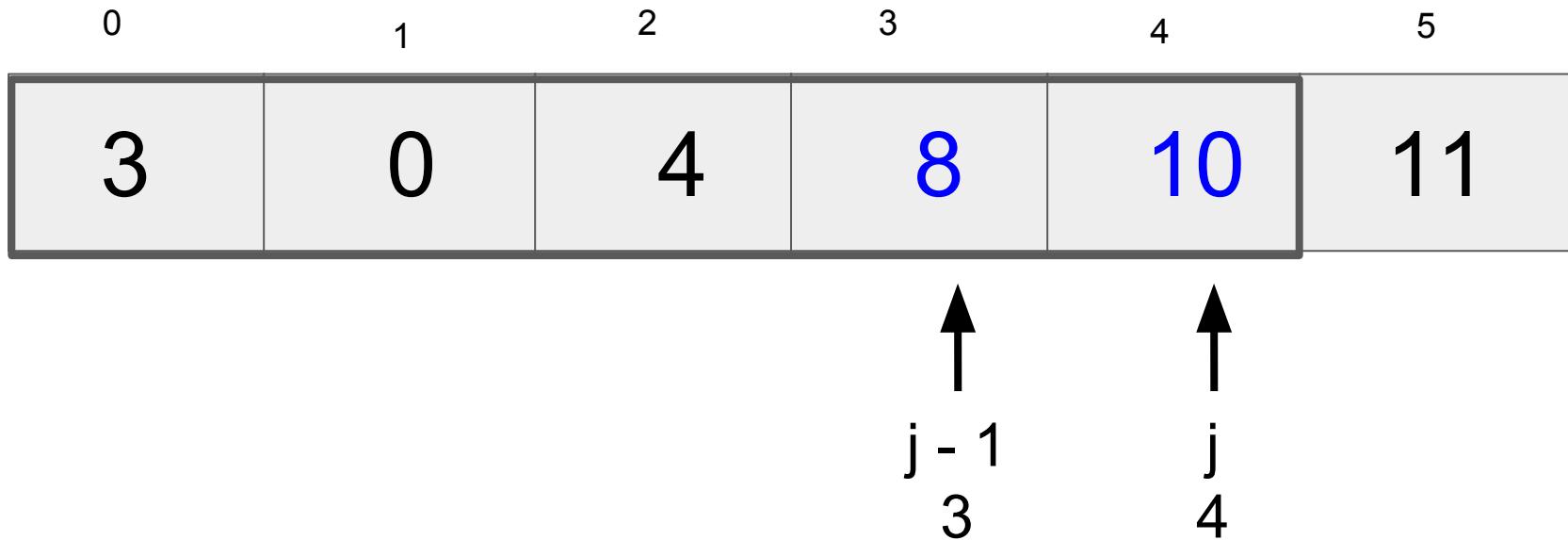


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 5

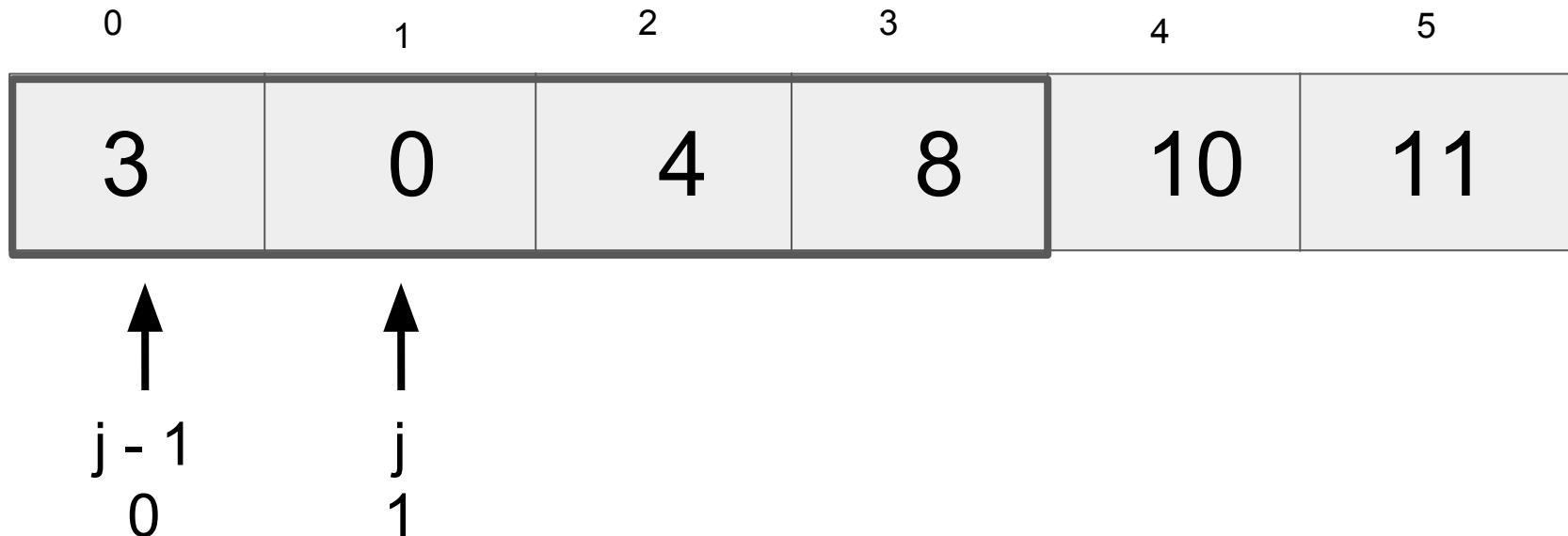


