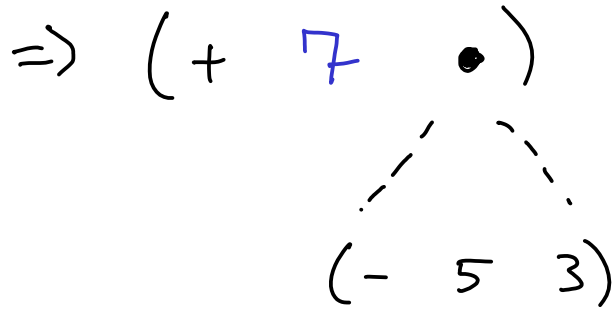
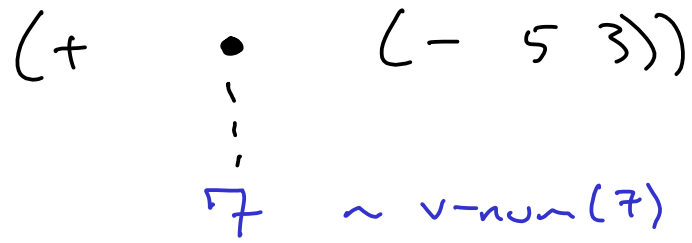
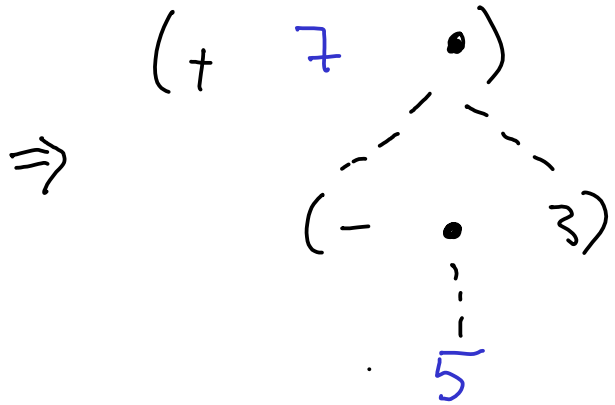
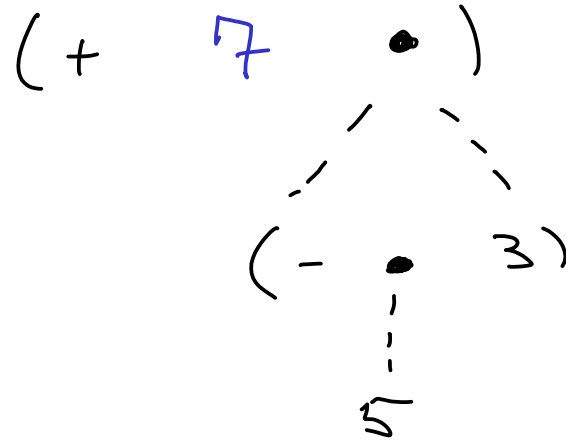


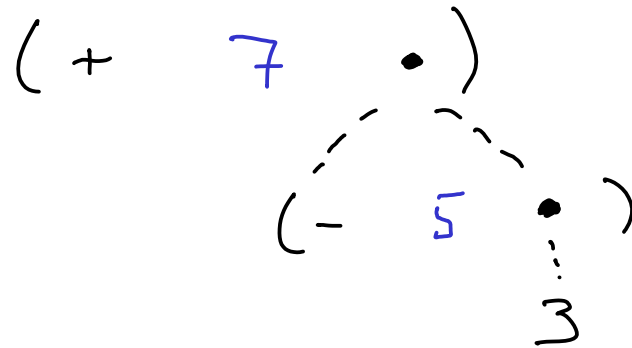
$\Rightarrow$

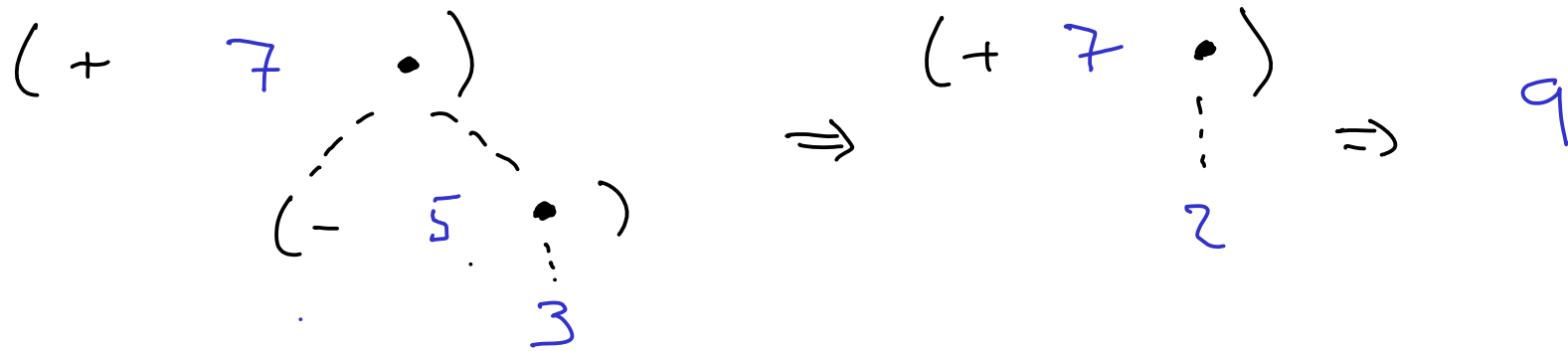


$\Rightarrow$



$\Rightarrow$





Contexts = (op • expr)  
 (op val •)

data Context:

| c-op-left (op::String,  
 right::Expr)

| c-op-right (op::String,  
 left::Value)

