

# CS46 Lab 12

Lab problems are an opportunity for discussion and trying many different solutions. They are **not counted towards your grade**, and **you do not have to submit your solutions**. The purpose of this lab is to get more practice with polynomial-time reductions.

1. Show that polynomial-time reductions are *transitive*; that is, show that if  $A \leq_P B$  and  $B \leq_P C$  then  $A \leq_P C$ .
2. Let  $3\text{-SAT}$  be the language that is like  $\text{SAT}$ , except that each clause must have three literals.
  - (a) Show that  $3\text{-SAT} \leq_P \text{SAT}$ .
  - (b) Show that  $\text{SAT} \leq_P 3\text{-SAT}$ .
3. Recall that  $\text{INDEPENDENT-SET} = \{ \langle G, k \rangle \mid G \text{ is an undirected graph that has an independent set of size at least } k \}$ .  
Reduce  $3\text{-SAT} \leq_P \text{INDEPENDENT-SET}$ .