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 4

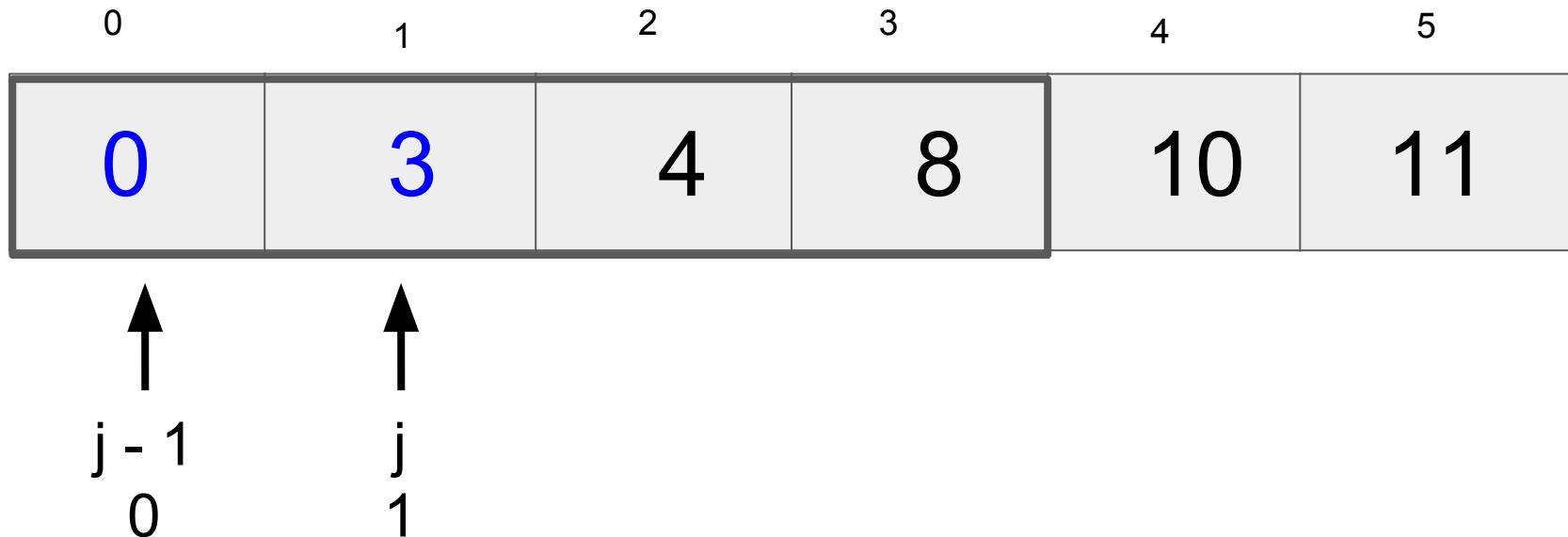


Reset and check pairs with shorter list

What next?