Program List < Context >, Value end

List < Context >, Expr

```


data Expr:
  | e-num(n :: Number)
  | e-op(op :: String, left :: Expr, right :: Expr)
end

type Value = Number

fun interp(e :: Expr) -> Value:
  cases(Expr) e:
  | e-num(n) => n
  | e-op(op, left, right) =>
    do-op(op, interp(left), interp(right))
  end
end

fun do-op(op :: String, l :: Value, r :: Value) -> Value:
  ...
end

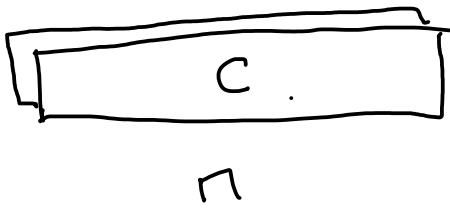
```

 =  
 (op • expr)

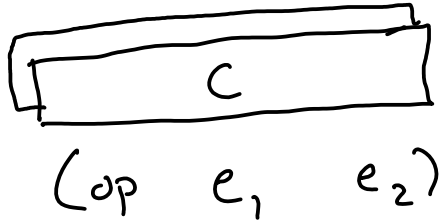
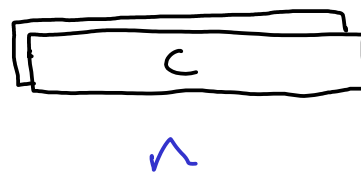
 =  
 (op val •)

type Program = List<Context> Value or Expr

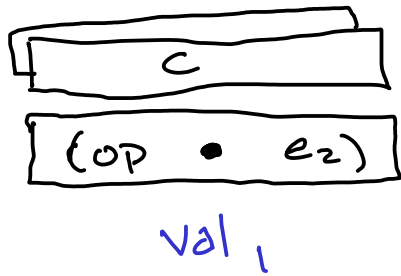
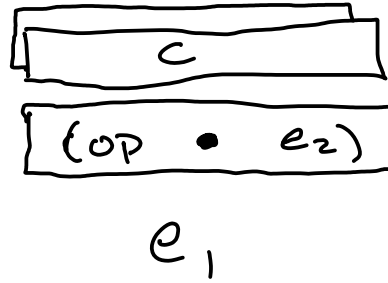
step Program → Program



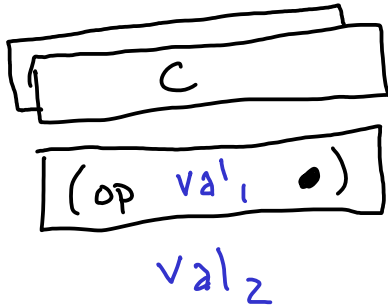
$\Rightarrow$



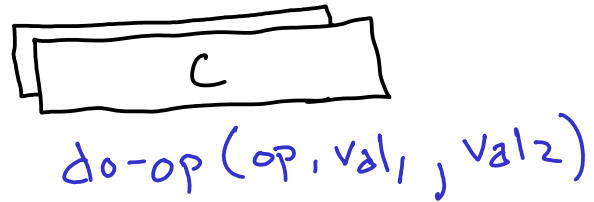
$\Rightarrow$



$\Rightarrow$



$\Rightarrow$



$c$   
(first  $e$ )

$\Rightarrow$

$c$   
(first  $\bullet$ )  
 $e$

$c$   
(rest  $e$ )

$\Rightarrow$

$c$   
(rest  $\bullet$ )  
 $e$

$c$   
(first  $\bullet$ )  
 $v\text{-link}(val_1, val_2)$

$\Rightarrow$

$c$   
 $val_1$

$c$   
(if  $e_1 e_2 e_3$ )

$\Rightarrow$

$c$   
(if  $\bullet e_2 e_3$ )  
 $e_1$

$c$   
 $(if \bullet e_2 e_3)$

$v\text{-true}$

$\Rightarrow$

$c$   
 $e_2$

$c$   
 $(if \bullet e_2 e_3)$

$v\text{-false}$

$\Rightarrow$

$c$   
 $e_3$

$c$   
 $(let (x e) e_b)$

$\Rightarrow$

$c$   
 $(let (x \bullet) e_b)$   
 $e$

$c$   
 $(let (x \bullet) e_b)$

$val$

$\Rightarrow$

$c$   
 $x = val$   
 $e_b$

$c$   
 $x = val$

$v_b$

$\Rightarrow$

$c$   
 $v_b$



x

$\Rightarrow$



lookup(x, c)



(lan(x) e\_b)

$\Rightarrow$



clos(c, x, e\_b)



v\_a

$\Rightarrow$



e\_b

Do you see the issue?  
(see next lecture, don't implement this :))

$v_f = \text{clos}(c', x, e_b)$