Bubble Sort

len = 4

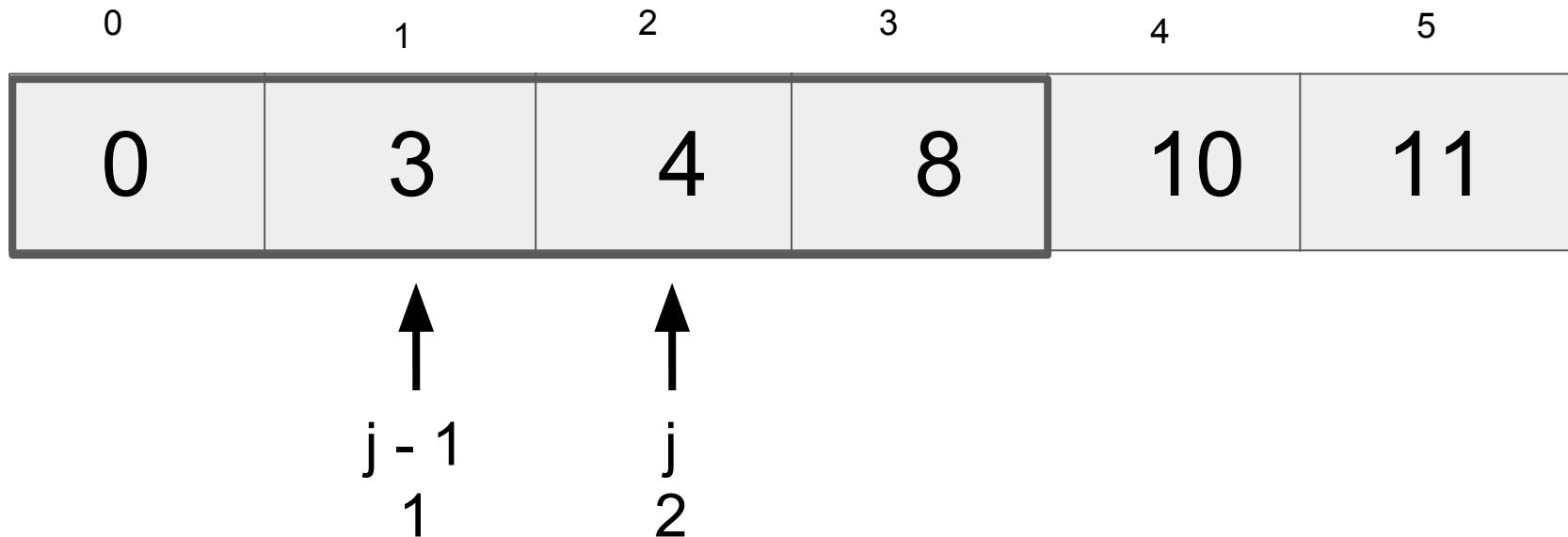


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 4

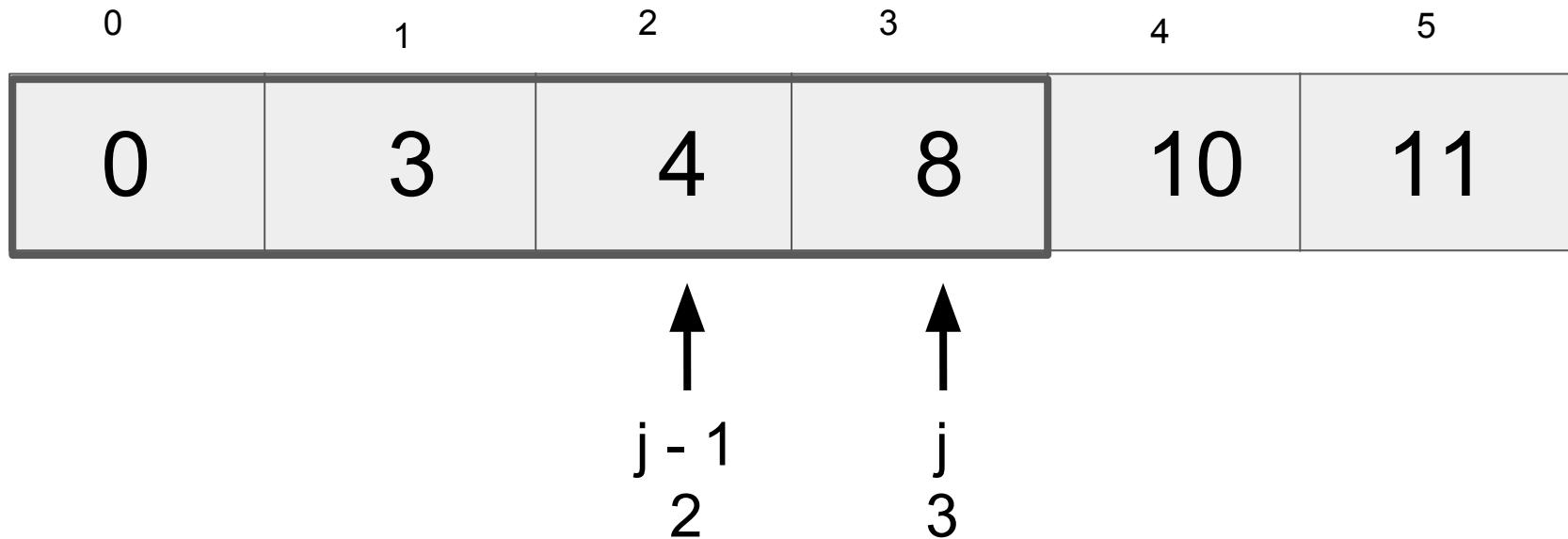


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 4

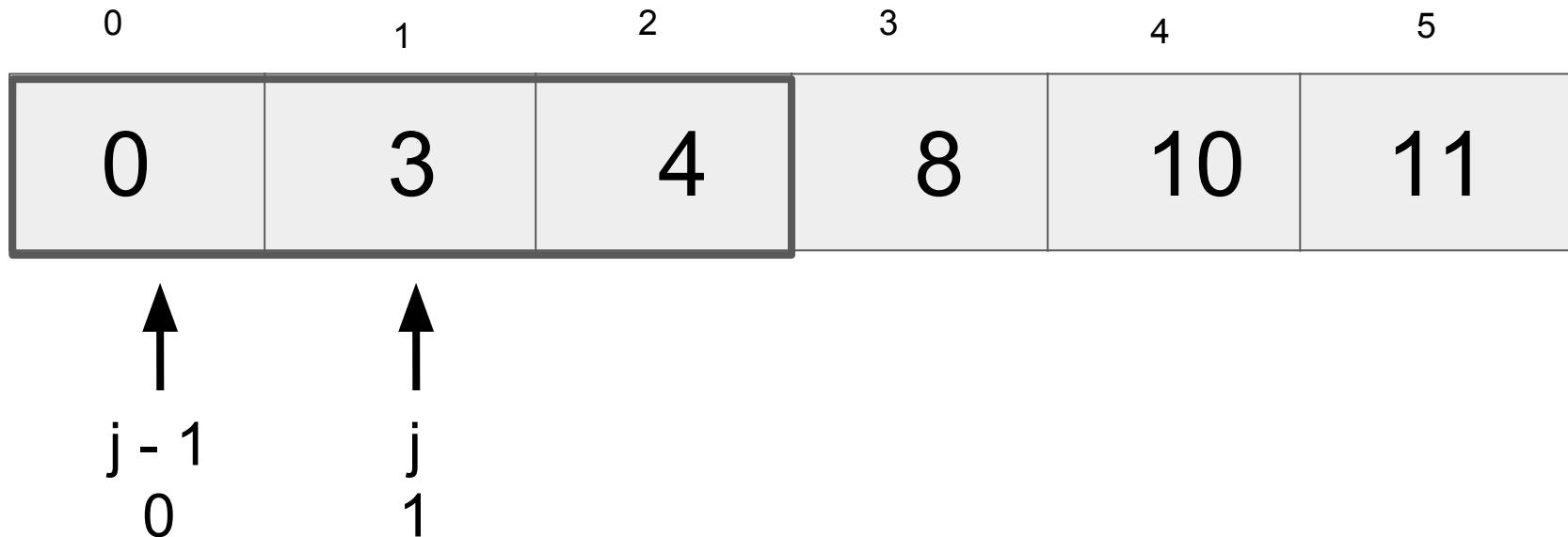


Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 3

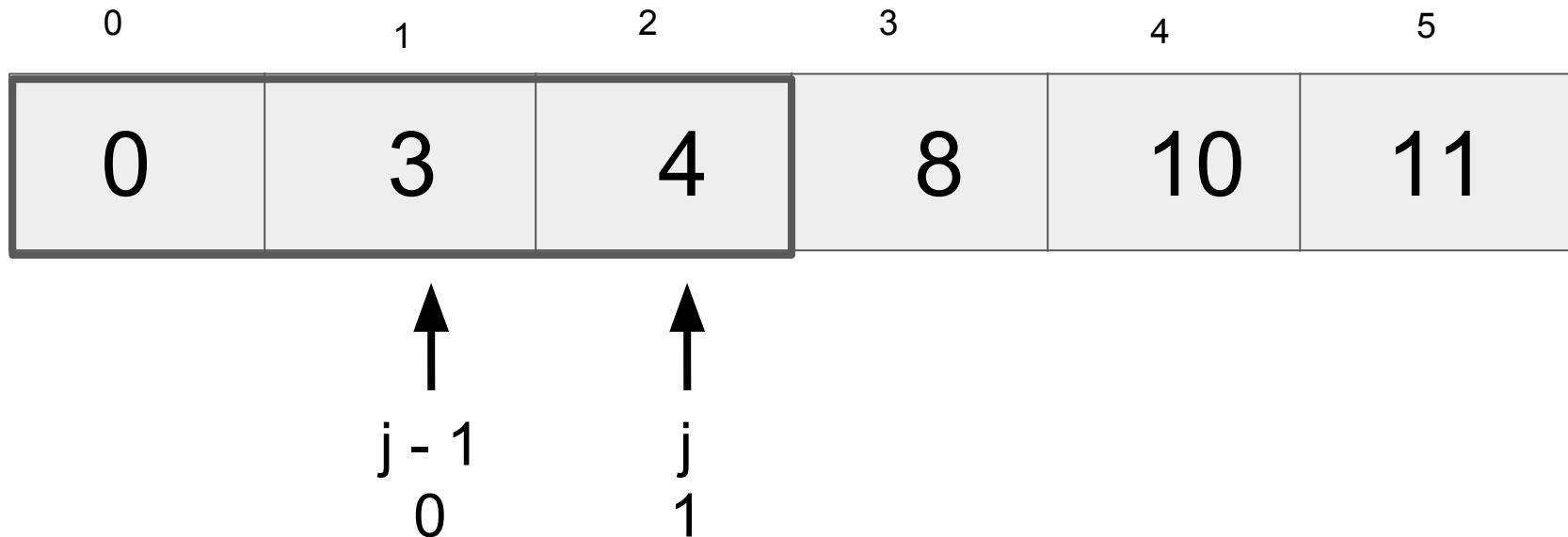


Reset; Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 3

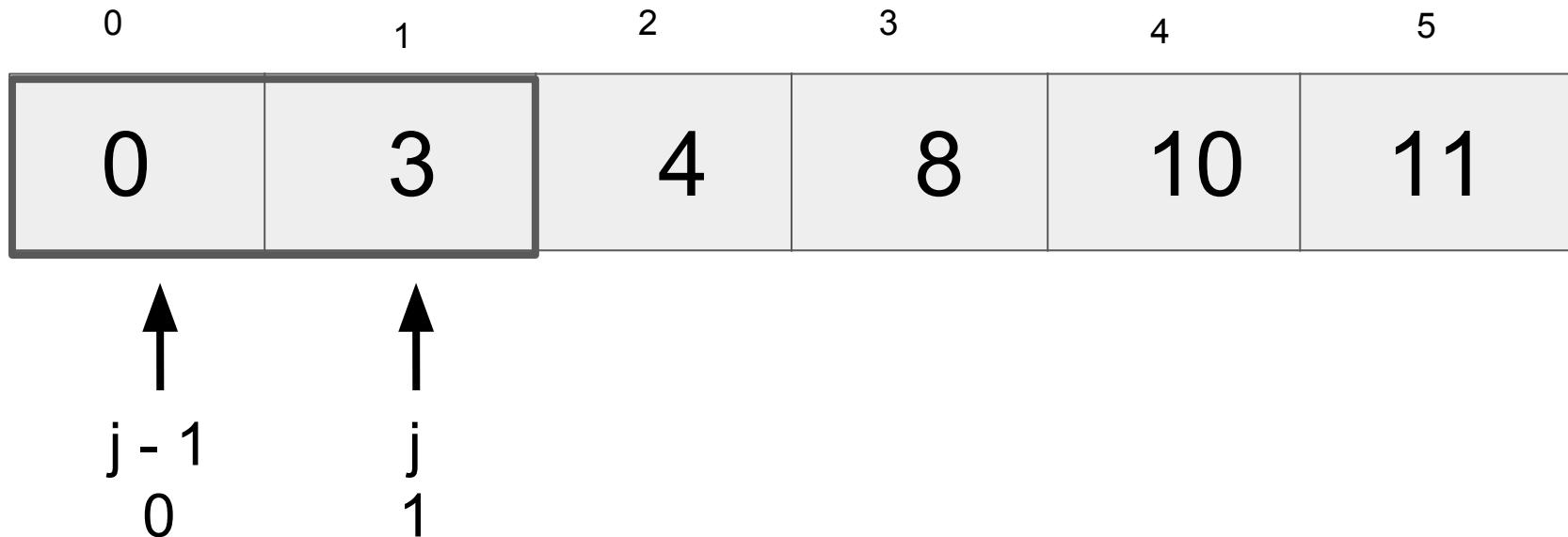


Reset; Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

len = 2



Reset; Compare $j-1$ and j ; Swap if $L[j-1] > L[j]$

What next?

Bubble Sort

Idea: bubble highest values to the end of the list; Check a shorter sublist each time

```
bubbleSort(L):
```

```
    for len in range(len(L), 1, -1):
```

```
        for j in range(1, len): # bubble
```

```
            if L[j-1] > L[j]:
```

```
                swap(j-1, j, L)
```

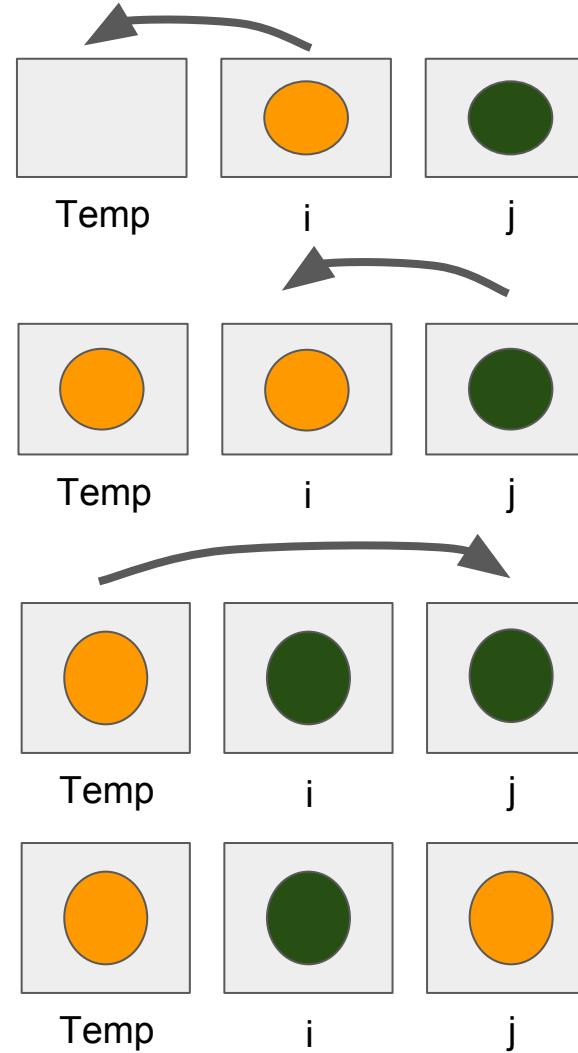
Bubble sort

`swap(i, j, L):`

`temp = L[i] # step 1`

`L[i] = L[j] # step 2`

`L[j] = temp # step 3`



```
10
11
12
13
14
15
16
17 """
18
19 import swap
20 import random
21 import isSorted
22
23 def bubbleSort(L):
24     """
25         Sort the list L in place using bubble sort
26         Param L (list): the list to sort
27         Return: None
28     """
29     for end in range(len(L), 1, -1):
30         for j in range(1, end):
31             if L[j-1] > L[j]:
32                 swap.swap(j-1,j,L)
33                 print("swap", j-1, j)
34
35
36 if __name__ == '__main__':
37     L = [10,4,3,0,11,8]
38     print("Before:", L)
39     bubbleSort(L)
40     print("After:", L, "IsSorted?", isSorted.isSorted(L))
41
42
```

Selection sort and Bubble sort are $O(N^2)$

